

# The Physics of Wind Park Optimization

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$$P \leq \frac{16}{27} \frac{1}{2} \rho A v^3$$

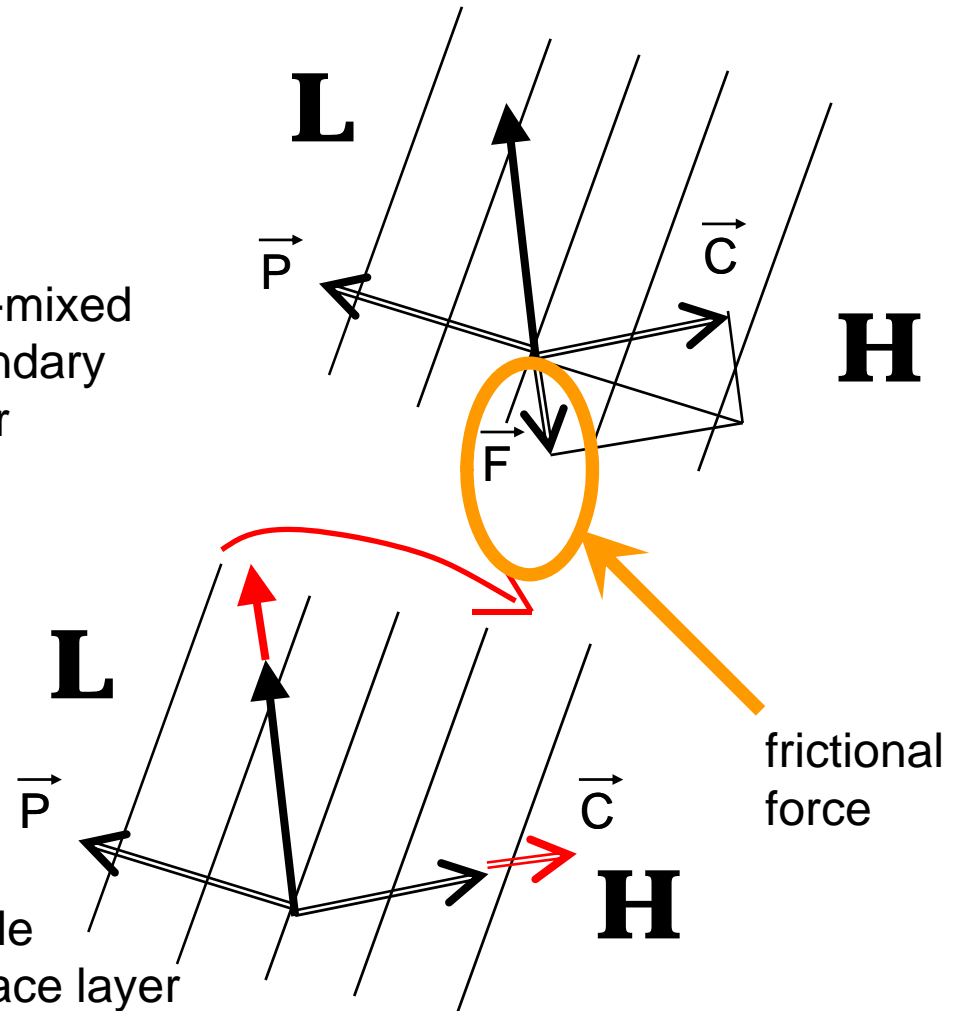
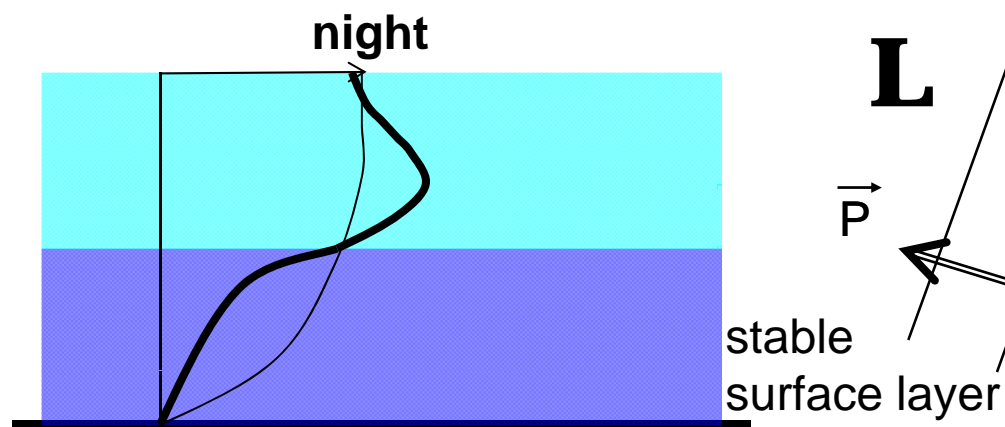
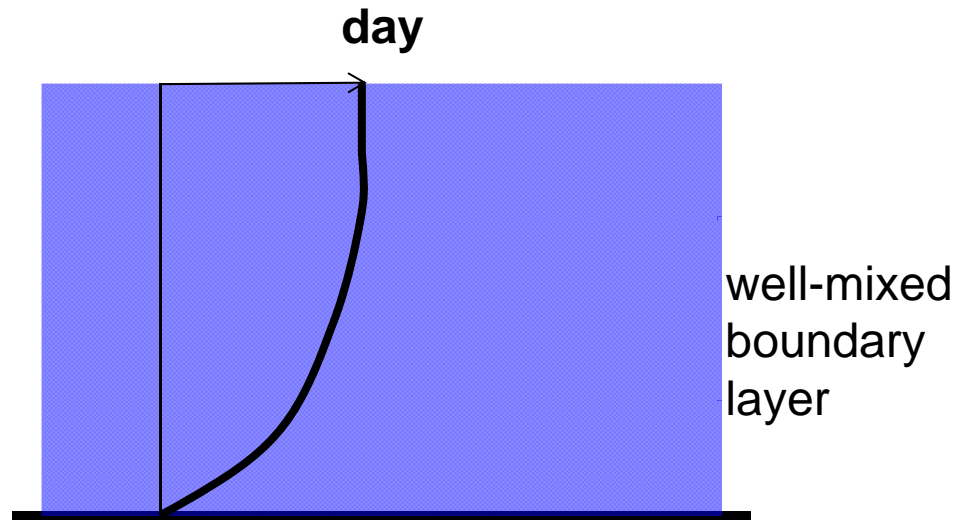
<b>P</b>	<b>power</b>	<b>W</b>
<b><math>\rho</math></b>	<b>air density</b>	<b>kg m<sup>-3</sup></b>
<b>A</b>	<b>rotor area</b>	<b>m<sup>2</sup></b>
<b>v</b>	<b>wind speed</b>	<b>m s<sup>-1</sup></b>
<b>16/27</b>	<b>Betz' factor</b>	<b>-</b>

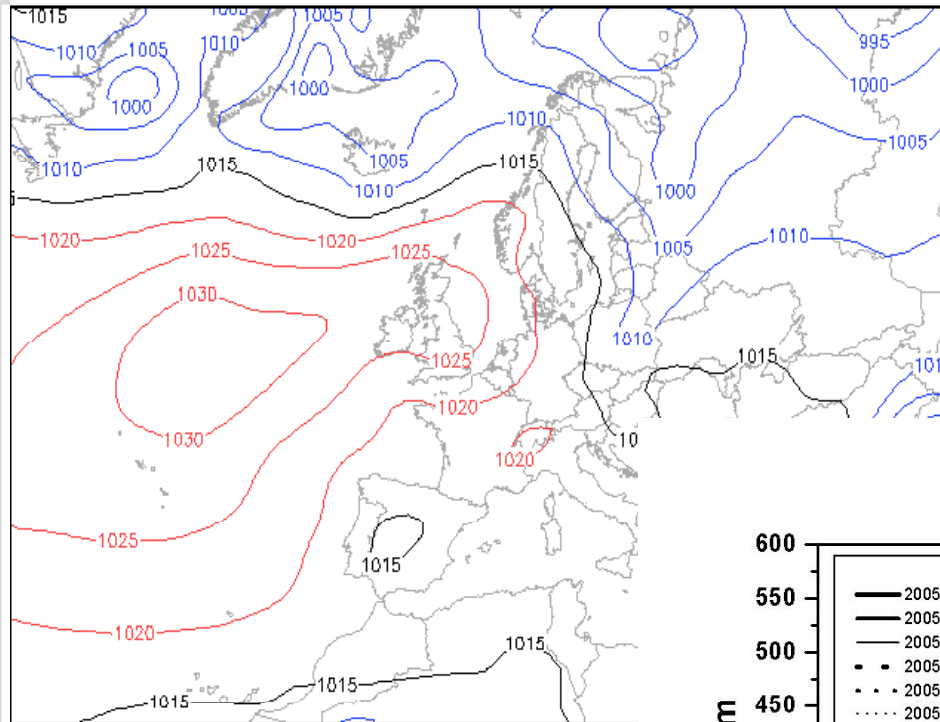
**but is it this simple? ...**

## Meteorological phenomena effecting energy generation from the wind (yields and loads)

<b>phenomenon</b>	<b>effect on yield</b>	<b>effect on loads</b>
<b>vertical wind profile</b>	<b>increase with growing hub height</b>	<b>increase with growing hub height</b>
<b>shear layers (inversions)</b>		<b>differential loads</b>
<b>low-level jets</b>	<b>nocturnal maxima</b>	<b>nocturnal maxima</b>
<b>extreme winds</b>	<b>shut-down of turbines</b>	<b>extreme loads, immediate damages</b>
<b>turbulence intensity</b>	<b>higher yields reduced wake lengths</b>	<b>higher loads</b>
<b>turbulence profile with height</b>		<b>differential loads</b>

