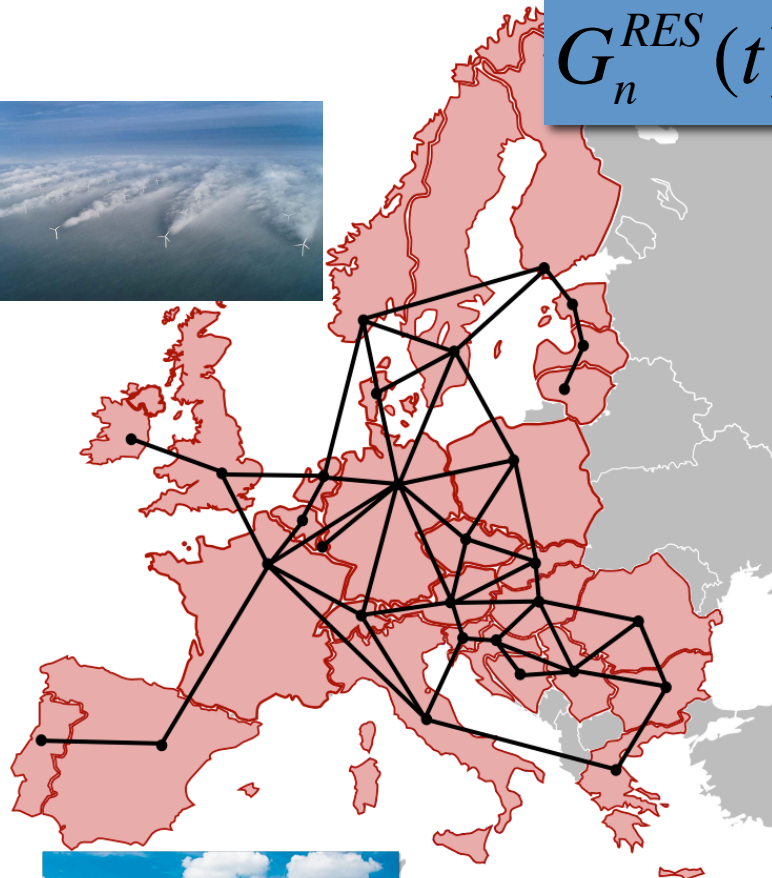


Complex Renewable Energy Networks

$$G_n^{RES}(t) + B_n(t) = L_n(t) + T_n(t) + C_n(t)$$



$$G_n^{RES}(t) = G_n^W(t) + G_n^S(t)$$

Renewable Energy Atlas

2000 – 2007: 1h, 45x45km²

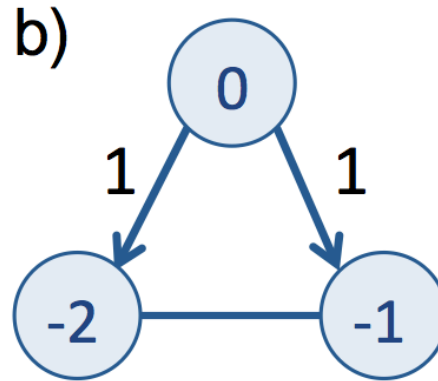
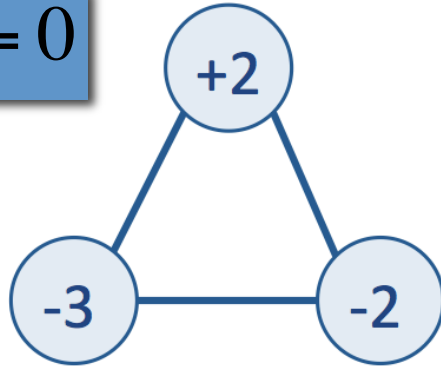
1980 – 2010: 1h, 30x30km²

$$\langle G_n^{RES} \rangle_t = \langle L_n \rangle_t$$

Coupling schemes between transmission and backup

$$\Delta_n(t) = G_n^{RES}(t) - L_n(t) - T_n(t)$$

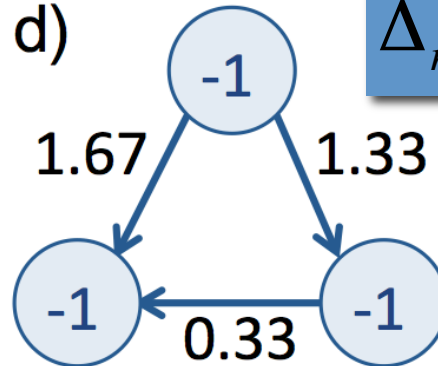
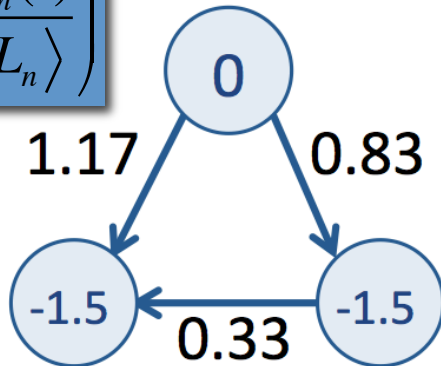
$$T_n(t) = 0$$



$$\min \left(\sum_n B_n(t) \right)$$

$$\min \left(\sum_l F_l^2(t) \right)$$

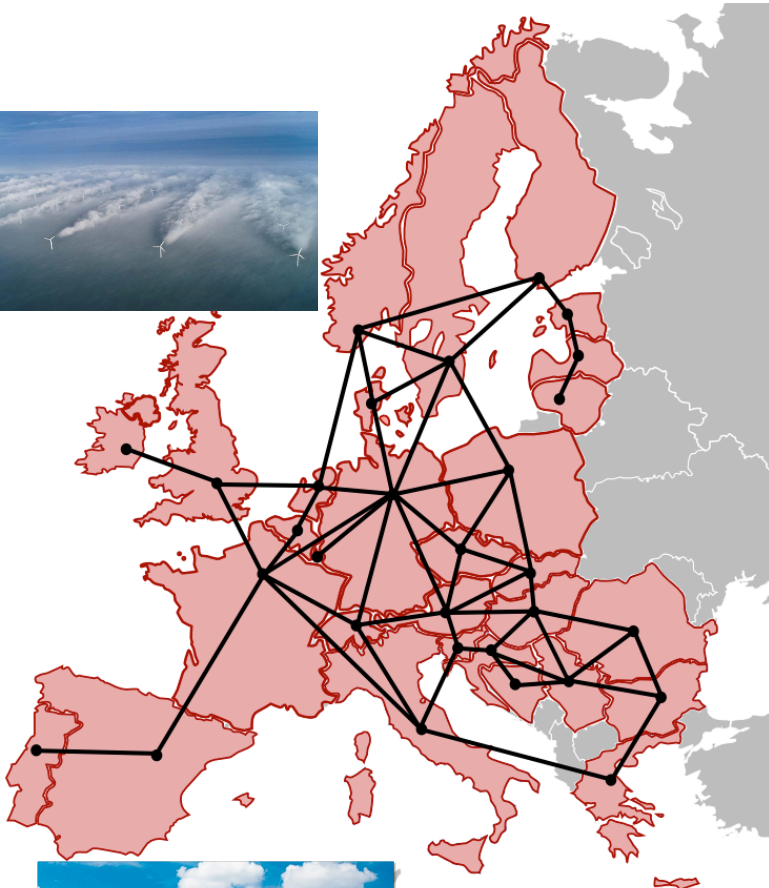
$$\min \left(\max_n \frac{B_n(t)}{\langle L_n \rangle} \right)$$



$$\Delta_n(t) = \beta(t) \langle L_n \rangle$$

$$\beta(t) = \frac{\sum_n \Delta_n(t)}{\sum_n \langle L_n \rangle}$$

Design of a fully renewable European energy system ---- challenges for the physics of complex systems ----



How much ...

... wind energy?

... solar PV energy?

... backup energy + power?

... transmission?

... storage?

... coupling of energy sectors?

and what about

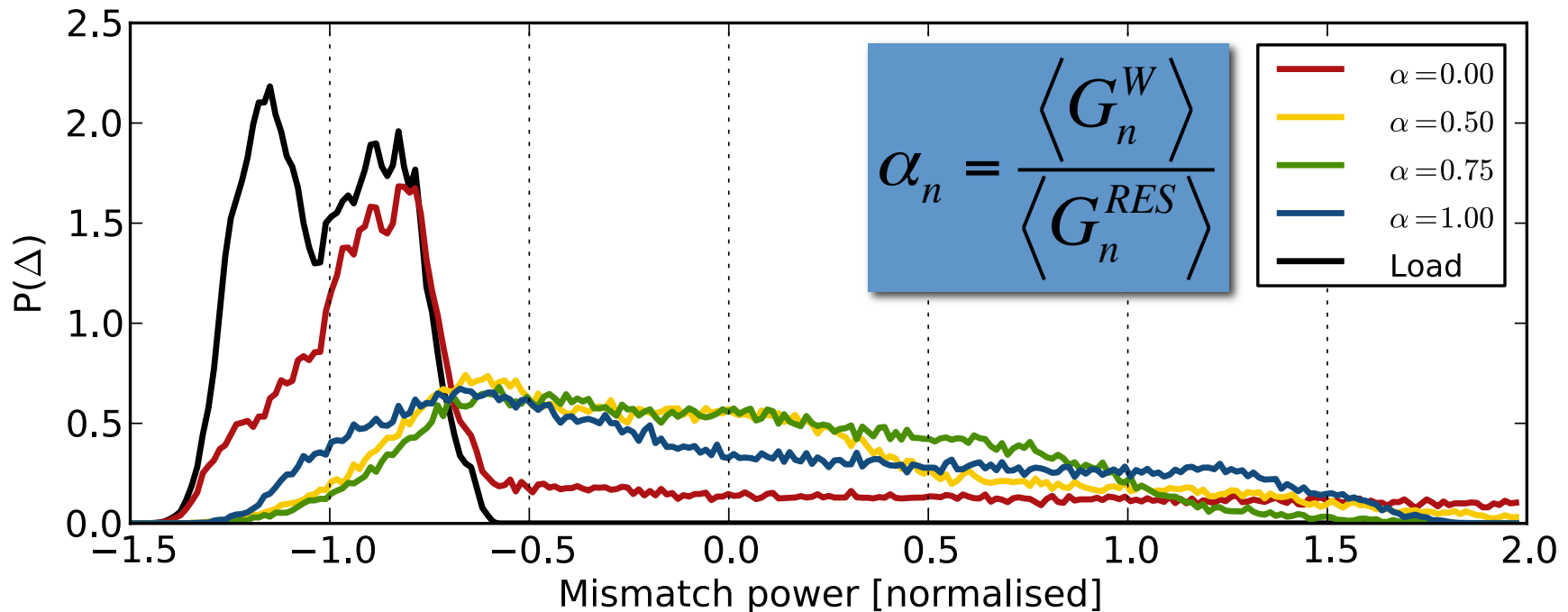
... transition 2050 → 2014?

