Renewable Energy in Europe – What is Needed, What is Possible?

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- Energy and Climate The CO₂-Problem
- Where is the Energy used? "Sectors"
- Greenhous-gas free Energy Supply "100% Renewable Energy"
- Storage Requirements
- Storage Technologies & cost
- Soutions to the Storage problem



Global Heating as a Consequence of the Cumulated CO₂-Emission



Quelle: IPCC-AR5 Climate Change 2014 Synthesis Report

Consequences for Germany?



VDI-Sonderdruck 2021, Regenerative Energien

Primary Energy – Final Energy – Net Energy Units: Joule, J, kJ, 1 kWh = 3600 kJ

Primary Energy: Energy stored in the originally ocurring form ("Energy source"),

- Chemical energy of coal, oil, Biomass or natural gas
- Transformed from other energy carriesr like Solar, Wind,

Secondary Energy: Supplied by transformation of primary energy, for instance:

- Coal, Gas, Nuclear Energy to Electricity
- Crude oil to fuel (petrol, diesel fuel, ...).

Considerable losses usually occur in this process.

Final Energy: Energy useable by consumer, (electricity, petrol, diesel) after "transfer", (there my be transfer losses).

Net Energy (Useful Energy): Actually used Energy (e.g. light, mechanical power, ...), i.e. final energy minus transformation losses (e.g. fuel to heat or fuel to motion) occuring by consumer.

Energy Fluxes, Germany 2020 Figures in Petajoule, 1 PJ = 10¹⁵ Joule (278 GWh)



Der Anteil der erneuerbaren Energieträger am Primärenergieverbrauch liegt bei 16,5 %. Abweichungen in den Summen sind rundungsbedingt.

* Alle Zahlen vorläufig/geschätzt.

29,3 Petajoule (PJ) ≙1 Mio. t SKE

Quelle: Arbeitsgemeinschaft Energiebilanzen 09/2021

Source: Arbeitsgemeinschaft Energiebilanzen 09/2021

What is a Peta Joule (PJ)?

Answer 1: 1 PJ = 10^{15} Joule or 278 GWh or 278 Mio. kWh



Answer 2: Daily Energy consumption of a human: ≈2400 Kilocalories or ≈10.000.000 Joule (10.000 kJ, 10⁷J)

All Germans (83 Mio.) per year (365 Tage): "Consume" 3.10¹⁷ J or **300 PJ** as food.

Corresponds to ca. **1/40** of the annual German Total Primary Energy usage of \approx 12.000 PJ.

Primary Energie Use in Germany



nergiebilanzen (2019a), *vorläufige Angaben

Renewable Energy 2020: 1700 PJ (≈17%)

Source: Agora Jahresauswertung: Die Energiewende im Stromsektor: Stand der Dinge 2019

Energy Supply from Renewable Sources, Germany, 2020, total: 470 TWh or 1700 PJ



¹ mit biogenem Anteil des Abfalls

Quelle: Umweltbundesamt (UBA) auf Basis AGEE-Stat Stand 10/2021

² Stromerzeugung aus Geothermie etwa 0,2 TWh (nicht separat dargestellt) ³ Verbrauch von EE-Strom im Verkehretwa 4,9 TWh

Abweichungen bedingt durch Pundungen

Abweichungen bedingt durch Rundungen

Source: Umweltbundesamt auf Basis AGEE-Stat: https://www.umweltbundesamt.de/themen/klima-energie/erneuerbare-energien/erneuerbareenergien-in-zahlen#uberblick

Fraction of RE in the Sectors Electricity, Heating and Transport, Germany 1990 - 2020



Source: Umweltbundesamt: https://www.umweltbundesamt.de/themen/klimaenergie/erneuerbare-energien/erneuerbare-energien-in-zahlen#uberblick 100% Renewable Energy (RE) in Germany, Europe, the World

See also: Lecture by Hans-Martin Henning

0. Approximation: Today (2022/2023 in D) we have ≈17% fraction of RE from the total use of primary energy
→ does it mean that an incease by a Faktor 1/0.17 ≈ 6 is necessary for 100% RE??

The matter is more complicated!

Problems:

Renewable Energy is "much better" than fossil Energy

- 1) **Primary Energie** is not a good measure, actually we are interested in **Net Energy**. Therefore we need to look at the sectors individually.
- 2) The RE supply is very variabel, we need to look at **Energy-mix**, **Storage** and **Excess-capacity**.