# Nocturnal low-level jet (LLJ) and turning of wind direction with height (northern hemisphere)

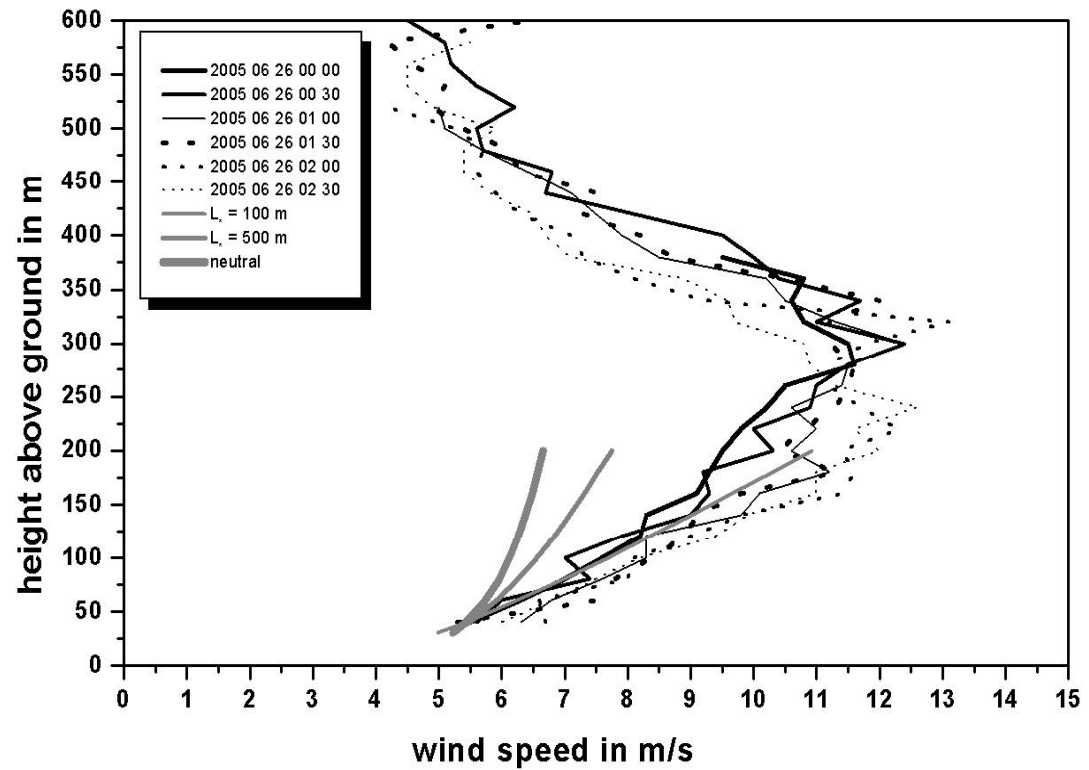




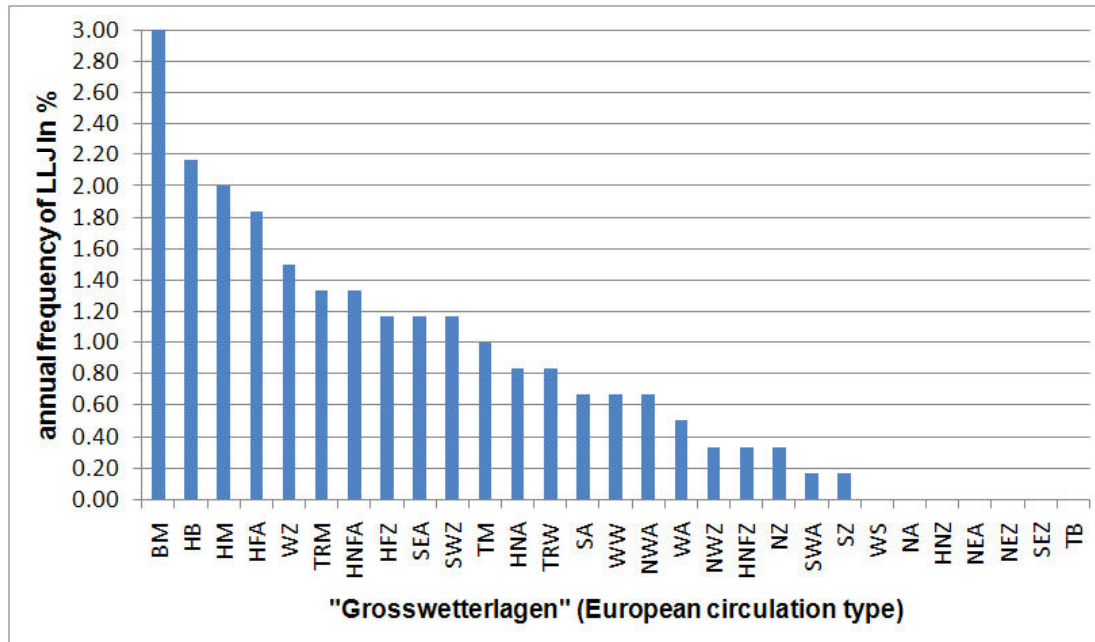
LLJ

Bodendruck GFS (hPa)

Sa 26.06.05 00  
WetterOnline



**26 June 2005**  
**Paris, Ch. de Gaulle airport**  
**SODAR measurements**



frequency of LLJ over Hanover for 20 months in the years 2001 to 2003

total is 23.17% of all nights

**circulation types:**

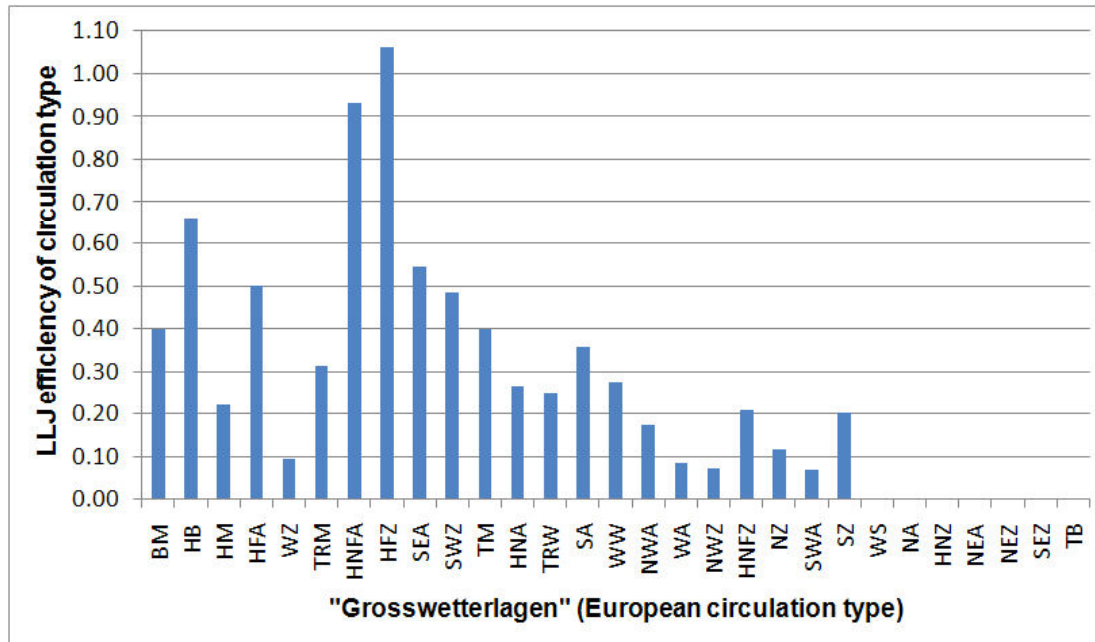
**BM** ridge over Central Europe  
**HB** high over British Isles  
**HM** high over Central Europe

...