Mismatch distribution (Germany)

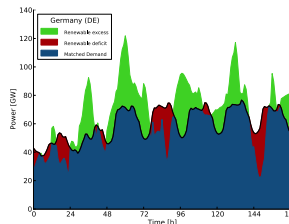
$$\Delta_n(t) = G_n^{RES}(t) - L_n(t) - T_n(t)$$

$$T_n(t) = 0$$

$$\langle G_n^{RES} \rangle = \langle L_n \rangle$$

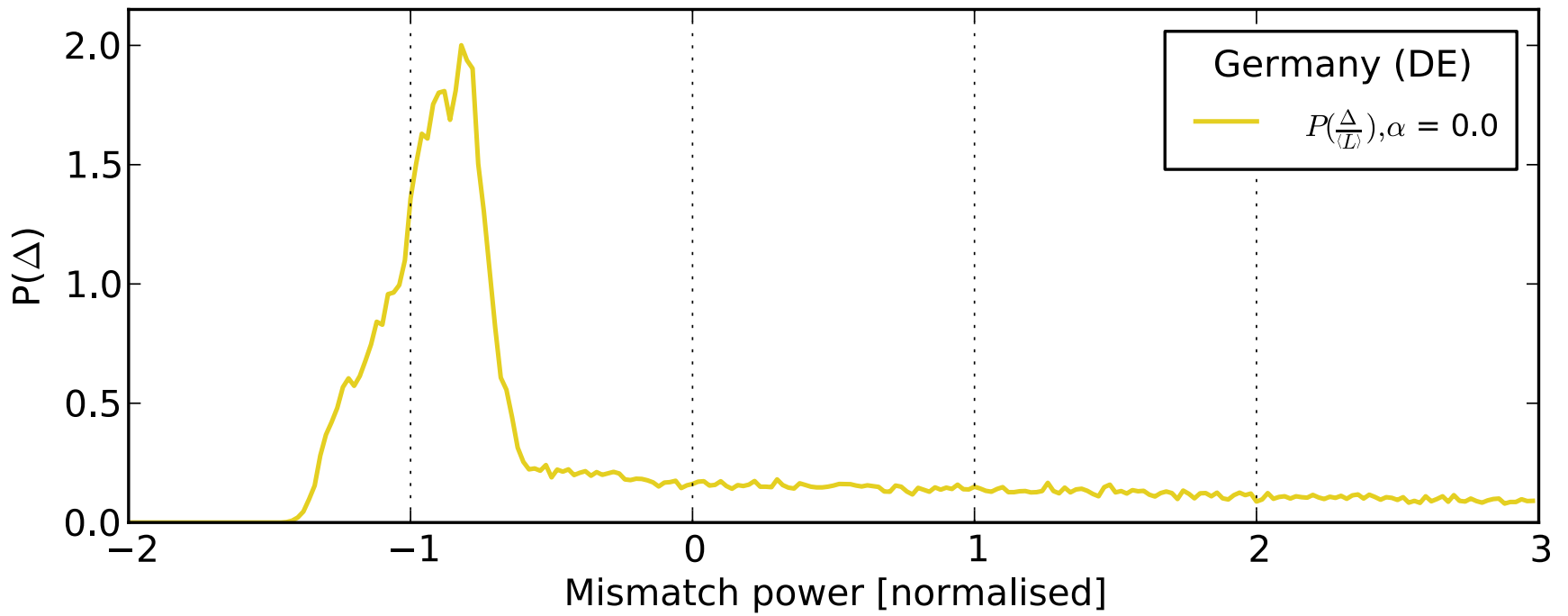


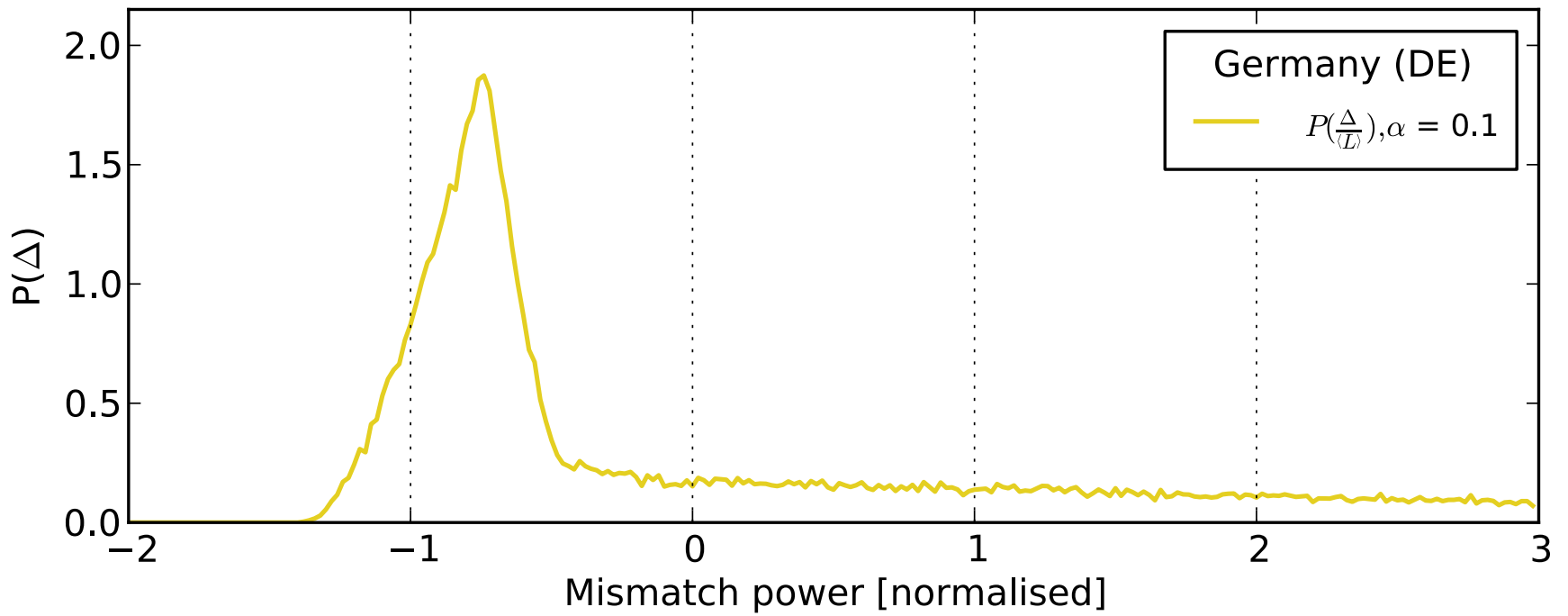
$$B_n(t) = -\min(\Delta(t), 0)$$