Primary Energy use in Germany in the Sectors



For 2018, Source: Arbeitsgemeinschaft Energiebilanzen

Looking into the Sectors 1: Electricity

Primary Energy Use 2018:4640 PJ (35,4% of PEU)Net inland 2000 PJ Electricity (\approx 64 GW x 1 yr) \approx 45% RE:Final Energy \approx Primary Energy \approx 55% Fossil+Nuclear:Final Energie \approx 0.35*Primary Energy

→ ≈23% of Primary Energie from Renewable E.

≈77% of Primary Energy from Fossil + Nuclear

→ 100% EE require ≈2000 PJ Energy from Wind, Solar, ... Only ≈45% of present day Primary Energy use for Electricity!



Looking into the Sectors 1: Total Electricity Usage in Germany 1990-2020 in TWh (=Billion KWh)



* Berücksichtigung des Stromhandelssaldos

** 2020 vorläufig; Ziel 2020: Energiekonzept der Bundesregierung 2010:

Senkung des Bruttostromverbrauchs um 10 % gegenüber 2008

Quelle: Umweltbundesamt auf Basis AG Energiebilanzen, Sondertabelle Bruttostromerzeugung in Deutschland von 1990 bis 2020 nach

Energieträgern, Stand 02/2021

Source: Umweltbundesamt: Sondertabelle Bruttostromerzeugung in Deutschland 1990-2020

Looking into the Sectors 2: Traffic

Primary Energy usage 2018: 2540 PJ (19,4%)

- \approx 10% Trains, Tram Final Energy \approx Primary Energy
- \approx 90% Combustion engines: Final Energy \approx 0,2*Primary Energy

Replacement by:

Final Energy = 0,8*Primary Energy

- → ≈10% (260 PJ) alread electrified (Trains, Tram)
 - \approx 90% (2280 PJ) Combustion engines
 - \rightarrow Battery electrical power
 - → 570 PJ

Electric cars

→ 100% RE requires only \approx 830 PJ Just \approx 30% of today's 2000 Primary Energy usage in the traffic sector 0 \rightarrow 570 PL (c2, 20%) additional Electricity

→ 570 PJ (ca. 20%) additional Electricity

See also Lecture by: Maximilian Fichtner "The transformation of propulsion"

Remarks:

H₂-cars: +80% additional electricity Synthetic fuels: +200% additional Electricity





Looking into the Sectors 4: Industry, Mining, Bussines & Trade (without electricity)

Primary Energy use 2018: 4100 PJ (31,3%)

Many different Processes

→ Energy requirement of (additional) electricity difficult to estimate, assume: 1000 PJ

(similar Faktor: Used Energy/Primary Energy as in Transport, Domestic)

Rest via Recycling (non energetic consumption), Biomass, Fossil Energy + CCS

→ Required \approx **1000 PJ** additional Electricity (e.g. for H₂)

ca. 50% additional Electricity required





More Energy required as Electricity ($2000 \rightarrow 3800 \text{ PJ}, +90\%$)

Problem: Variability of RE \rightarrow Storage

*Source: Agora Jahresauswertung: Die Energiewende im Stromsektor: Stand der Dinge 2019

Question: How much Storage Capacity is Required for 100% Electricity Supply from Renewable Sources?

Measure of Storage Size: SupplyTime = $\frac{\text{Stored Energy}}{\text{Mean Consumption}}$

Some Answers: 3 Months (!)

Better Answers:

Depends on Energy Mix (i.e. Wind – Solar) Depends on Excess capacity* Depends on desired Reliability of Supply

Let us have a look on these topics ...

*Term "Excess Capacity" will be explained later

See also: Lecture by Franz W. Iven

The "Meteorological based Energy Eqilibrium Testing – Model" (MEET)



Potential of Wind and Solar Power in Europe (Mean 2000 to 2010)

Annual PV electricity generation potential

Annual wind-electricity generation potential





Percentage: Fraction of generated kWh's of 8760 kWh

Annual/Weekly Electricity Demand in Europe (MEET)





Required Storage Capacity (100% renewable),



→ Combination of Wind + Solar reduces required storage capacity by a factor of >4 Still large storage requirement (ca. 2 weeks)!



Required Storage Capacity vs. Renewable Energy Fraction

Tröndle 2014



What is **Excess Capacity**?