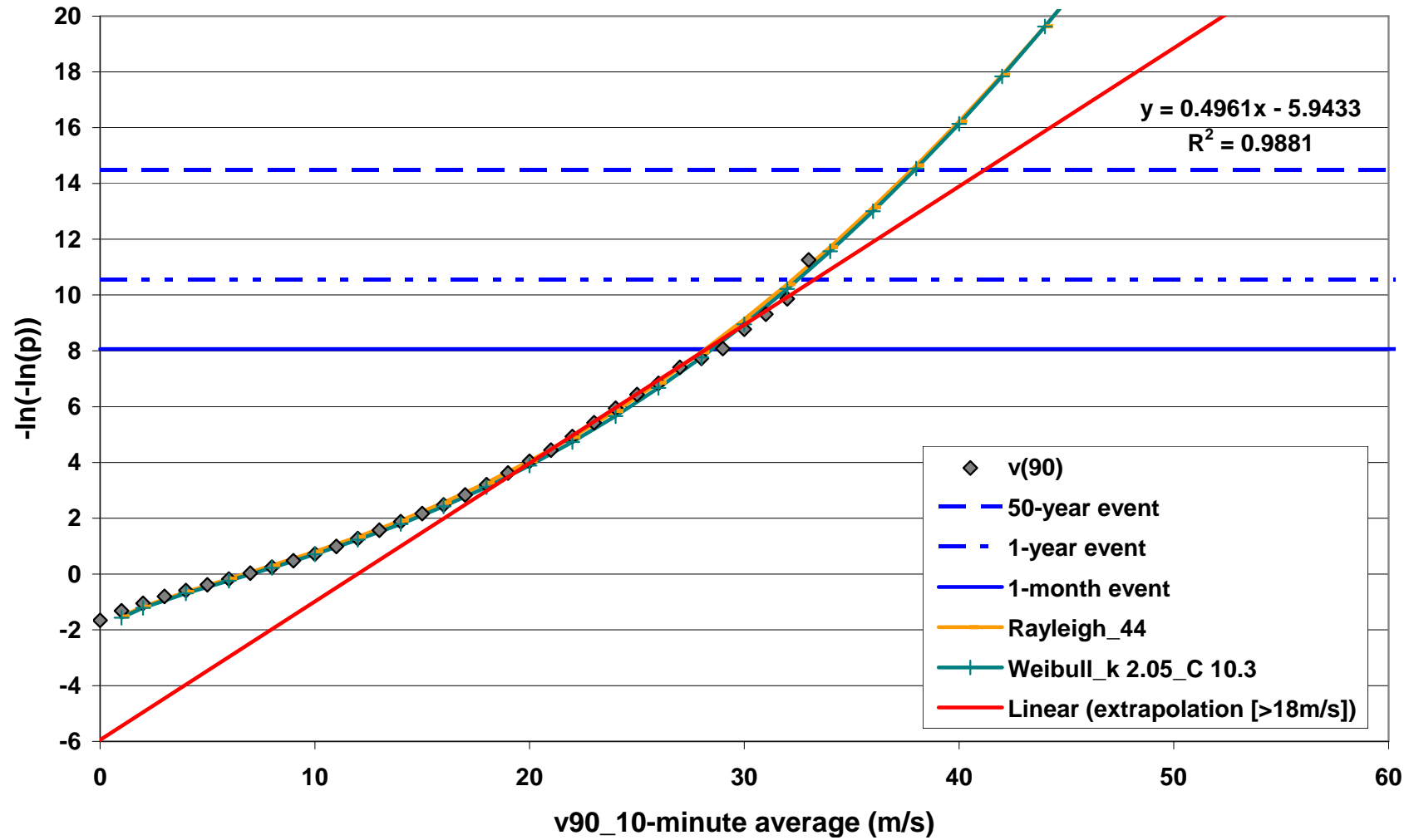
**HFZ** high over Scandinavia  
**HNFA** high over North Atlantic

...

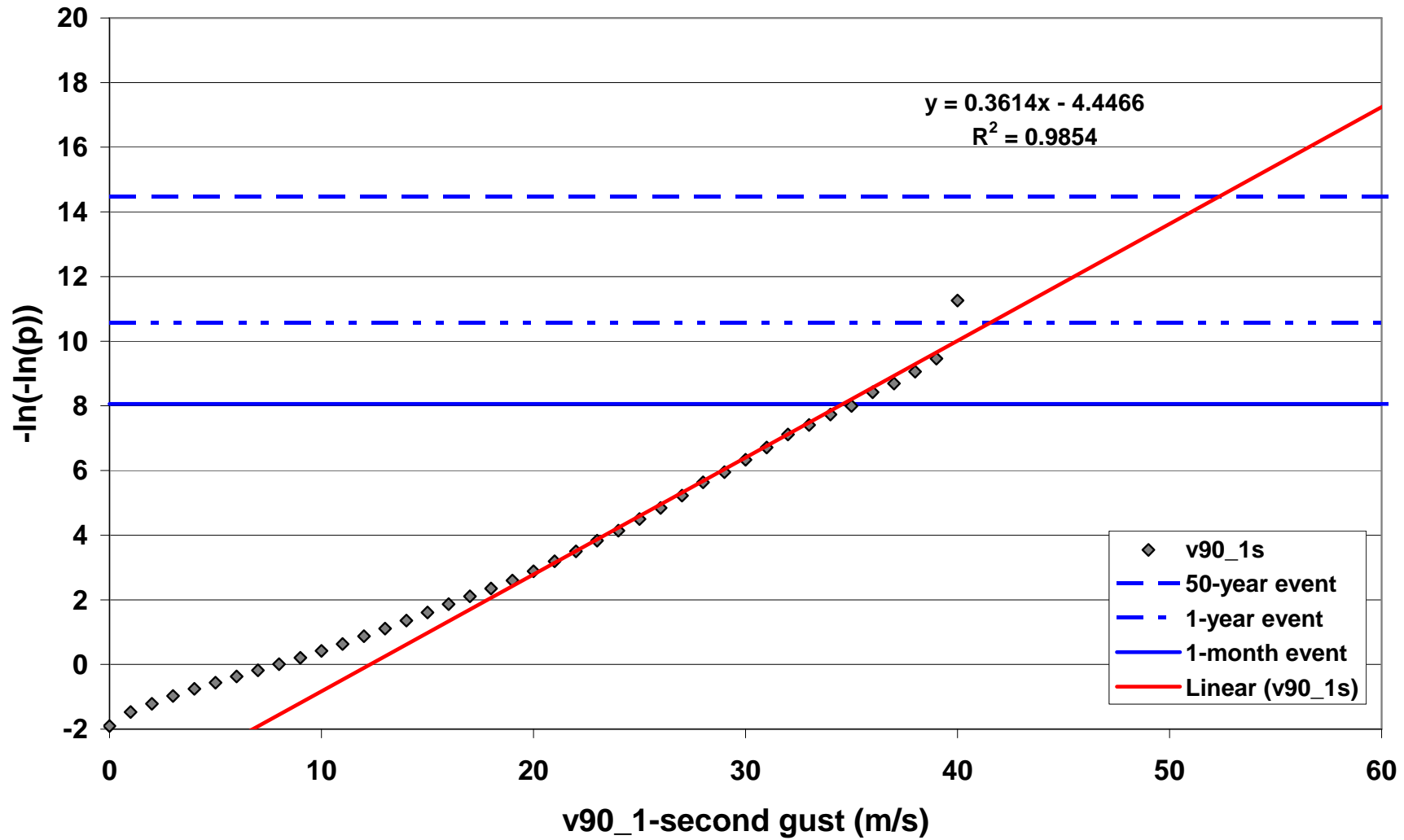
“efficiency” of a circulation type to produce a LLJ over Hanover for 20 months in the years 2001 to 2003



# 10 min extreme wind speed at FINO1



# 1 sec extreme wind speed at FINO1





**extreme winds**

**shut-down of turbines**

**extreme loads,  
immediate damages**



**This turbine has been damaged  
by gale force winds in Northern  
Germany in February 2011**

**→ forecasts of extreme wind  
conditions important**

Photo: dpa, Hamburger Abendblatt, February 6, 2011  
<http://www.abendblatt.de/region/article1778907/Niedersachsen-duehwirbelt-Feuerwehr-im-Dauereinsatz.html>

# Wind parks

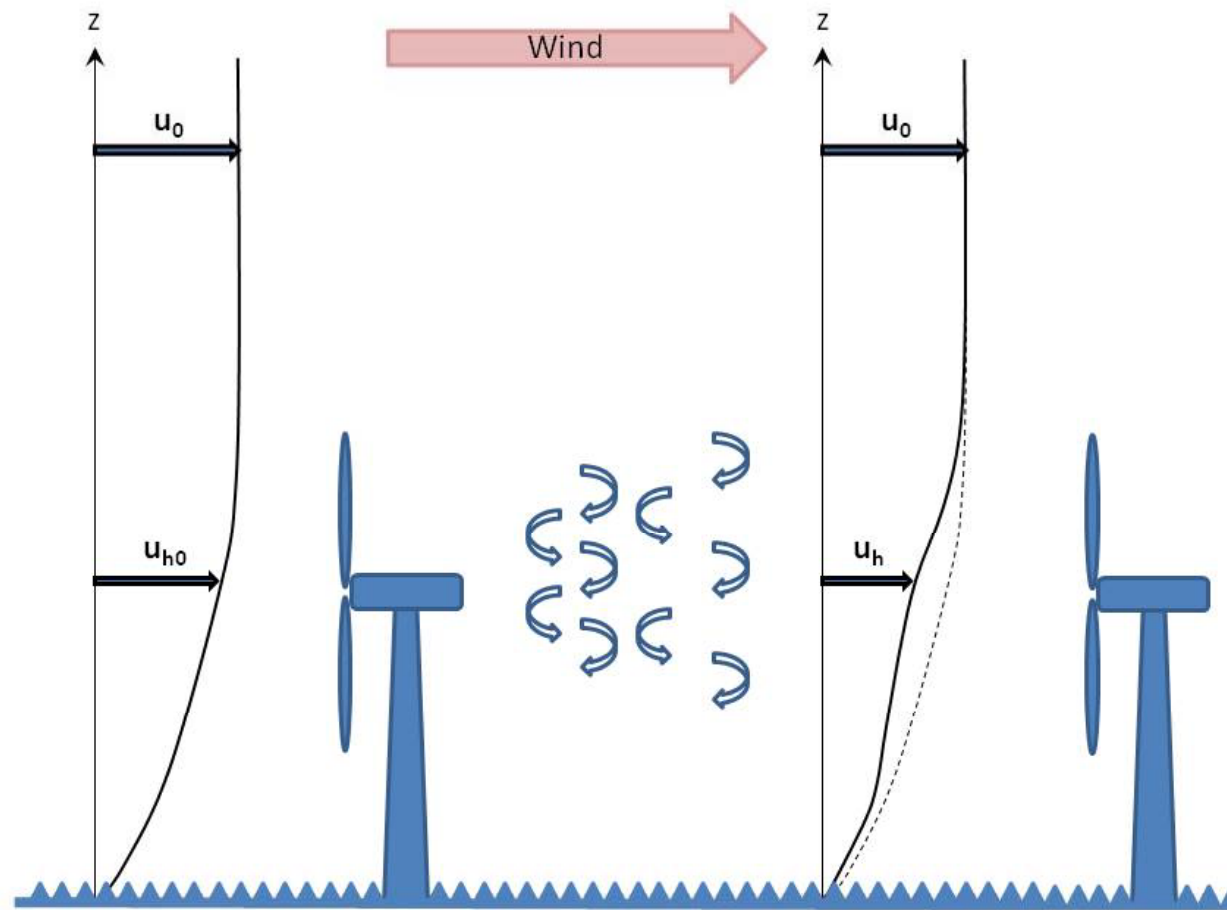
**what happens when turbines are close together? ...**