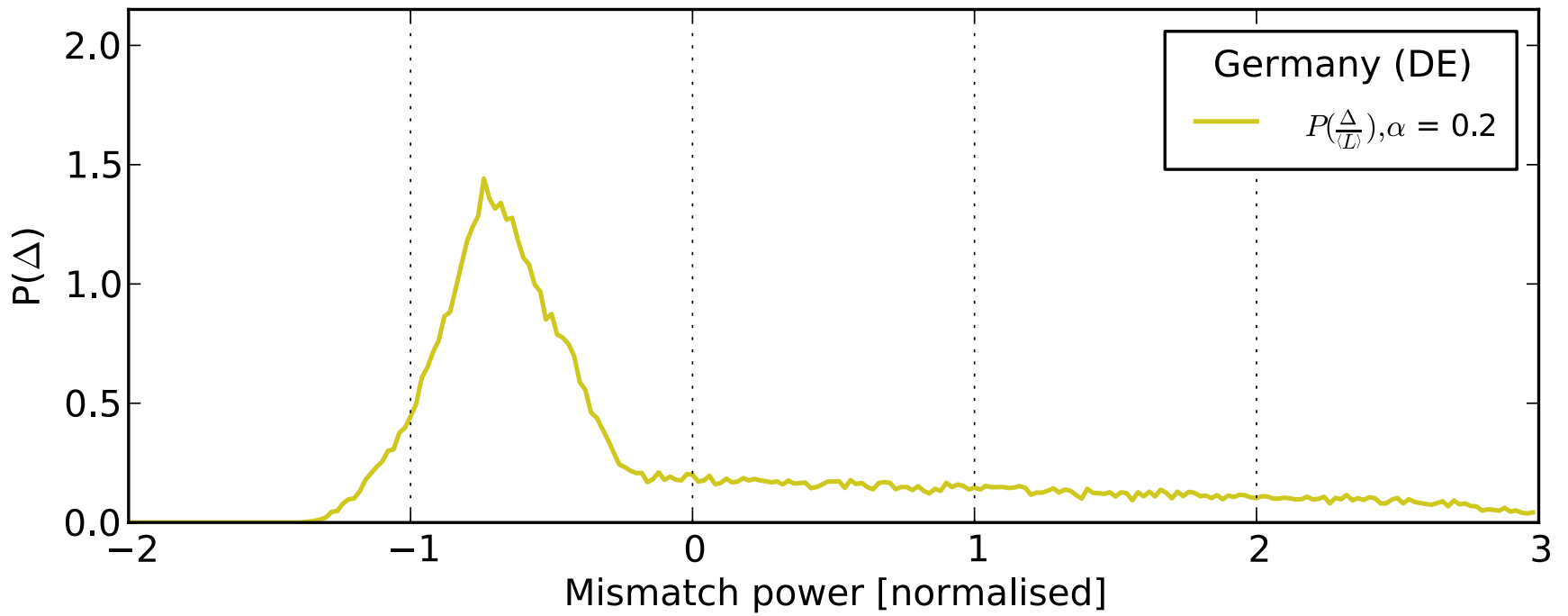


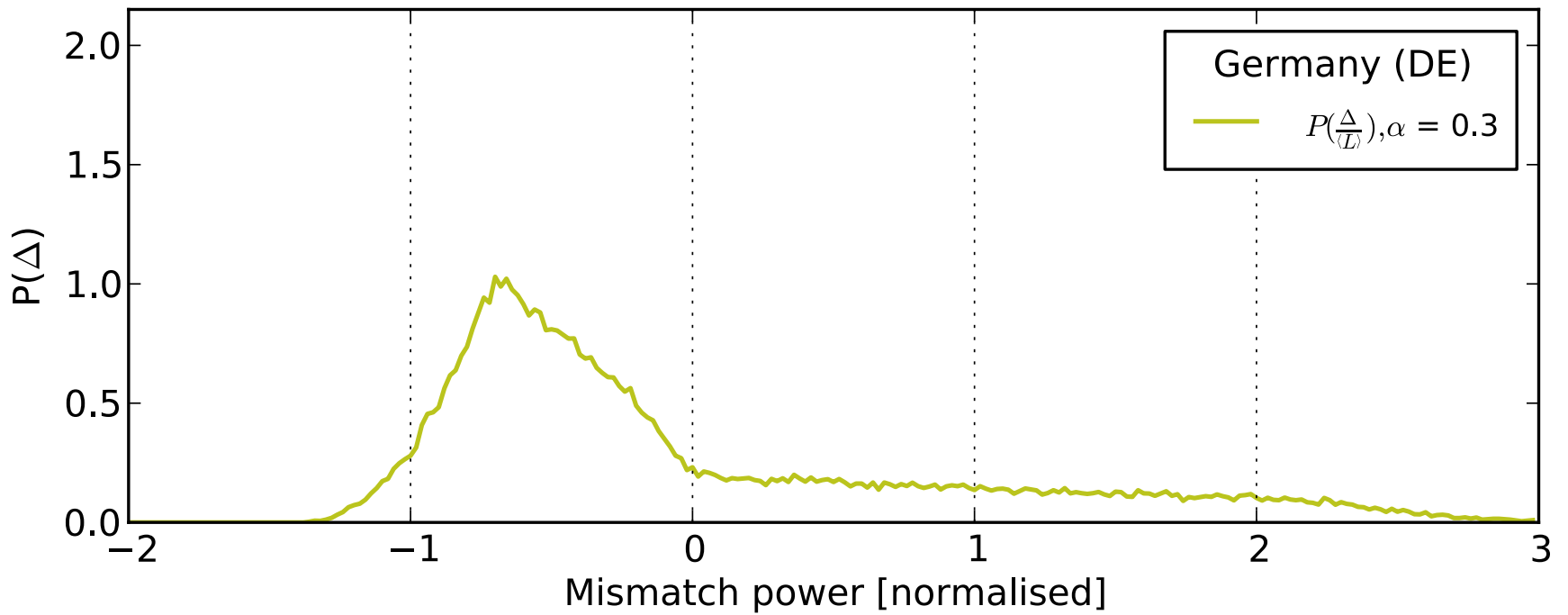
$$C_n(t) = \max(\Delta(t), 0)$$

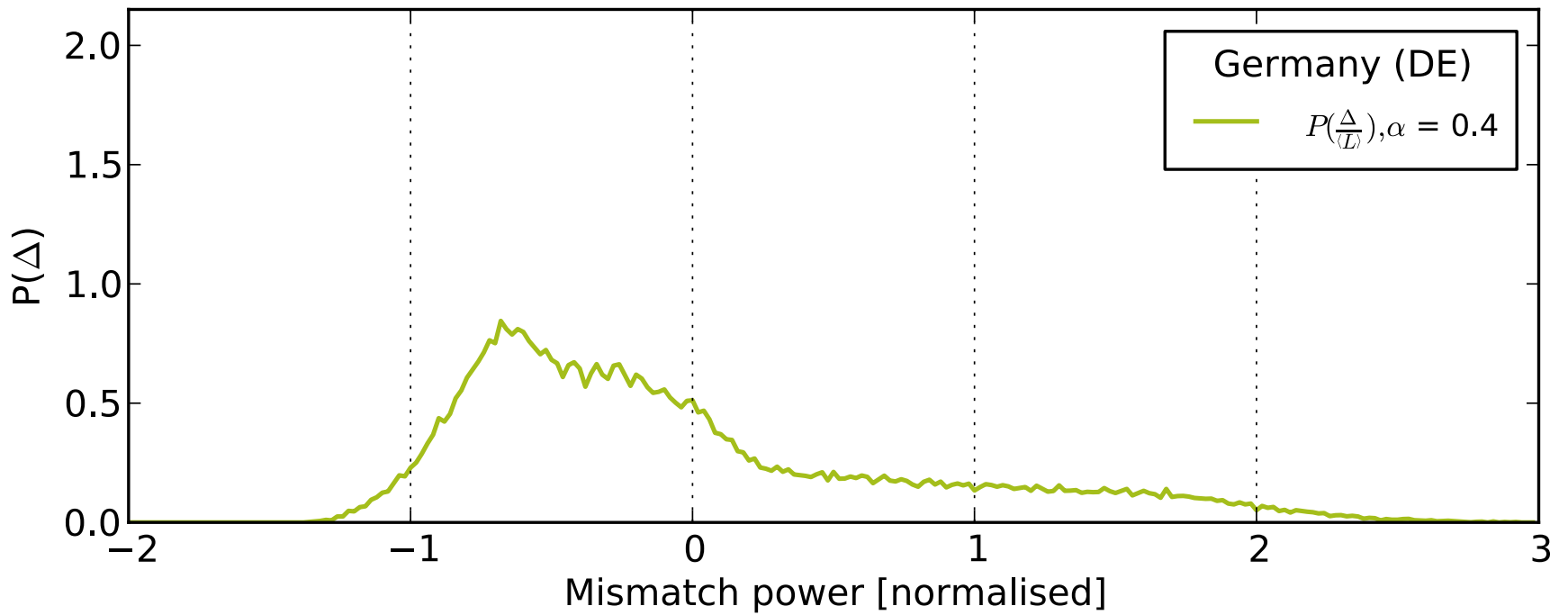


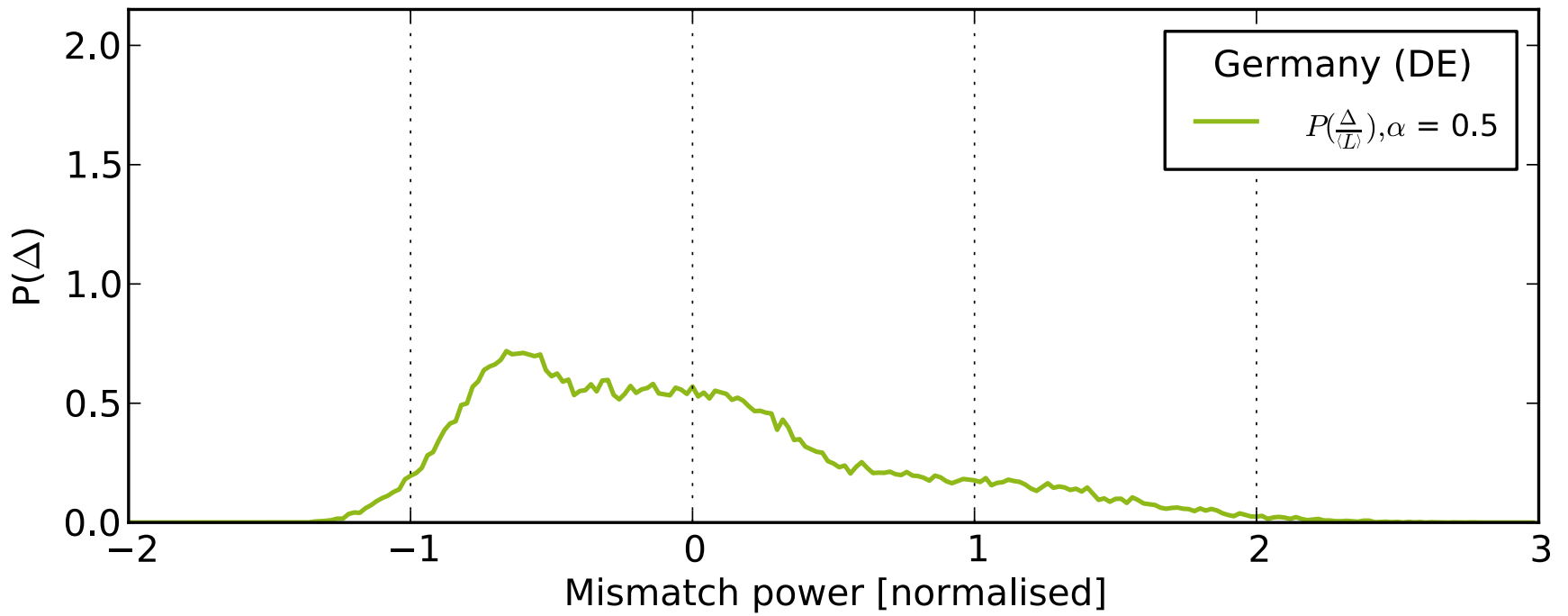


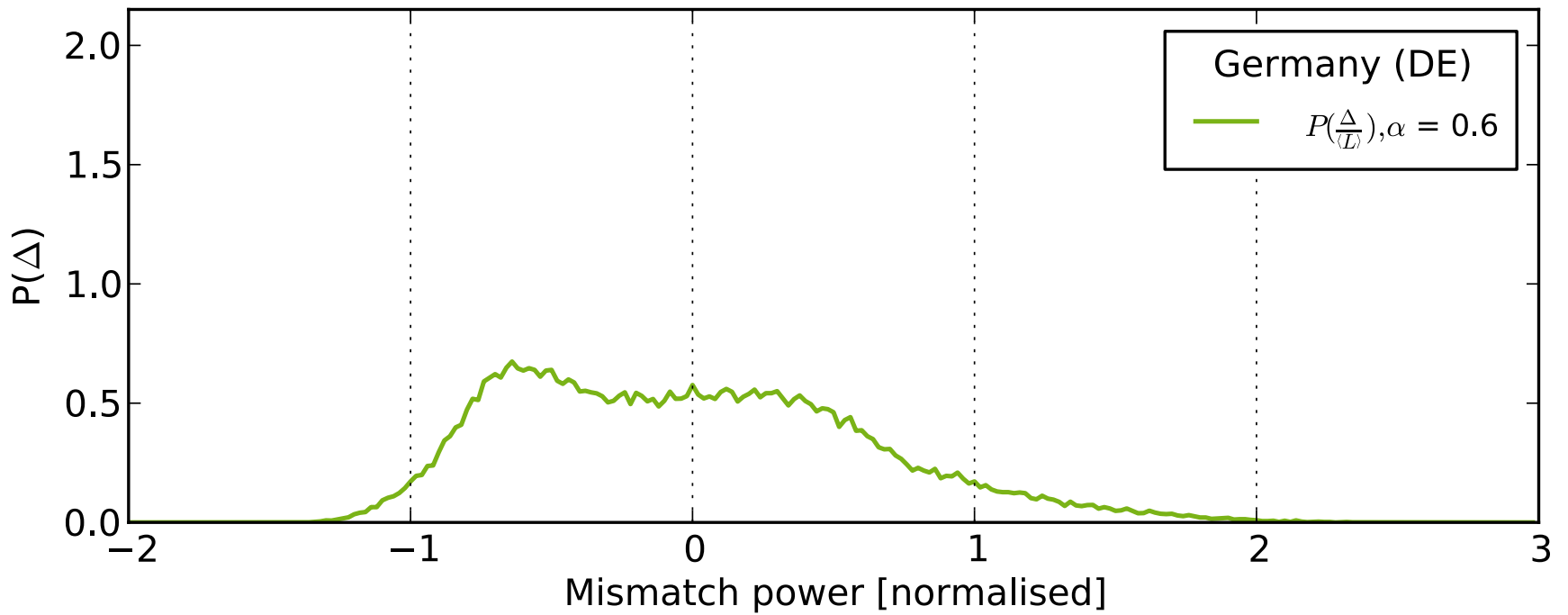


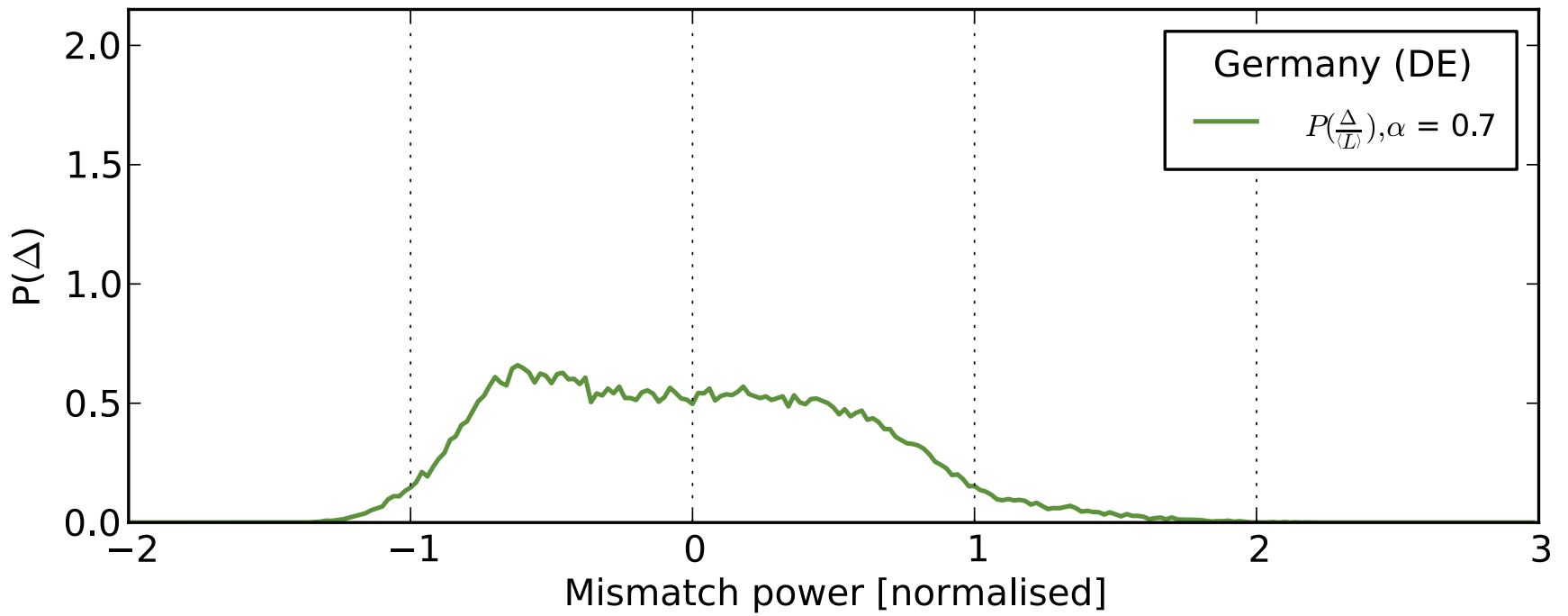


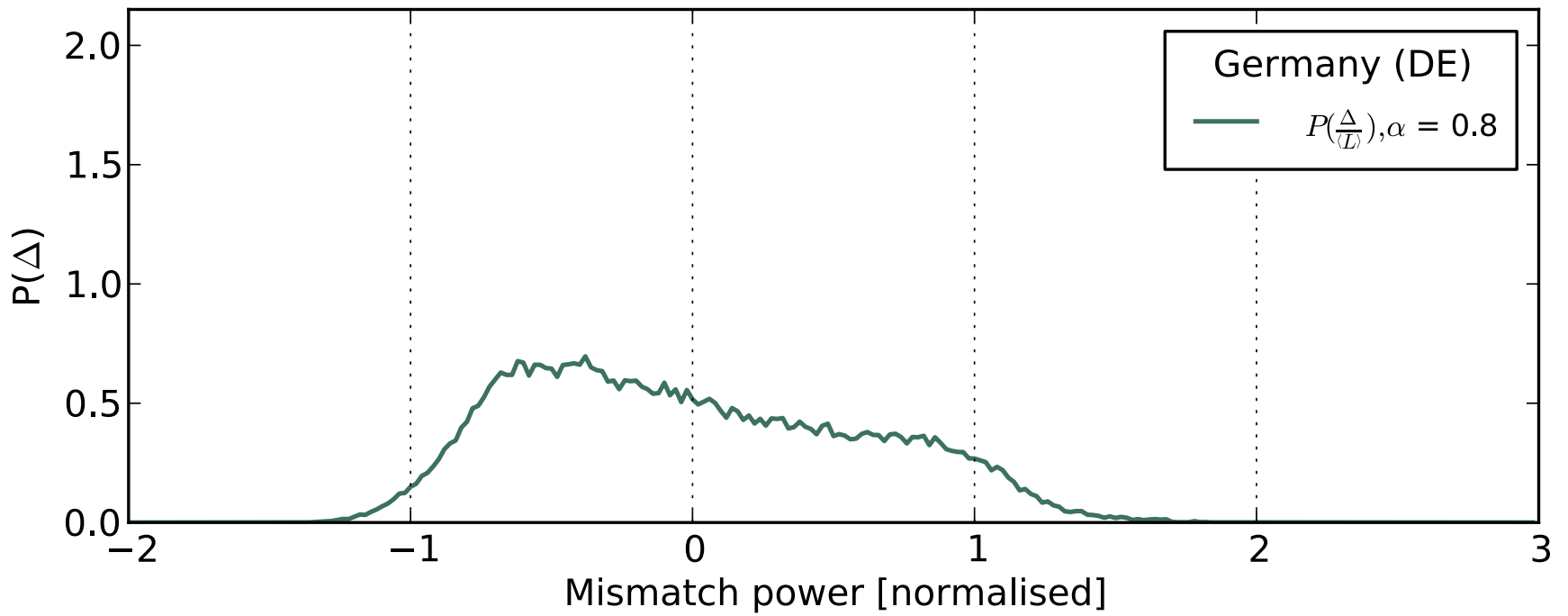