All Electricity supply systems encompass a (annual mean) production capacity exceeding größer the (annual mean) consumption. thus:

Excess capacity = $\frac{\text{Installed Capacity} - \text{Mean Consumption}}{\text{Mean Consumption}} \cdot 100\%$

Example: Germany has had 100-120% Excess Capacity since decades (Without Renewable Energy!).

Do not confuse with Capacity Factor

Typ.

Renewable Energy is usually available only during a fraction of time, thus:

Capacity	Eactor - Instal	led Power · 8760 hours	100%
Capacity	/ T actor – – – – – – – – – – – – – – – – – – –	Annual Harvest	· 100 /0
Capacity Factors:	Solar Germany	10%	
	Solar S. Europe:	20%	
	On shore Wind: Off shore Wind:	20% 40%	

Required Storage vs. Excess Capacity



Cost of Power + Storage

including excess cap Breakdown of cost:



Storage Technologies for Electric Energy



Diffusion: The Pfeffer Cell Apparatus

Wilhelm Pfeffer 1877

van't Hoff's law:





The Osmotic Pressure of Salt Solutions

In first approximation, i.e. for diluted solutions, the osmotic pressure Π of two salt solution with salt concentration (in moles/m³) c₁, c₂ is given by Van't Hoff's law (Van't Hoff 1887):

$$\Pi_{VH} = \mathbf{n}_{i} \cdot \mathbf{R} \cdot \mathbf{T} \cdot \left(\mathbf{c}_{2} - \mathbf{c}_{1}\right)$$

with:

n_i = Van't Hoff factor denoting the number of ions per dissolved molecule (n_i = 2 for NaCl)

R = Universal gas constant: 8.31 J/(mole K)

T = Absolute temperature, e.g. 293.2 K

For concentrated solutions the ,activity' of solute (salt) and solvent (water) has to be used. This can lead to large deviations from V.H. Law

van't Hoff J.H. (1887), Die Rolle des osmotischen Druckes in der Analogie zwischen Lösungen und Gasen, Zeitschrift für Physikalische Chemie, Band 1U, Heft 1, 481–508, ISSN (Online) 2196-7156, ISSN (Print) 0942-9352, DOI: https://doi.org/10.1515/zpch-1887-0151

The (theoretical) Energy Storage Density of Osmotic Plant (1)

Amount E of energy released from an initial brine volume V₀ containing an initial salt concentration c_0 giving rise to an initial osmotic pressure Π_0 : Energy dE released upon injection of a fresh water volume dV and keeping in mind that the salt concentration c = n/V reduces with the amount of fresh water admitted to the osmosis cell:

 $dE = \Pi(V)dV$ $E(V) = \int_0^V \Pi(V')dV'$

Assuming a linear correspondence between osmotic pressure and salt conc.

$$\Pi(c) \propto c$$
 and $c(V) = c_0 \cdot V_0 / (V_0 + V)$ we obtain:

$$\Pi(\mathsf{V}) = \Pi_0 \cdot \frac{\mathsf{v}_0}{\mathsf{V}_0 + \mathsf{V}}$$

and:

$$\begin{split} \mathsf{E}(\mathsf{V}) &= \int_{0}^{\mathsf{V}} \Pi(\mathsf{V}') \mathsf{d}\mathsf{V}' = \Pi_{0} \mathsf{V}_{0} \int_{0}^{\mathsf{V}} \frac{\mathsf{d}\mathsf{V}'}{\mathsf{V}_{0} + \mathsf{V}'} \\ &= \Pi_{0} \mathsf{V}_{0} \cdot \mathsf{ln} \bigg(\frac{\mathsf{V}_{0} + \mathsf{V}'}{\mathsf{V}_{0}} \bigg) \Big|_{0}^{\mathsf{V}} = \Pi_{0} \mathsf{V}_{0} \cdot \mathsf{ln} \bigg(\frac{\mathsf{V}_{0} + \mathsf{V}}{\mathsf{V}_{0}} \bigg) = \Pi_{0} \mathsf{V}_{0} \cdot \mathsf{ln} \bigg(1 + \frac{\mathsf{V}}{\mathsf{V}_{0}} \bigg) \end{split}$$

The (theoretical) Energy Storage Density of Osmotic Plant (2)