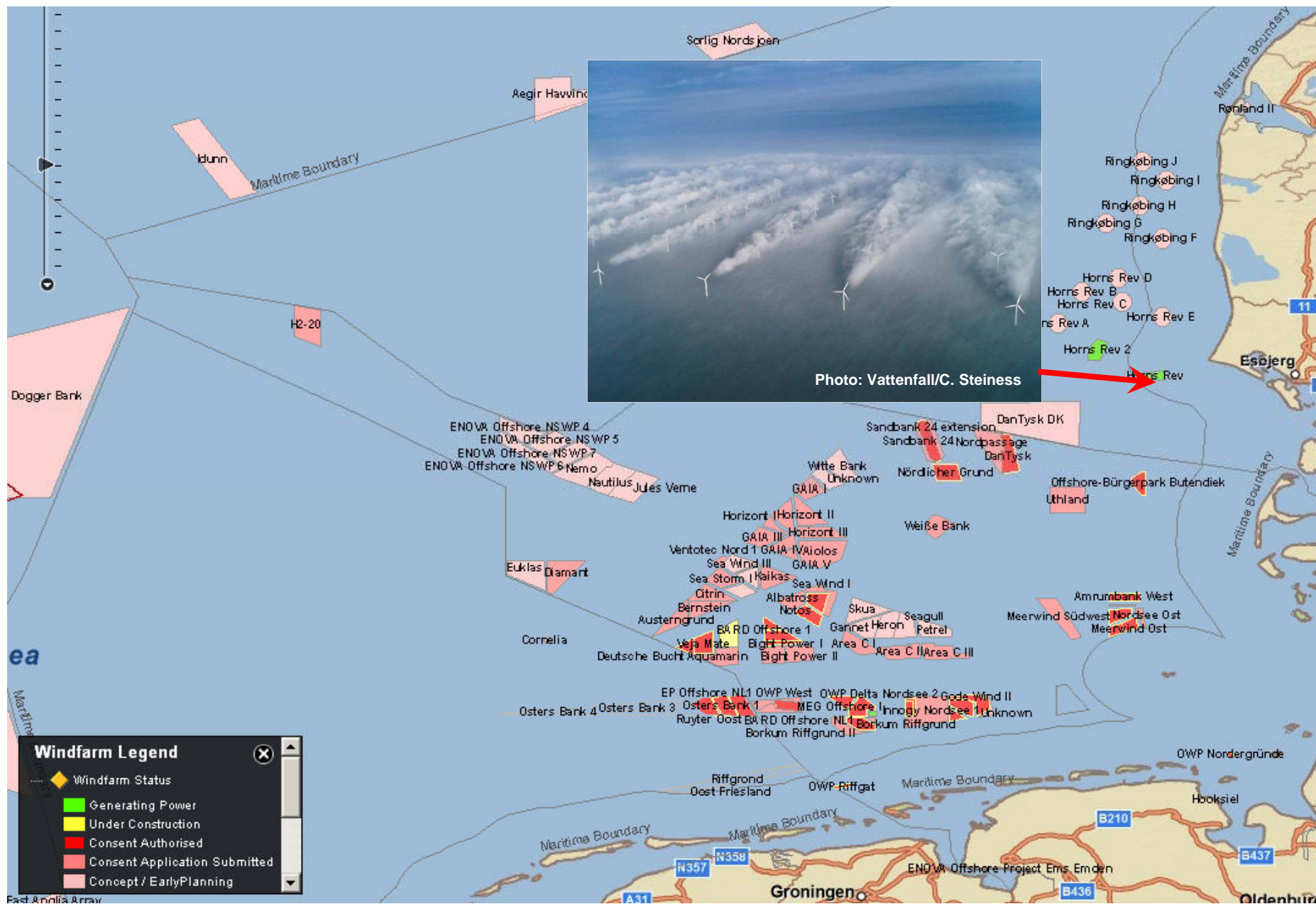
## wake formation behind a wind turbine

- less wind speed

- more turbulence

ahead of the next turbine in a wind park





source: <http://www.4coffshore.com/offshorewind/>

**Wind energy generation is based on momentum (energy) extraction from the air**  
**momentum extraction decelerates the wind**

**→ (1) wind park efficiency depends on the equilibrium wind speed  
in the interior of the park**

**- equilibrium between extraction and re-supply of momentum**

**→ (2) wind park wakes influence other wind parks downstream**

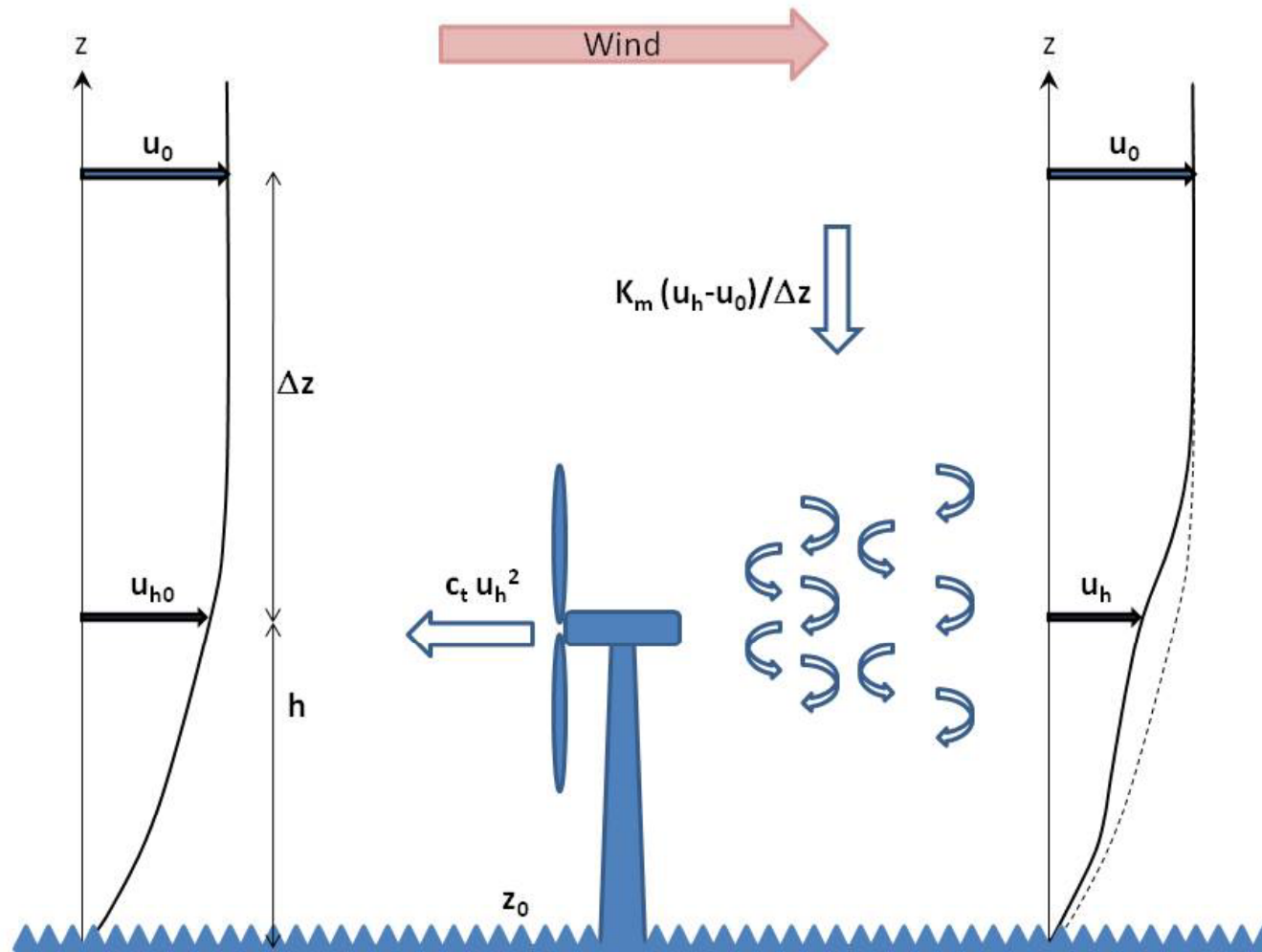
**- wake length is inversely proportional to the momentum re-supply**

**→ for wind park design it is important to know:**

**1) the magnitude of wind speed reduction in the park interior**

**2) the length of wakes**

## 1) the magnitude of wind speed reduction in the park interior



## basic idea of the analytical model

reduction of wind speed in the park interior (calculation of the equilibrium condition for the momentum fluxes)

$$C_{teff} u_h^2 = \frac{K u_* z (u_0 - u_h)}{\Delta z \phi_m}$$

extraction = re-supply from above

turbine and surface drag

flux-gradient-relationship

Emeis, S., 2010: A simple analytical wind park model considering atmospheric stability. *Wind Energy*, 13, 459-469.