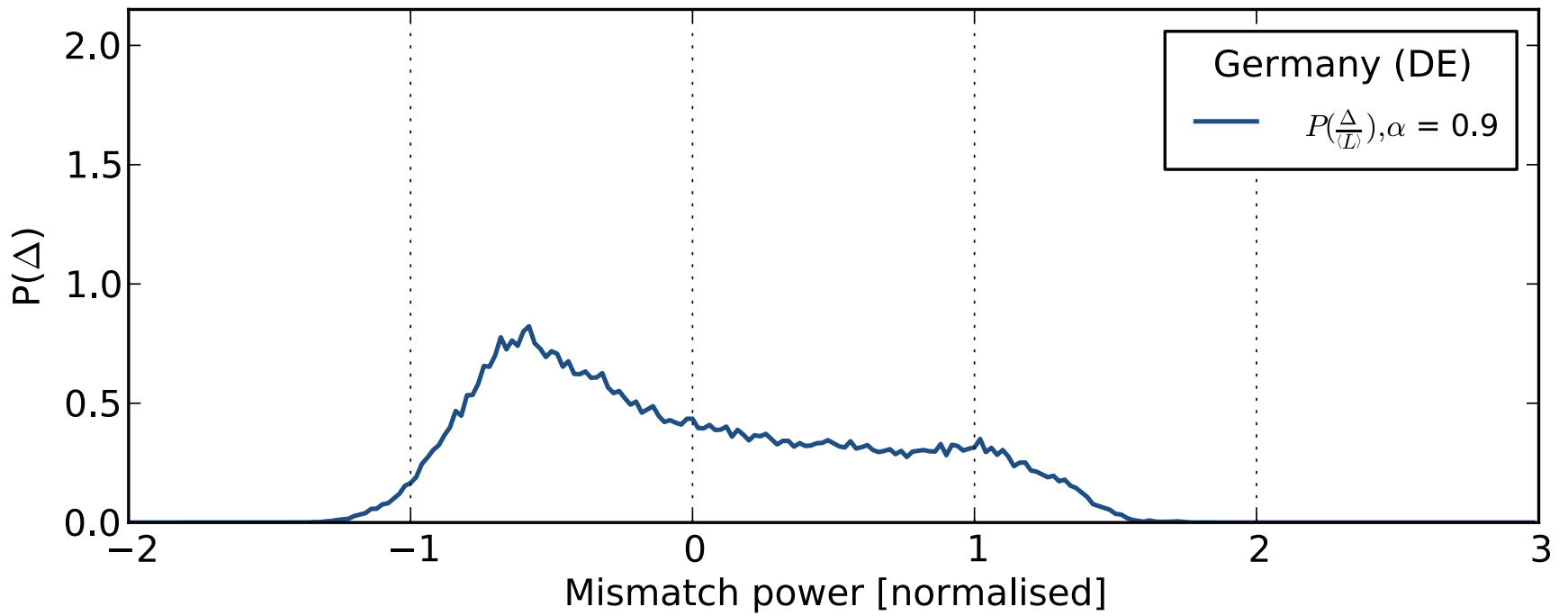


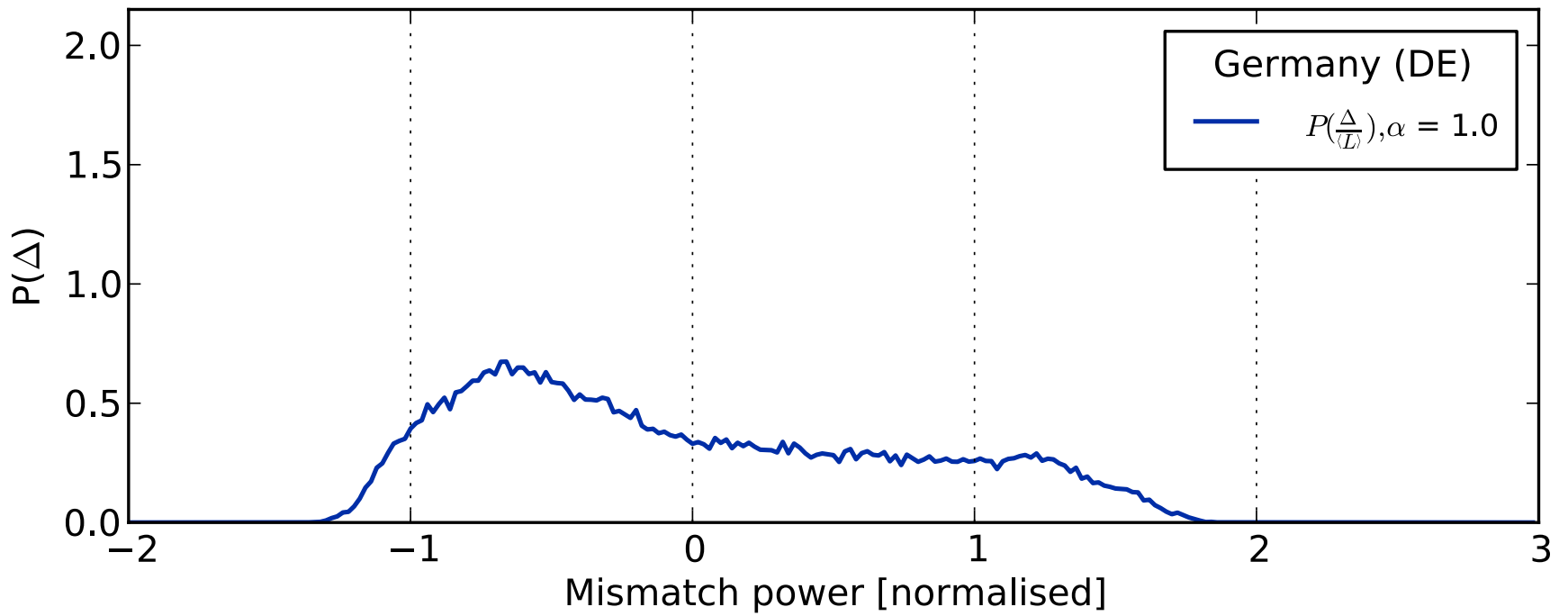










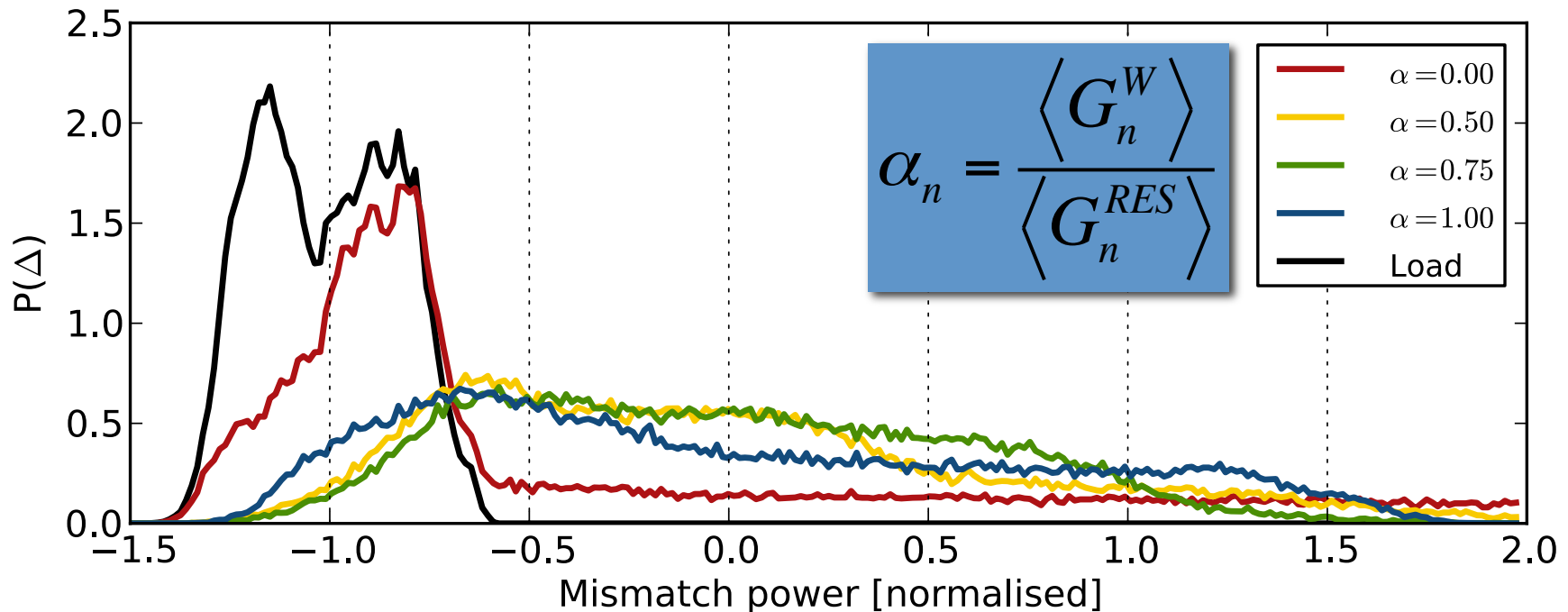


Mismatch distribution (Germany)

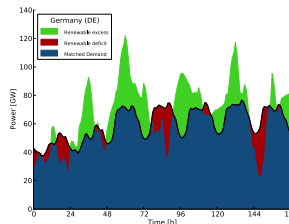
$$\Delta_n(t) = G_n^{RES}(t) - L_n(t) - T_n(t)$$

$$T_n(t) = 0$$

$$\langle G_n^{RES} \rangle = \langle L_n \rangle$$