For very small volumina V << V_0 of added fresh water this simplifies to

While for very large volumina V >> V_0 we get approximately:

$$\mathsf{E}(\mathsf{V}) \approx \Pi_0 \mathsf{V}_0 \cdot (1 + \frac{\mathsf{V}}{\mathsf{V}_0} - 1) = \Pi_0 \mathsf{V}$$

$$\mathsf{E}(\mathsf{V}) \approx \Pi_{\mathsf{0}} \mathsf{V}_{\mathsf{0}} \cdot \mathsf{ln}\left(\frac{\mathsf{V}}{\mathsf{V}_{\mathsf{0}}}\right) \propto \mathsf{ln}(\mathsf{V})$$

 \rightarrow The amount of mixing energy for a given amount of salt solution can become infinite if infinite amounts of fresh water are available.

However the interesting quantity is the **energy density** $E(V)/(V+V_0)$, which can be achieved in a particular configuration.

For a 'one reservoir' configuration the energy density Q is given by:

$$Q(V) = \frac{E(V)}{V + V_0} = \Pi_0 V_0 \cdot \frac{ln\left(\frac{V + V_0}{V_0}\right)}{V + V_0}$$

The (theoretical) Energy Storage Density of an Osmotic Plant (3)



Comment: Pressure [N/m²] = Energy Density [Nm/m³ = J/m³]

Measured Osmotic Pressures of Some Salts



Sketch of an Osmotic Storage Plant Discharge Operation



See e.g.: Dinger F., Tröndle T., Platt U. (2013), Osmotic power plants and their potential, J. Renewable Energy, (Hindawi Publishing Corp.) Vol. 2013, Article ID 496768, doi.org/10.1155/2013/496768.

Helfer F., Lemckert C., Anissimov Y.G. (2014), Osmotic power with Pressure Retarded Osmosis: Theory, performance and trends – A review, J. Membrane Science 453, 337–358.

Sketch of an Osmotic Storage Plant Charging Operation



Alternative Designs of Osmotic Storage Plant (Charging Operation) А **Pressure Exchanger Plant** Membrane Pump 1) Use ,external' supply Reservoir 1 of fresh water (River, ground water) Reservoir 2 C_1 Ca **Pressure Exchanger**



- 2) Put salt water reservoir ,inside' fresh water reservoir
- → Reservoir level stays constant

Energy Density and Efficiency of Storage Technologies

Technology	Efficiency	Energy density	Remark
		kWh/m³	
Pump storage	75-80%	≈1*	at ∆h=350m
Compressed air storage CAES	54-70%	≈3*	at p=13 MPa (130 bar)
Li Ion Battery	70-95%	≈200	
Hydrogen	34-44%	≈2.6 (1.6*)	Atm. pressure
		≈340 (200*)	at p=13 MPa (130 bar)
Methane (Power-to-Gas)	30-38%	≈400*	at p=13 MPa
Osmotic storage	40-60%	≈12*	MgCl ₂

*including electricity re-conversion losses

Further possibilities:	Use biomass as storage	
	(<10% of annual consumption required)	

Hambacher Loch" Loch" Hambach Surface Volume: ca. 10 Mrd m³ Mine (18.6 km³ in 2040) → At 11.6 kWh/m³ Stored Energy: >1.10¹⁴ Wh or 100 TWh or Germany for ≈60 days





Total annual electricity consumption in Germany: 600 TWh

See:

https://en.wikipedia.org/wiki/ Hambach_surface_mine

https://de.wikipedia.org/wiki/ Tagebau_Hambach

Luther G. and Schmidt-Böcking H., The role of short-term storage like hydropower in abandoned opencast mines in the energy transition.

Other (realistic) "Storage" Technologies

Short-term storage (<24h): Small amount of energy, but turnover ca. 100 times/year

 \rightarrow Pump storage, Osmotic storage, Batteries

Long-term storage (>24h) turnover few times/year

→ 1) Pump storage, Osmotic storage,
2) Gas turbine with Bio-gas:

Equivalent cost of storage: 1-2 €/kWh

ca. 6% of (present day) electricity generation from Biogas, but only about 0,25-1% of annual generation are required as long-term storage .

The available amount of bio- gas (Germany) would be sufficient to fill the storage about 5-times/year (at twice the present electricity demand).