## solution of the analytical model

reduction of wind speed in the park interior (calculation of the equilibrium condition for the momentum fluxes):

momentum extraction by the turbines

surface roughness

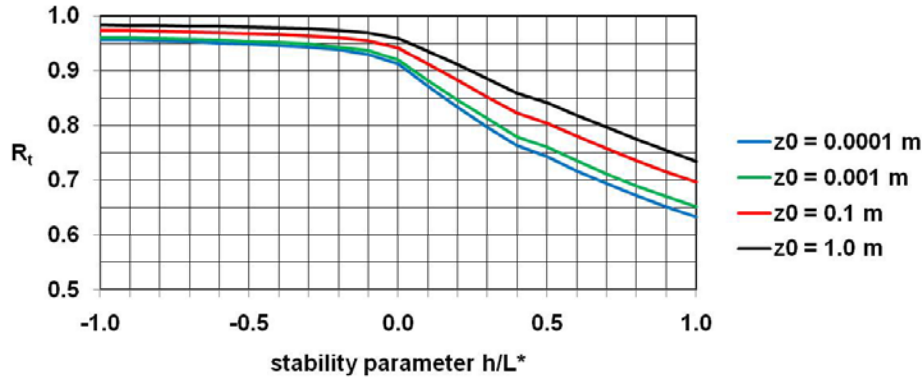
thermal layering of the PBL

turbine-induced turbulence

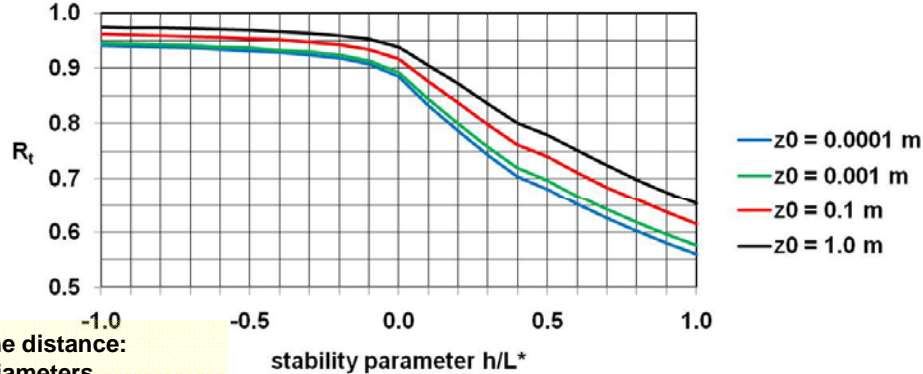
$$R_t = \frac{\left( f_{h,\Delta z} T_i + \frac{\phi_m}{K^2} c_{s,h} \right)}{\left( f_{h,\Delta z} T_i + \frac{\phi_m}{K^2} c_{teff} \right)}$$

Emeis, S., 2010: A simple analytical wind park model considering atmospheric stability. *Wind Energy*, 13, 459-469.

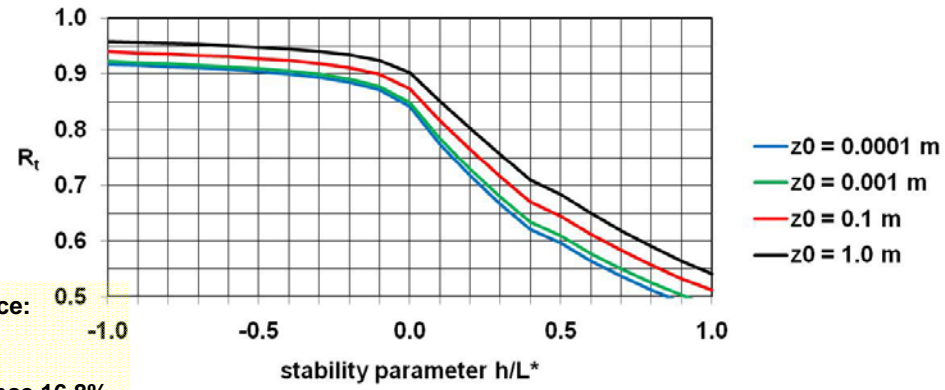
# reduction of wind speed in the park interior



mean turbine distance:  
10 rotor diameters  
→ turbine-induced turbulence 10.1%

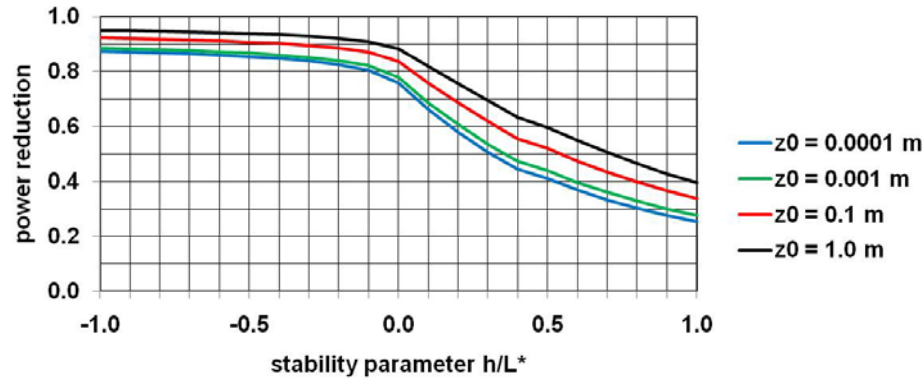


mean turbine distance:  
8 rotor diameters  
→ turbine-induced turbulence 12.6%



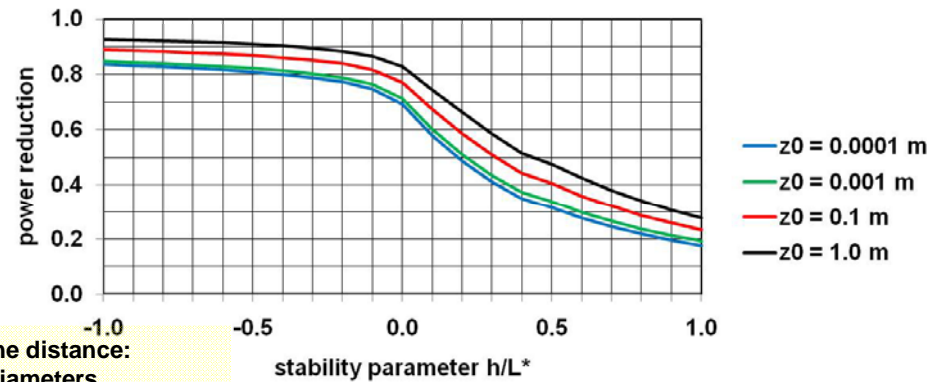
mean turbine distance:  
6 rotor diameters  
→ turbine-induced turbulence 16.8%

# reduction of wind **power** in the park interior



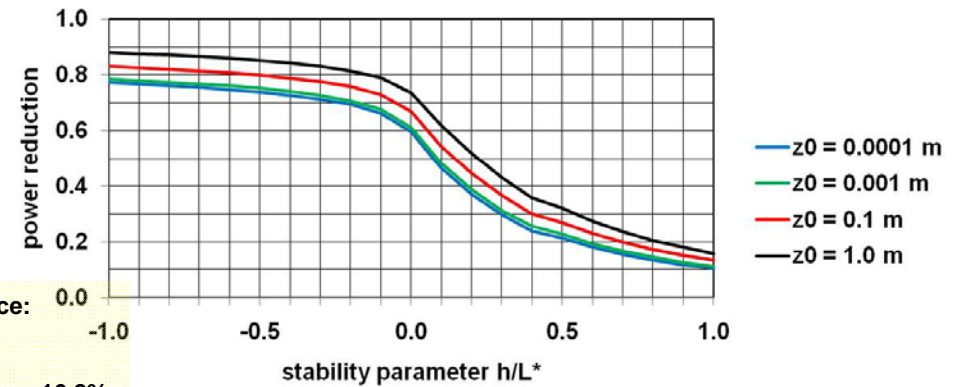
mean turbine distance:  
10 rotor diameters