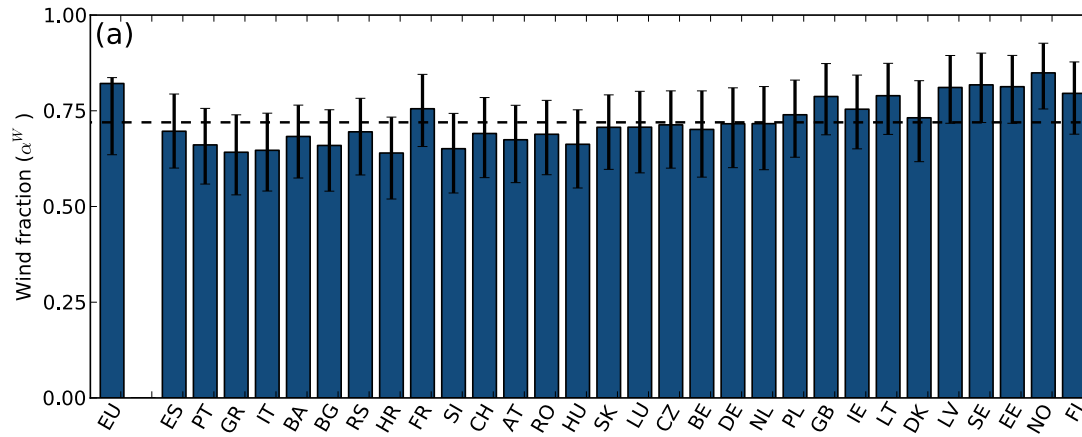
$$B_n(t) = -\min(\Delta(t), 0)$$



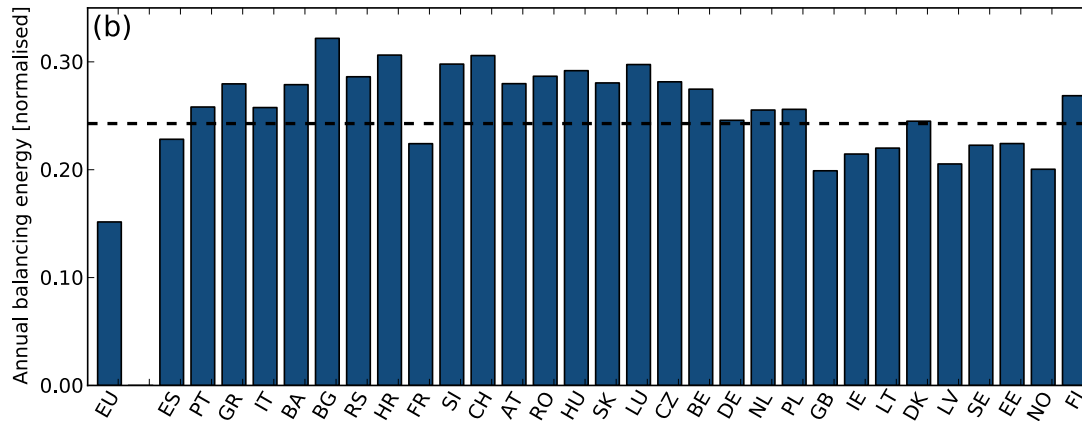
$$C_n(t) = \max(\Delta(t), 0)$$



BACKUP ENERGY: European countries



$$\alpha_{\min}$$



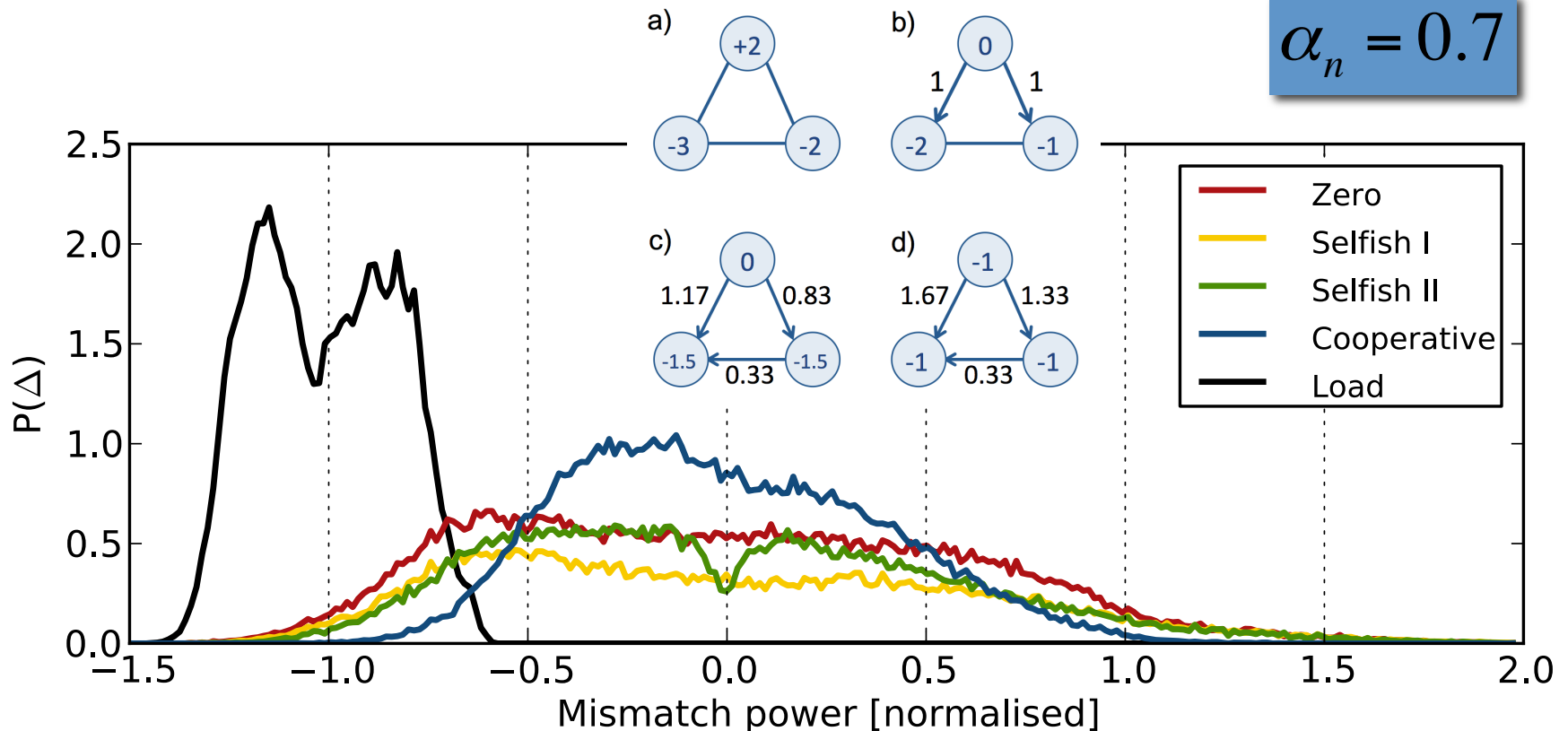
$$\langle B_n \rangle \approx 0.24$$

Mismatch distribution (Germany)