Model result: only 2-3 times required (at 150% capacity)

→ Only about 1% of the electricity demand pass the storage

100% Renewable Energy Supply, Significance for Germany (1)

Assume: 150% Capacity (50% Excess Capacity)

30%/70% Wind/Solar (mean. power: 9/7, 56%/44%)

Wind: Annual mean =30% of installed peak power Solar: Annual mean =10% of installed peak power

Germany: \approx 60 GW → 114 GW mean Electricity consumption 100% EE (+90%) → \approx 170 GW incl. 50% Excess Capacity

→ \approx **750 GW Solar** (75 GW MW) + **320 GW Wind** (96 GW MW)

→ 2021 in G. installed: 56 GW Solar, 62 GW Wind (incl. ≈8 GW offshore)

 \rightarrow Solar x13; Wind x5 (rough calculation) Total: x9

Includes Elektromobility, Industry & Heating!

100% Renewable Energy Supply, Significance for Germany (2)

 \approx **750 GW Solar** (75 GW MW) + \approx **320 GW Wind** (95 GW MW)

Required Area for Solar at 200 W/m²: 3.750 km²

Potential G.: 6.000 km² Roof Area, 12.000 km² From



Required Area for Wind at 26 MW/km² (mean value)⁽²⁾ \rightarrow 12.500 km², \approx 3.5% of the total area (357.600 km²)

Compatible with 2%

Max useable on-shore Wind Power: 1800 GW³

Reduction due to off-shore Wind Energy, Energy Imports (H₂, Electricity, Synthetic Fuels)

¹see e.g. Behnisch et al. 2020, doi: DFNS/2020_12_DFNS/025_behnisch.pdf
 ²Bons et al.(2019), Flächenanalyse Windenergie an Land, Abschlussbericht, CLIMATE CHANGE 38/2019 EVUPLAN, Forschungskennzahl 37EV 16 117 0 FB000157.
 ³Miller et al. 2015, www.pnas.org/cgi/doi/10.1073/pnas.1408251112



Conclusions

- 100% renewable energy is well possible with existing technologies (there is no time anyway to develop fundamentally new technologies)
- Our energy System must be converted to (>80%) carbon free within the coming two decades in order to avoid a climate catastrophy
- Renewable energy can be supplied at competitive cost
- Energy storage is probably less critical than frequently implied
- Osmotic storage can provide storage densities of up to ≈12 kWh/m³, equivalent to a >4000 m altitude difference pump storage plant, about one order of magnitude more than conventional pump storage plants
 - No need for mountains

 \rightarrow lower investment, (in particular if not too much power is required), much more freedom in siting the plant

- However, (somewhat) lower efficiency ($\leq 60\%$ vs. $\leq 80\%$)

Thank You!

Some Further Literature

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Studie-Wege-zu-einem-klimaneutralen-Energiesystem-Update-Klimaneutralitaet-2045.pdf

Anthropogenic CO₂-Emission 1958-2018 in GtC



Sources of Anthropogenic CO₂-Emissions 1958-2018 in GtC



Friedlingstein P., et al. 2019, Earth Syst. Sci. Data, 11, 1783–1838, https://doi.org/10.5194/essd-11-1783-2019

Cumulative Anthropogenic Emission of (fossile) CO_2 (in GtC) since 1850



Source: Carbon Dioxide Information Analysis Center (CDIAC.com) and values of atmospheric CO_2 concentrations from Mauna Loa, as well as other locations. Excluding carbon emissions from change of land use and deforestation.

Which Salt(s) to Use?

Solubility data and osmotic pressures of a number of salts dissolved in water at 25°C (data from Cath et al. 2006)

Solute	Solubility (293.2 K) (g/l)	Molecular weight (g/mole)	Molar solubility (mole/l)	Van't Hoff Const. n _i	Osmotic pressure van't Hoff law (bar@5M)	Measured Osmotic pressure (bar@5M)
MgCl ₂	543	95.21	5.70	3	371.7	1130
CaCl ₂	745	110.98	6.71	3	371.7	1000
NaCl	358	58.44	6.13	2	247.8	310
KCI	347	74.55	4.65	2	247.8	220
		-	Γ	Much hiaher	than van't Hoff	

Much higher than van't Hoff Formula would suggest!

Cath T.Y., Childress A.E., Elimelech M. (2006), Forward osmosis: Principles, applications, and recent developments, J. Membrane Science 281, 70–87.