→ turbine-induced turbulence 10.1%



mean turbine distance:  
8 rotor diameters

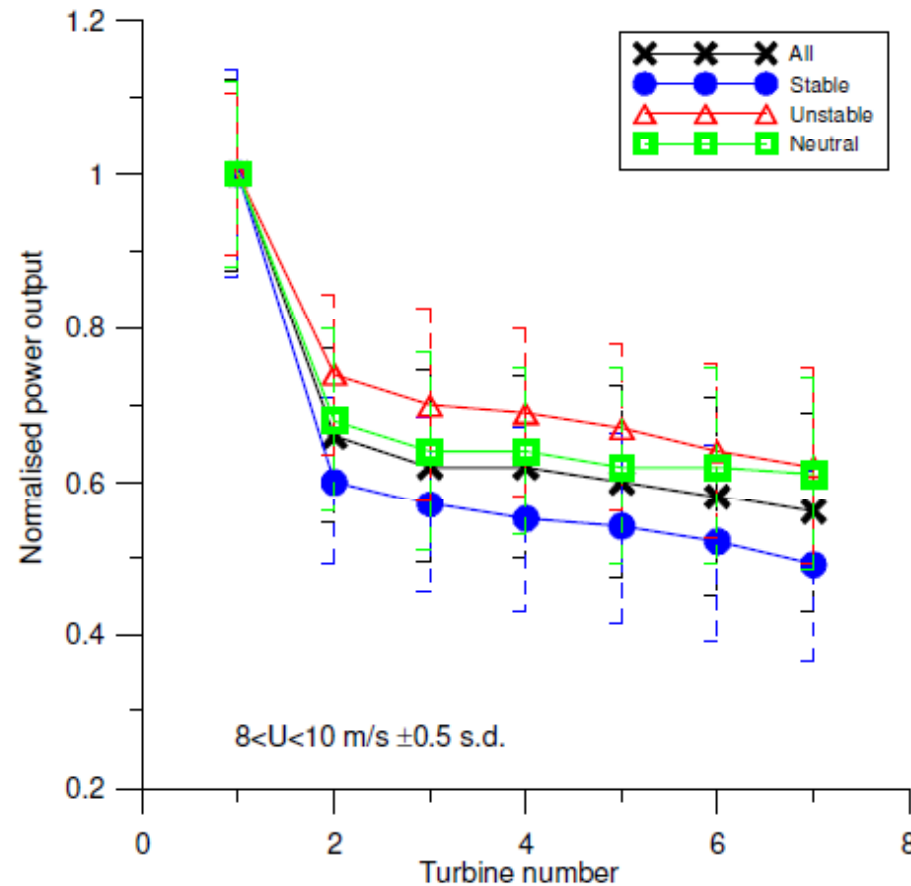
→ turbine-induced turbulence 12.6%



mean turbine distance:  
6 rotor diameters

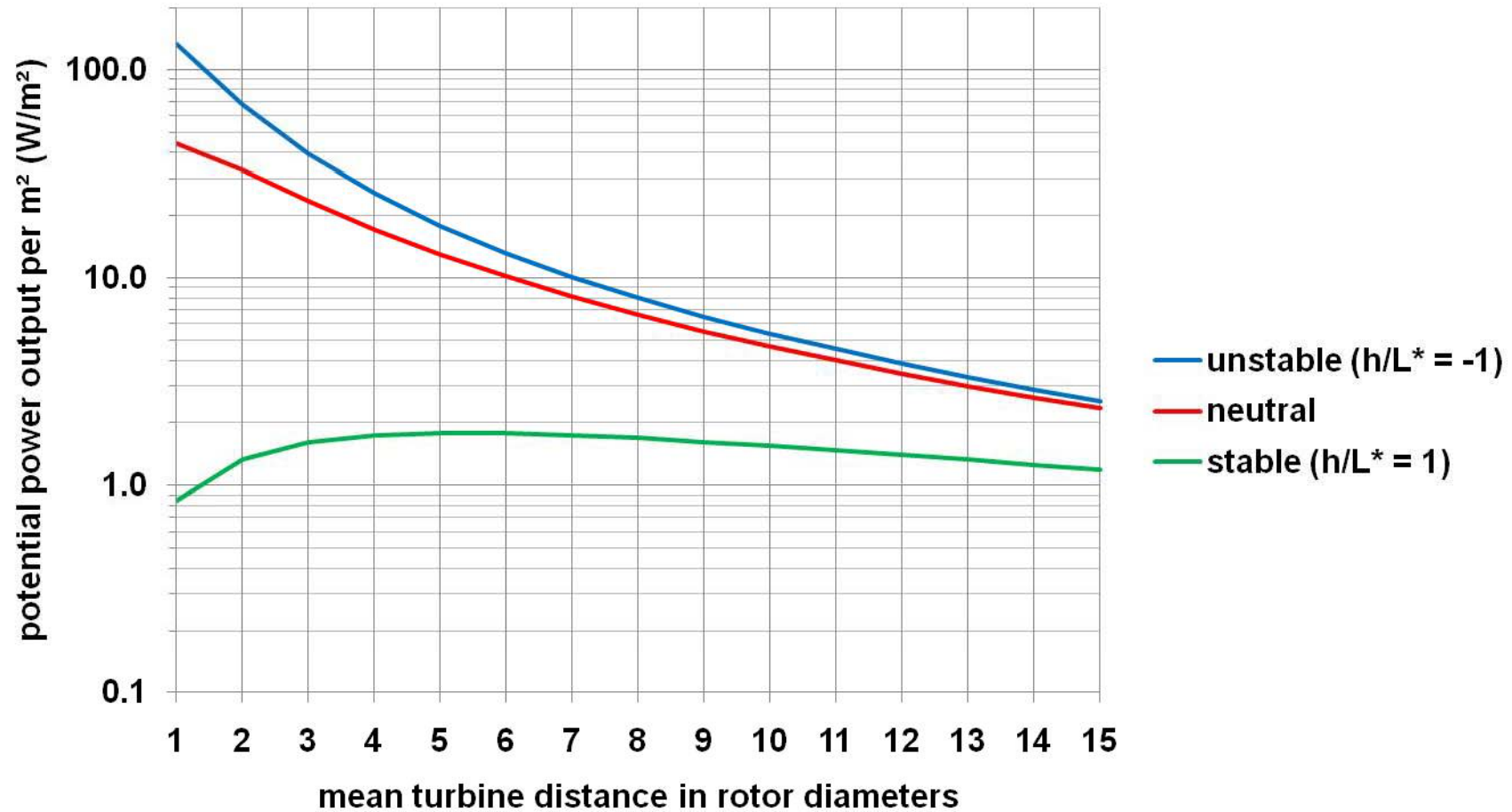
→ turbine-induced turbulence 16.8%

## reduction of wind **power** in the park interior measurements at Nysted wind park (Baltic sea)

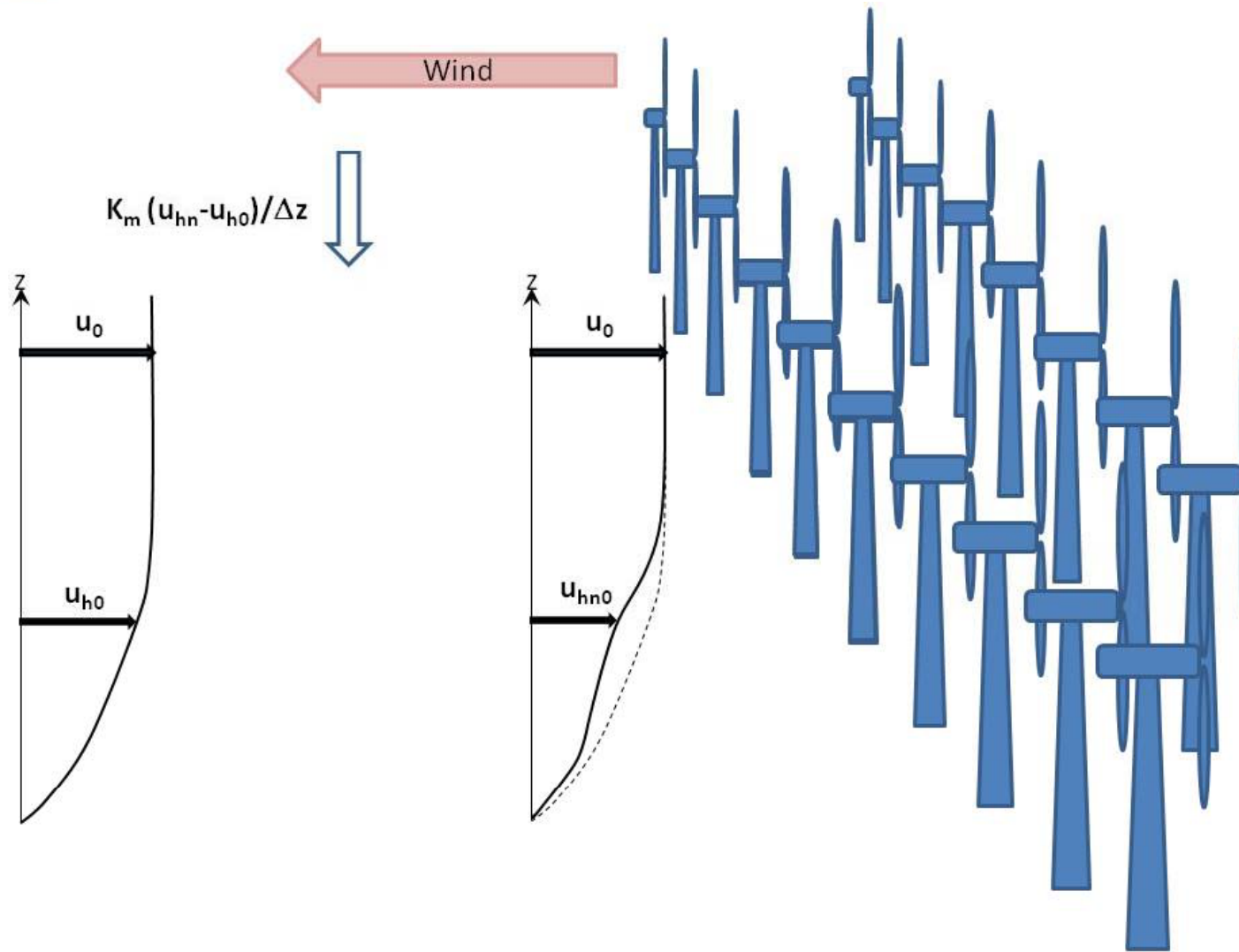


Barthelmie R, Frandsen ST, Rethore PE, Jensen L., 2007:  
 Analysis of atmospheric impacts on the development  
 of wind turbine wakes at the Nysted wind farm.  
 Proceedings of the European Offshore Wind Conference,  
 Berlin 4.-6.12.2007.