$$\Delta_n(t) = G_n^{RES}(t) - L_n(t) - T_n(t)$$

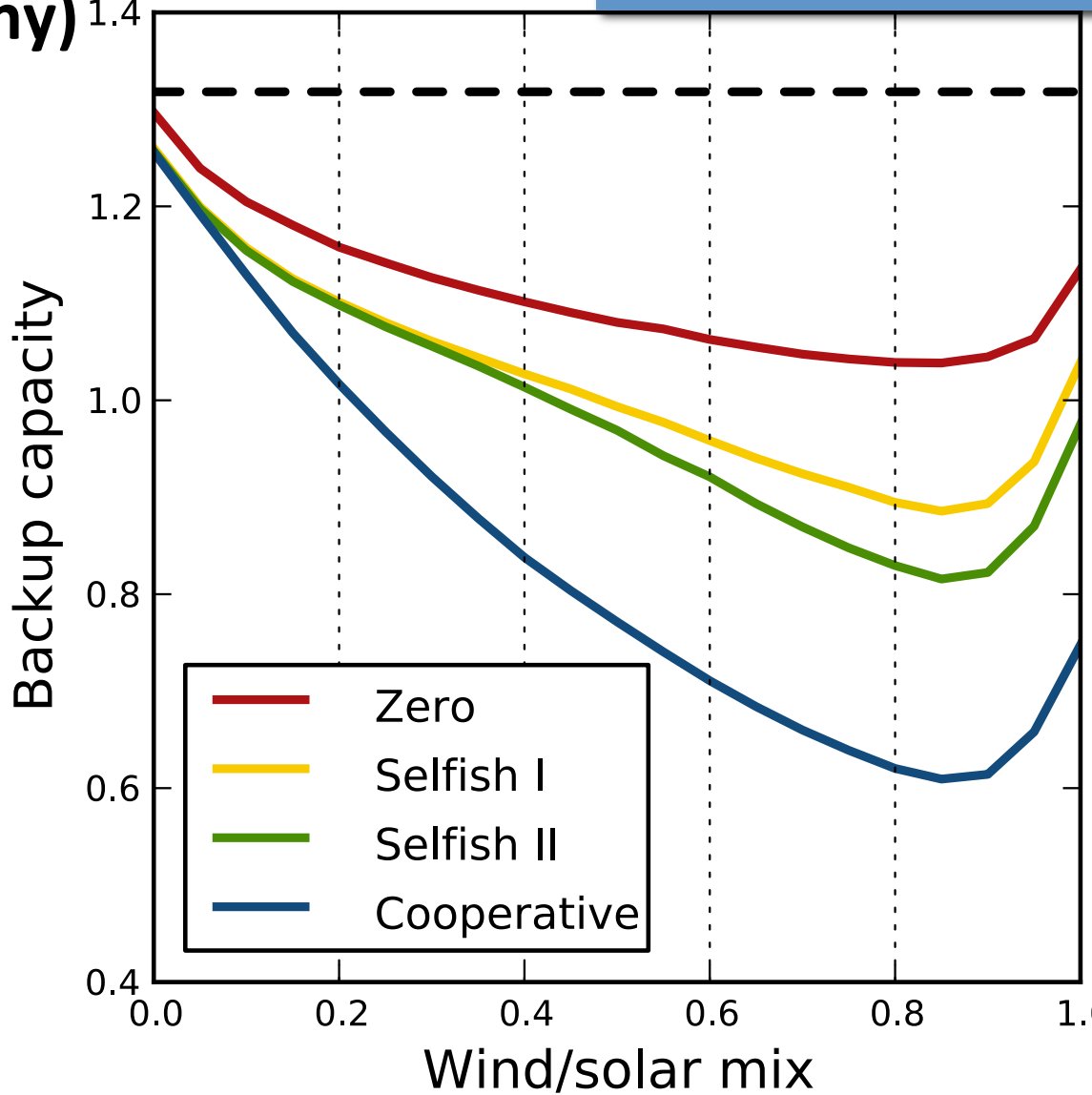
$$\langle G_n^{RES} \rangle = \langle L_n \rangle$$

$$\alpha_n = 0.7$$



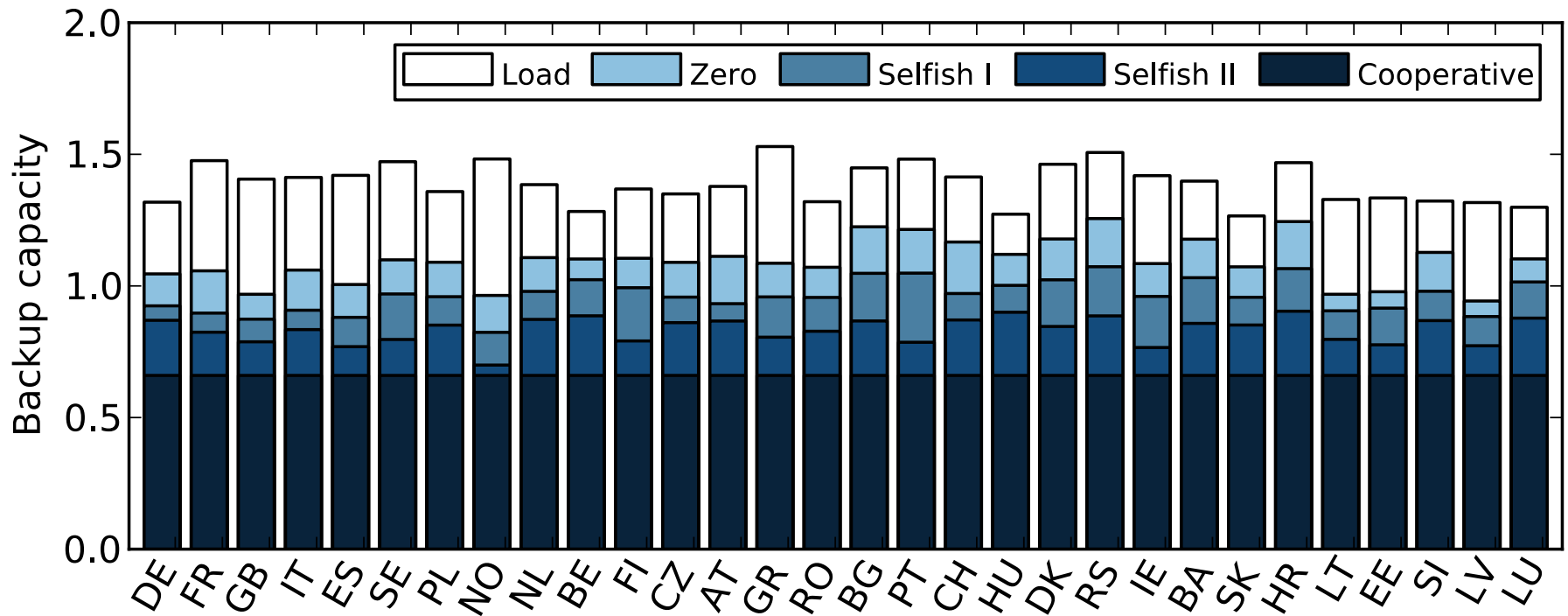
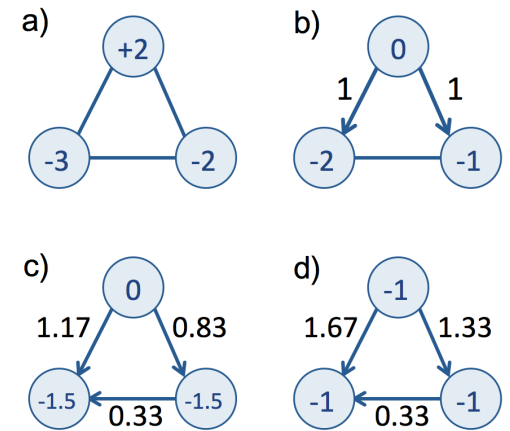
Backup Capacity (Germany)

$$B_n^C = -\min_t (G_n^{RES}(t) - L_n(t) - T_n(t))$$

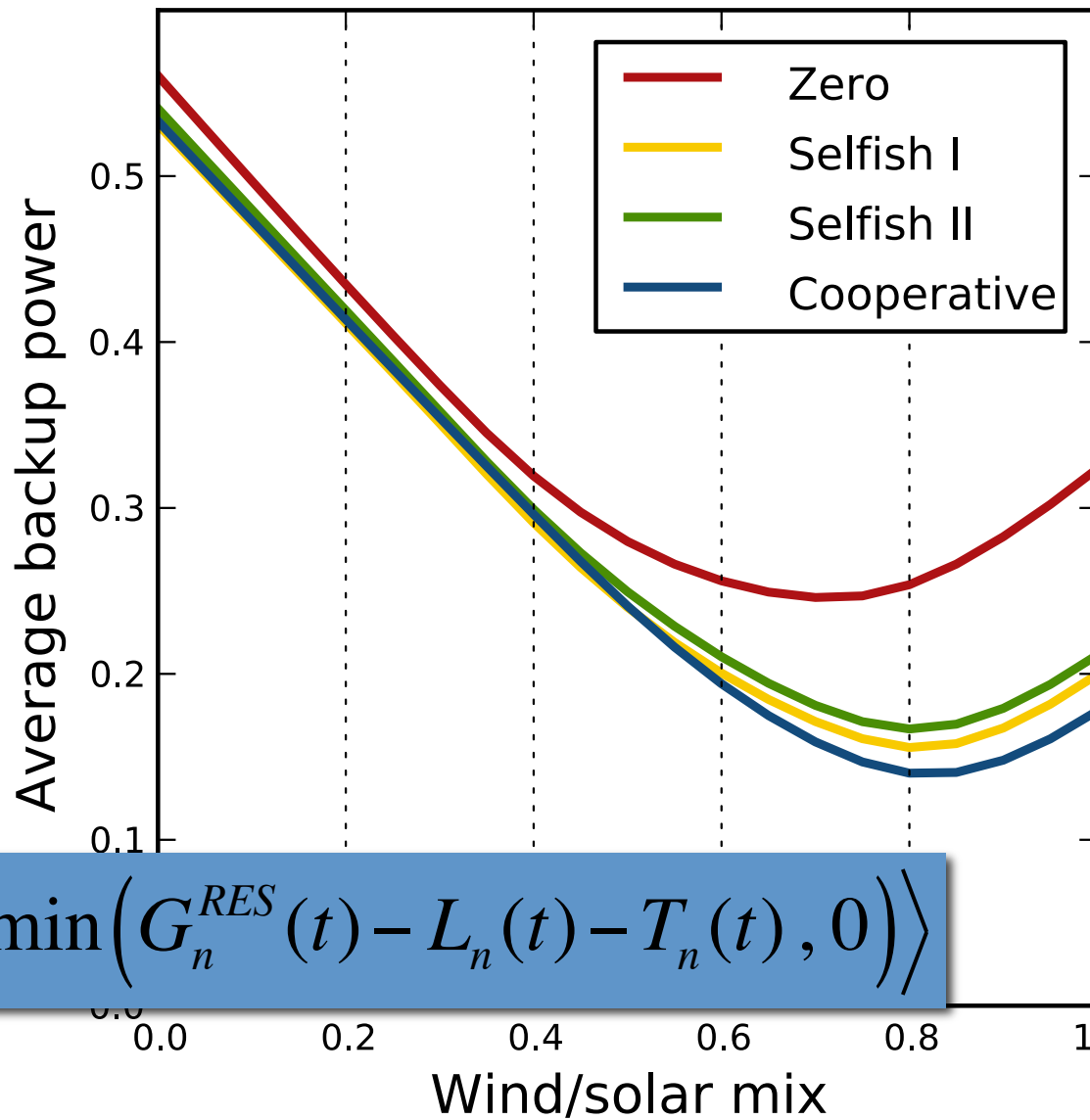


$$\alpha_n = \frac{\langle G_n^W \rangle}{\langle G_n^{RES} \rangle}$$

Backup Capacity



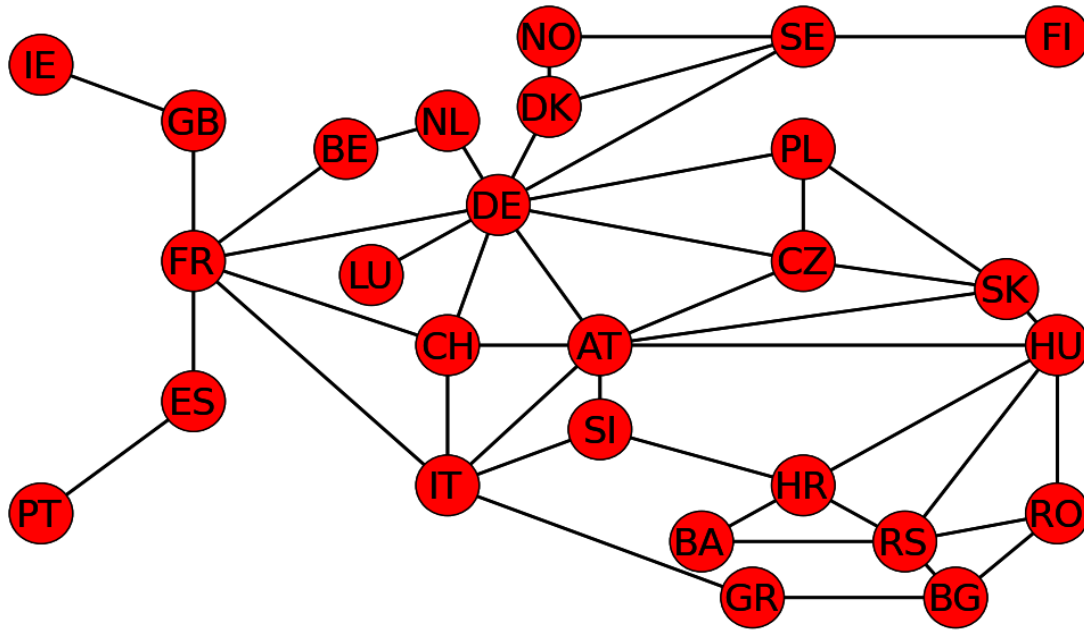
Average Backup Power (Germany)