Hamdan M., Sharif A.O., Derwish G., Al-Aibi S., Altaee A. (2015), Draw solutions for Forward Osmosis process: Osmotic pressure of binary and ternary aqueous solutions of magnesium chloride, sodium chloride, sucrose and maltose, J. Food Engineering 155, 10–15.

Maximum Energy Storage Density of an Osmotic Plant (1)

The maximum energy density (MED) is reached at:

$$\frac{dQ(V)}{dV} = 0 = \frac{d}{dV} \left(\frac{E(V)}{V + V_0} \right) = \Pi_0 V_0 \cdot \frac{d}{dV} \left(\frac{\ln\left(\frac{V + V_0}{V_0}\right)}{V + V_0} \right)$$

Equivalent to:

$$0 = \frac{d}{dV} \left(\frac{\ln\left(\frac{V + V_0}{V_0}\right)}{V + V_0} \right) = -\frac{\ln\left(\frac{V + V_0}{V_0}\right) - 1}{\left(V + V_0\right)^2}$$

 \rightarrow (since V>0 and V₀>0) the volume for maximum energy density, V_{MED} is:

$$\ln\left(\frac{V_{0} + V_{MED}}{V_{0}}\right) = 1 \iff \frac{V_{MED}}{V_{0}} + 1 = e \iff V_{MED} = V_{0}(e-1) \approx 1.718 \cdot V_{0}$$

 \rightarrow The MED is:

he MED is:

$$Q_{1} = \frac{E(V_{MED})}{V_{MED} + V_{0}} = \Pi_{0}V_{0} \cdot \frac{\ln\left(\frac{V_{0} + V_{MED}}{V_{0}}\right)}{V_{MED} + V_{0}} = \Pi_{0}V_{0} \cdot \frac{\ln\left(\frac{eV_{0}}{V_{0}}\right)}{eV_{0}} = \frac{\Pi_{0}}{e}$$

Maximum Energy Storage Density of an Osmotic Plant (2)

Depending on the assumptions there are 3 types of storage density:

- 0) Precipitation of salt is allowed, thus c=const. during charge/discharge
- 1) "fresh water" is taken/discarded from/to well, river, or ocean
- 2) "fresh water" is taken from another storage reservoir, this needs to have at least a volume of $V_{\rm MED}$

$$\begin{aligned} & \mathsf{Q}_{0} = \Pi_{0} \left[\mathsf{Pa} = \frac{\mathsf{N}}{\mathsf{m}^{2}} = \frac{\mathsf{Nm}}{\mathsf{m}^{3}} = \frac{\mathsf{J}}{\mathsf{m}^{3}} \right] \\ & \mathsf{Q}_{1} = \frac{\mathsf{E} \big(\mathsf{V}_{\mathsf{MED}}\big)}{\mathsf{V}_{\mathsf{MED}} + \mathsf{V}_{0}} = \frac{\Pi_{0}}{\mathsf{e}} \approx 0.37 \cdot \Pi_{0} \Rightarrow \\ & \mathsf{Q}_{2} = \frac{\mathsf{E} \big(\mathsf{V}_{\mathsf{MED}}\big)}{2\mathsf{V}_{\mathsf{MED}} + \mathsf{V}_{0}} = \frac{\mathsf{E} \big(\mathsf{V}_{\mathsf{MED}}\big)}{2\mathsf{V}_{0} \left(\mathsf{e} - 1\right) + \mathsf{V}_{0}} = \frac{\mathsf{E} \big(\mathsf{V}_{\mathsf{MED}}\big)}{2\left(\mathsf{e} - 1\right)\mathsf{V}_{0}} = \frac{\Pi_{0}\mathsf{V}_{0}}{2\left(\mathsf{e} - 1\right)\mathsf{V}_{0}} = \frac{\Pi_{0}}{2\mathsf{e} - 2} \\ & \mathsf{Q}_{2} = \frac{\mathsf{e}}{2\mathsf{e} - 2} \cdot \mathsf{Q}_{1} \approx 0.79 \cdot \mathsf{Q}_{1} \approx 0.29 \cdot \Pi_{0} \end{aligned}$$

The (realistic) Energy Storage Density of an



φ: Ratio between flowthrough the pressureexchanger andmembrane flow

 $\Psi = \Delta p_J / \Pi_0$: Fraction of membrane pressure drop from total osmotic pressure.