## Optimization of turbine density in a wind park



## 2) the length of wakes



## basic idea of the analytical model

speed-up of wind  
speed downstream  
of a wind park:

$$\frac{\Delta u_{hn}}{\Delta t} = \frac{\kappa u_* z}{\Delta z^2} (u_{h0} - u_{hn})$$

speed-up = re-supply from above

Emeis, S., 2010: A simple analytical wind park model considering atmospheric stability. *Wind Energy*, 13, 459-469.



## solution of the analytical model

speed-up of wind  
 speed downstream  
 of a wind park:

momentum extraction by the turbines

surface roughness

thermal layering of the PBL

turbine-induced turbulence

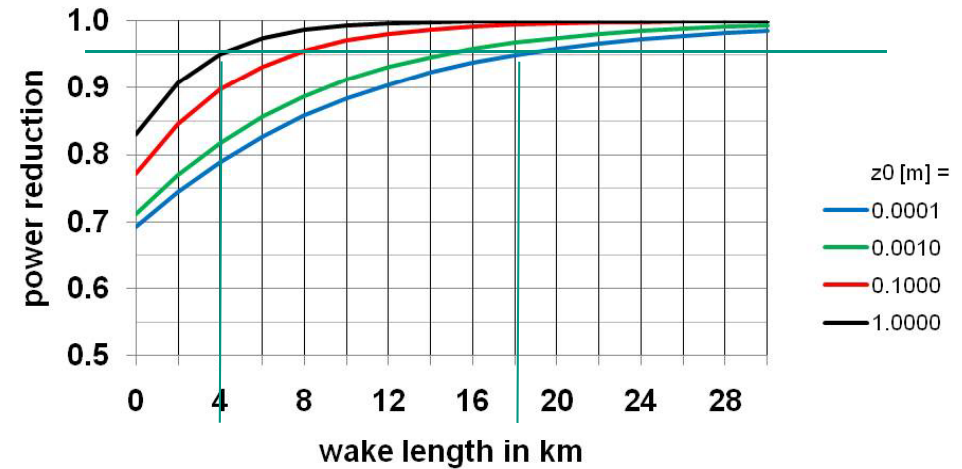
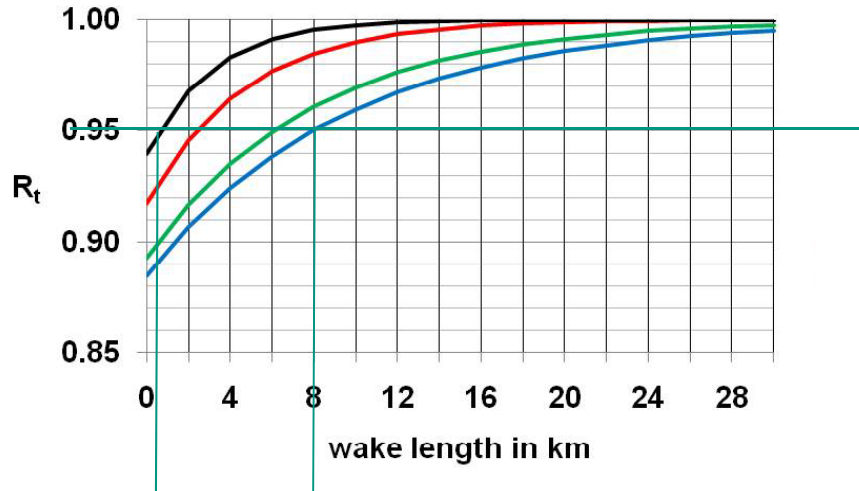
$$R_n = \frac{u_{hn}(t)}{u_{h0}} = 1 + \left( \frac{u_{hn0}}{u_{h0}} - 1 \right) \exp(-at)$$

Emeis, S., 2010: A simple analytical wind park model considering atmospheric stability. *Wind Energy*, 13, 459-469.

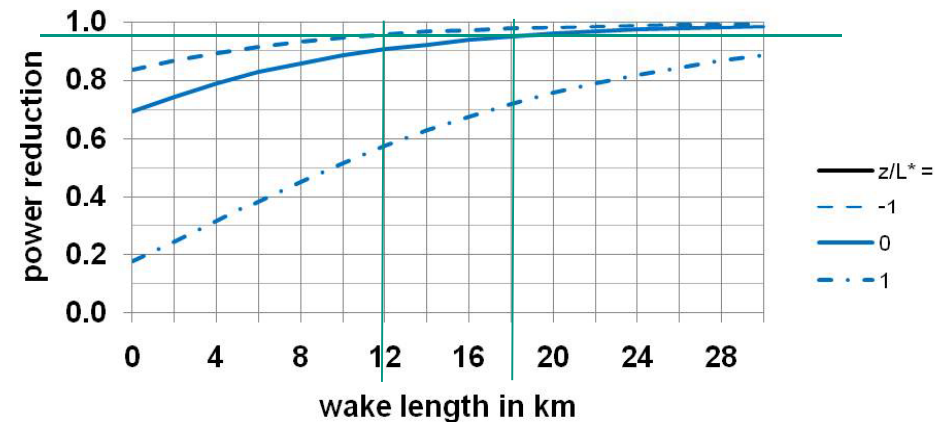
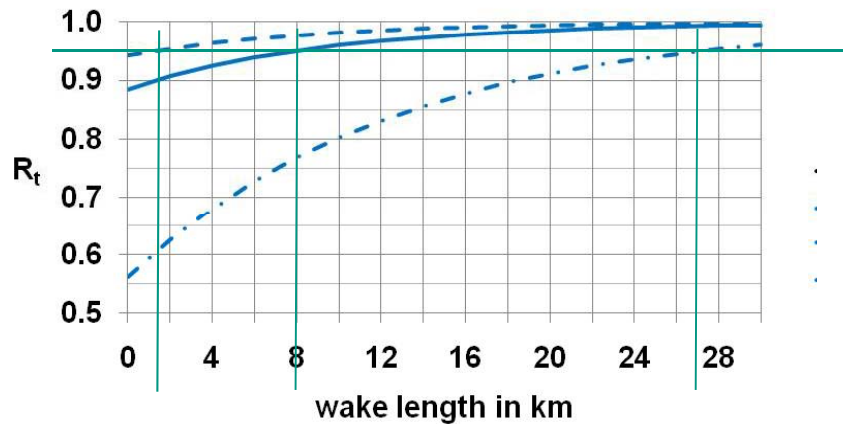
recovery of wind **speed (left)** and **power (right)** behind a wind park,  
 mean turbine density: 8 rotor diameters