$$\langle B_n \rangle = - \left\langle \min \left(G_n^{RES}(t) - L_n(t) - T_n(t), 0 \right) \right\rangle$$

$$\alpha_n = \frac{\langle G_n^W \rangle}{\langle G_n^{RES} \rangle}$$

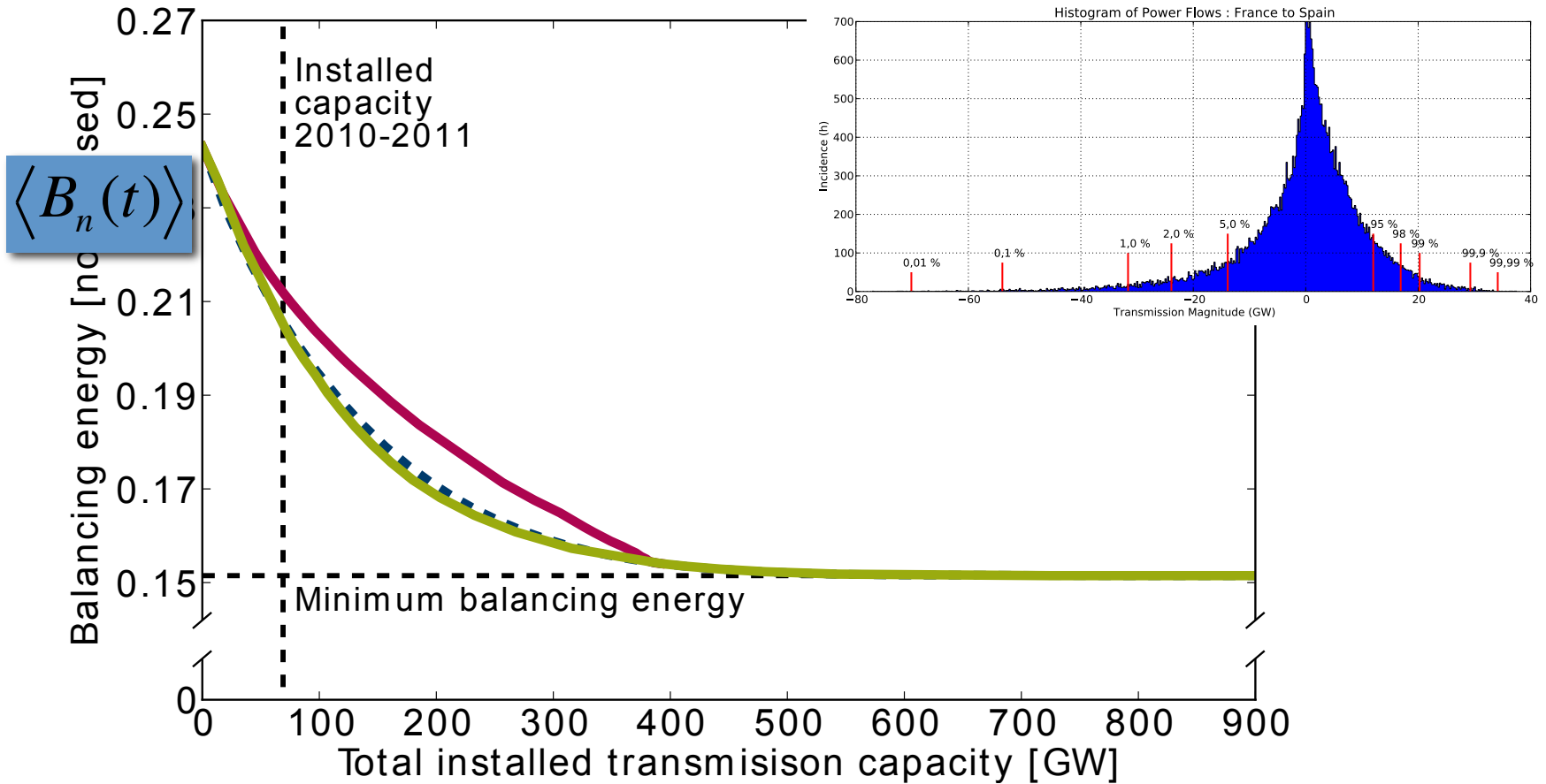
How much transmission?



$$\min \sum_n B_n$$

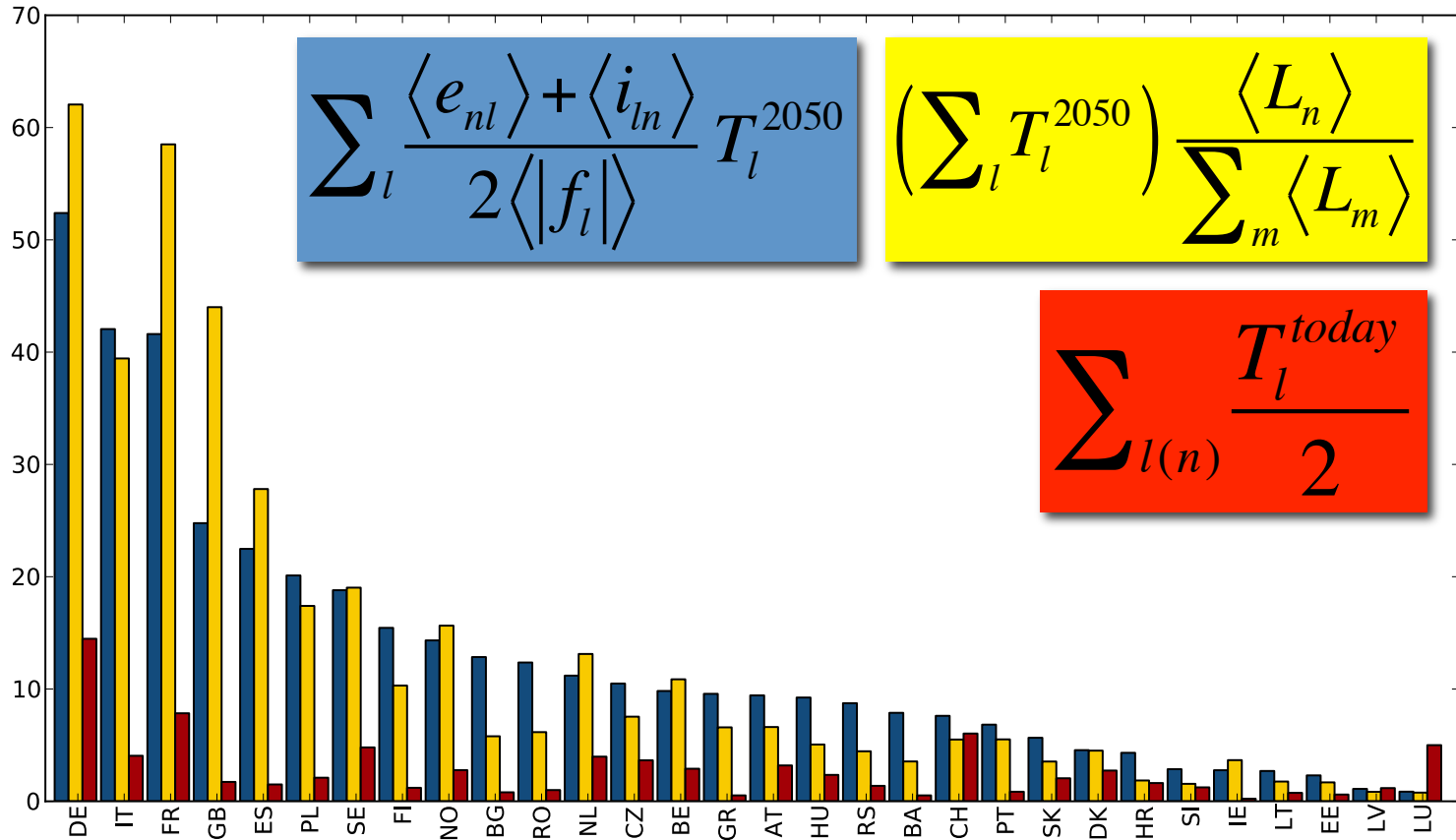
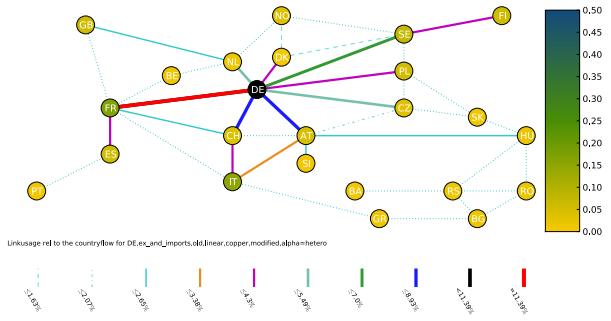
$$\min \sum_l F_l^2$$