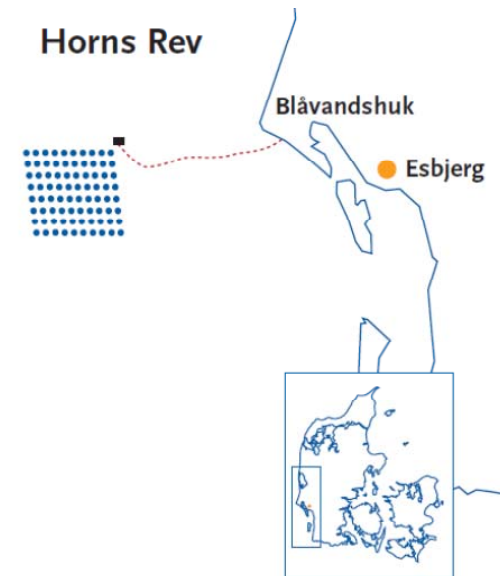
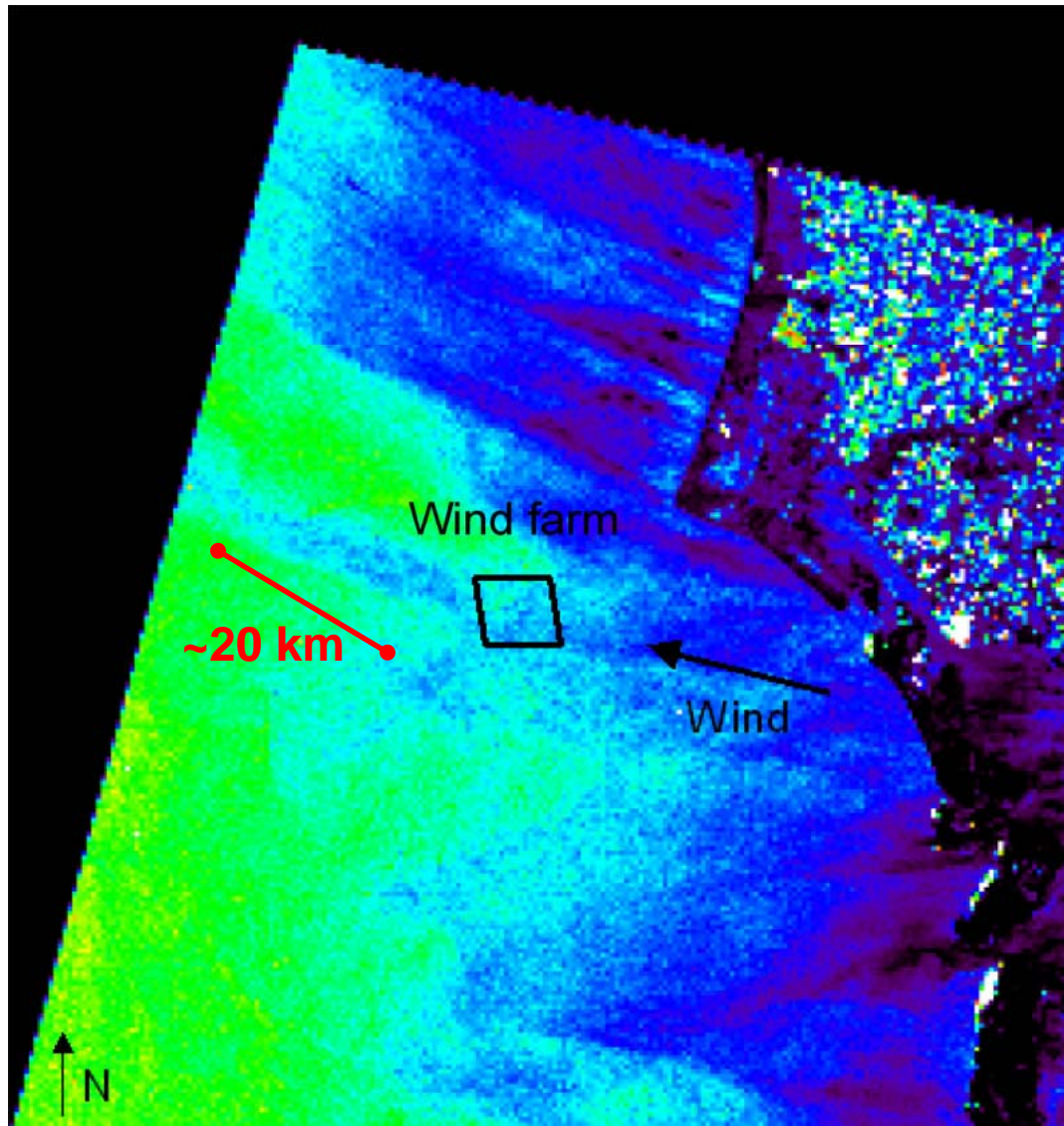
onshore ( $z_0 = 1.0$  m) – offshore ( $z_0 = 0.0001$  m)



unstable ( $h/L_* = -1$ ) – neutral – stable ( $h/L_* = 1$ )



# speed-up of wind speed behind the wind park measurements (Envisat, SAR) at Horns Rev ( 4 km x 5 km)



[http://www.hornsrev.dk/nyheder/brochurer/Horns\\_Rev\\_TY.pdf](http://www.hornsrev.dk/nyheder/brochurer/Horns_Rev_TY.pdf)

25. 02. 2003

© ERS SAR/Risø  
[http://galathea3.emu.dk/satelliteeye/projekter/wind/back\\_uk.html](http://galathea3.emu.dk/satelliteeye/projekter/wind/back_uk.html)

## Conclusions 1:

### vertical wind profile important

- higher hub heights lead to more power output
- nocturnal low-level jet frequency influences overall power output
- for large turbines (hub height more than 80-90 m), logarithmic or power wind profiles are too simple, turning of the wind becomes important, too

### extreme winds important

- shut down of turbines

### turbulence important

- higher power output
- higher loads
- reduced wake effects

## **Conclusions 2 (wind parks):**

**wind speed reduction: offshore stronger than onshore**

- (partial) compensation of higher offshore wind speed**
- offshore requires a larger distance between turbines**

**larger harvest from wind parks during unstable stratification**

- offshore: annual cycle of energy production**
- onshore: diurnal cycle of energy production**

**offshore wake length is several times larger than onshore**

- offshore requires larger distances between wind parks**

**but, analytical model is strongly simplified**

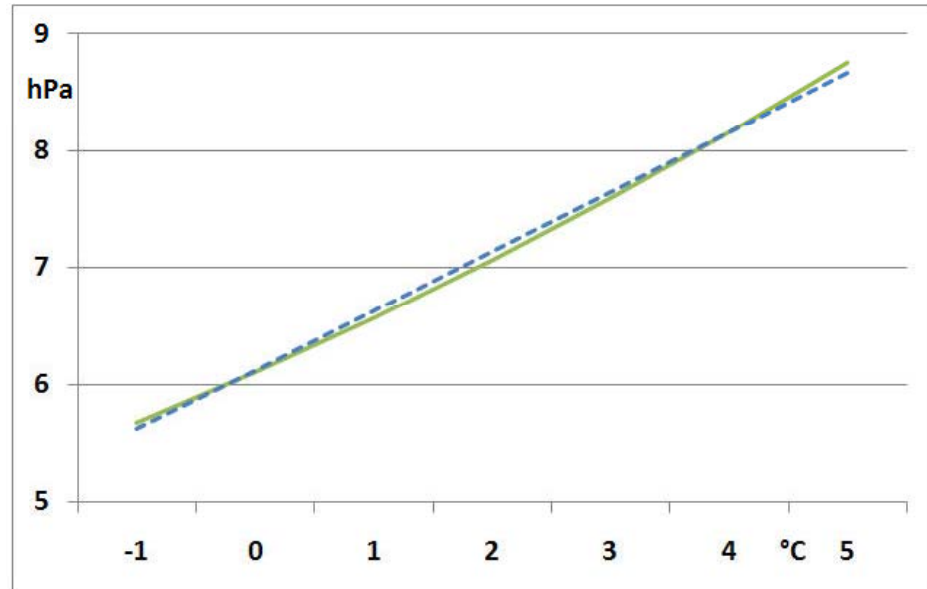
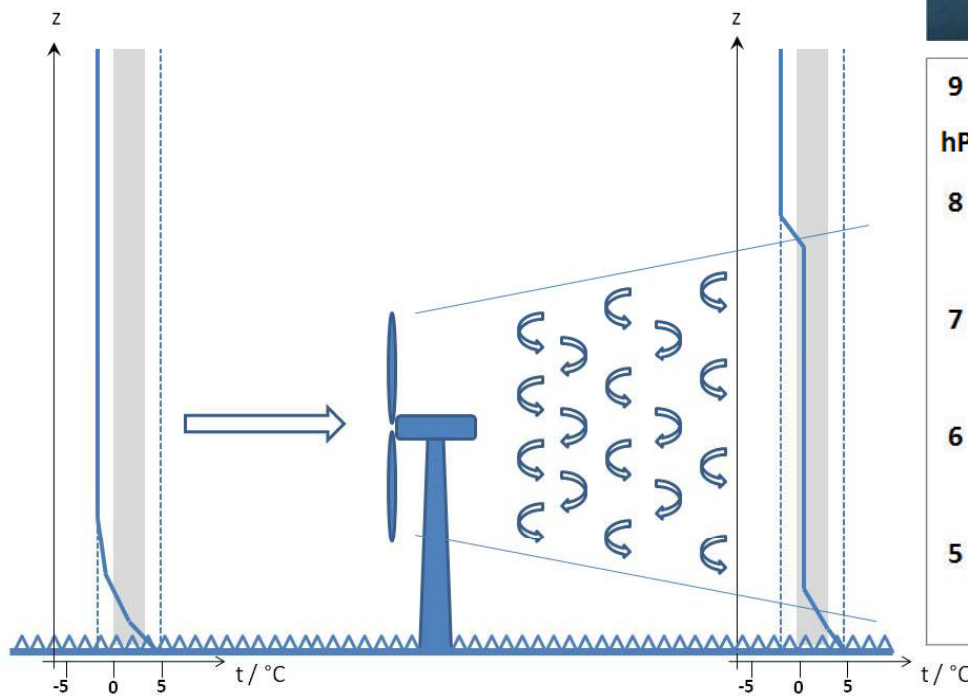
- only for rough estimation, exact simulations with numerical models necessary**

# explanation of wake clouds: mixing fog



Photo: Vattenfall/C. Steiness

12. 02. 2008



air directly over the water:  
 air at hub height:  
 after mixing:

5°C, more than 99% relative humidity  
 -1°C, more than 99% relative humidity  
 2°C, above 101% humidity → clouds



**Thank you for your attention**