Backup vs. Transmission

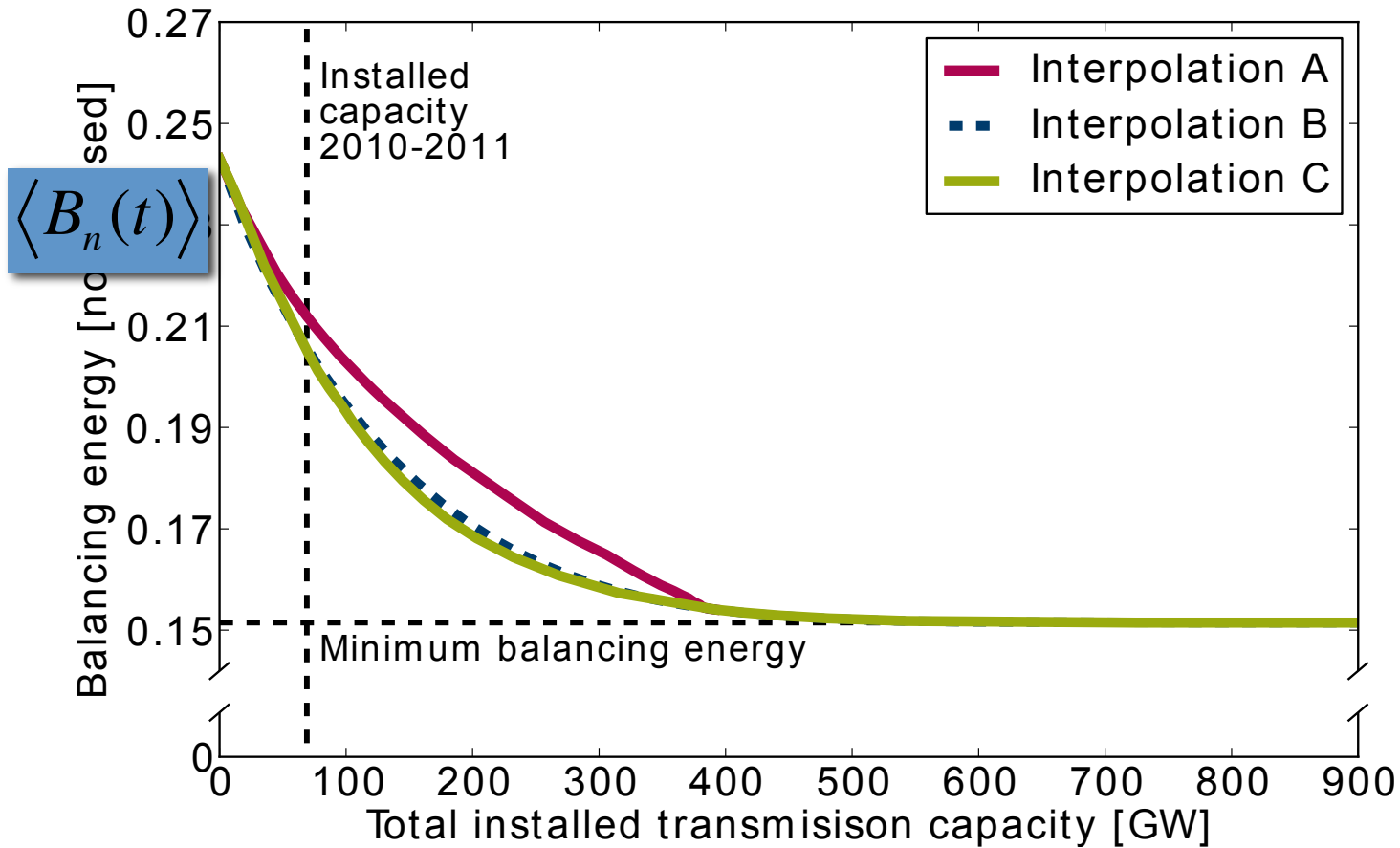


Who pays the transmission bill?

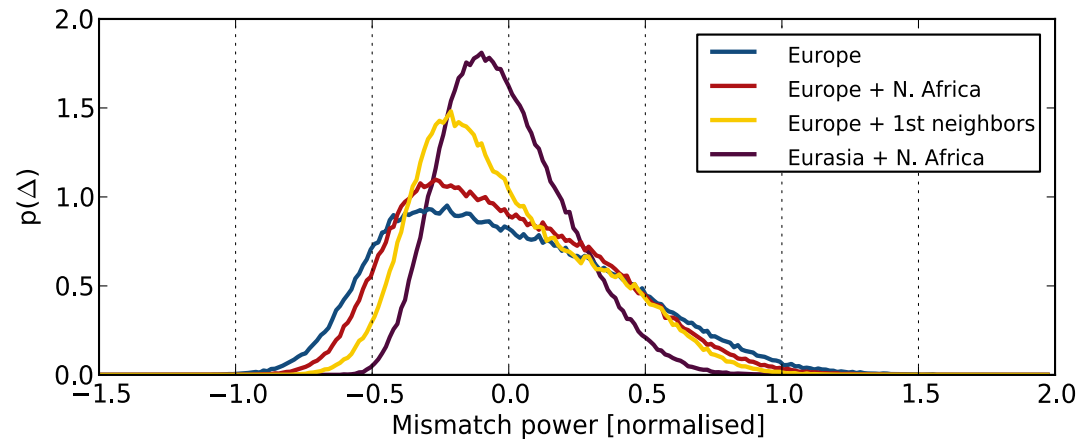
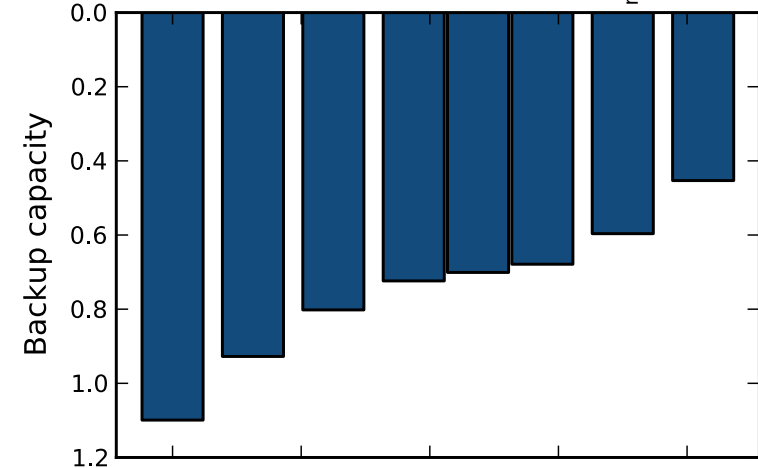
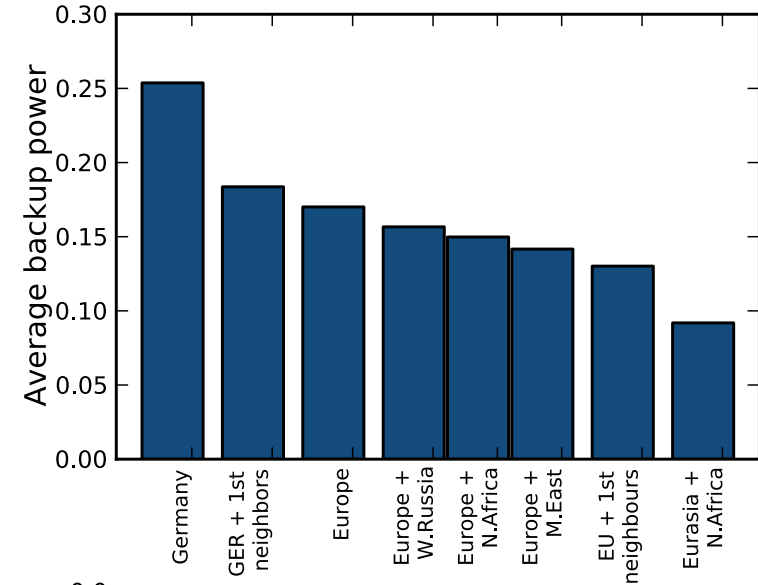
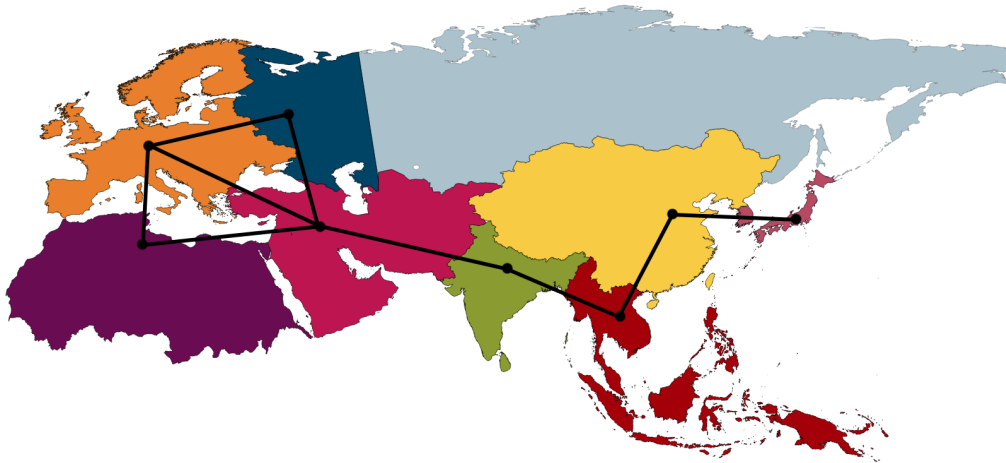
..... Flow tracing



More reduction of backup?



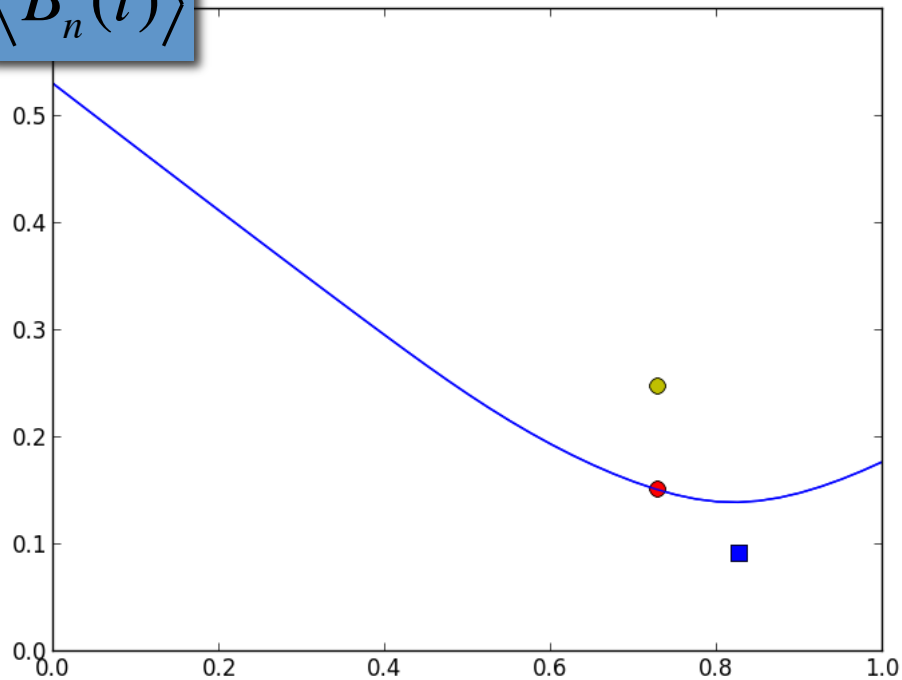
Answer 1: Transmission beyond EU



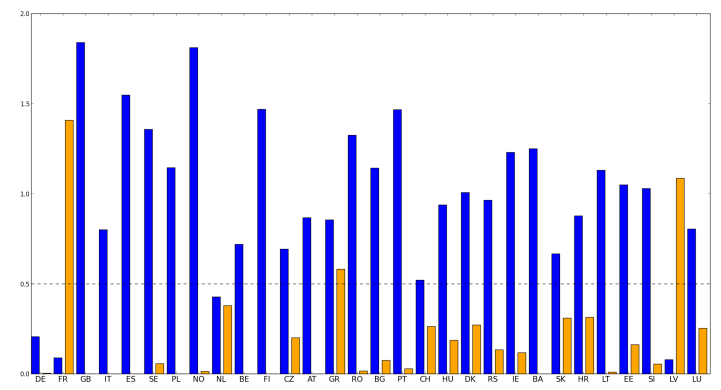
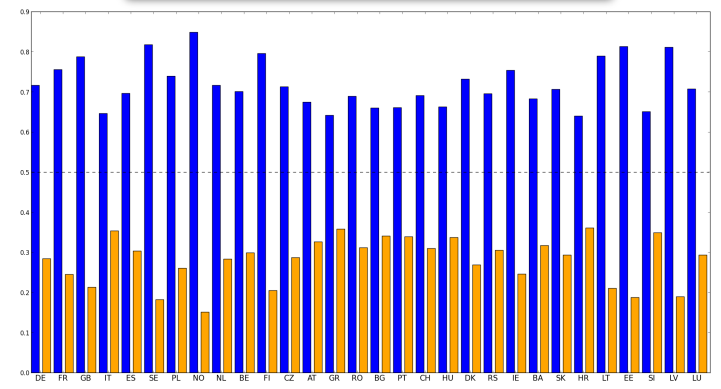
Answer 2: Optimization

optimal portfolio theory,
genetic optimization

$$\langle B_n(t) \rangle$$



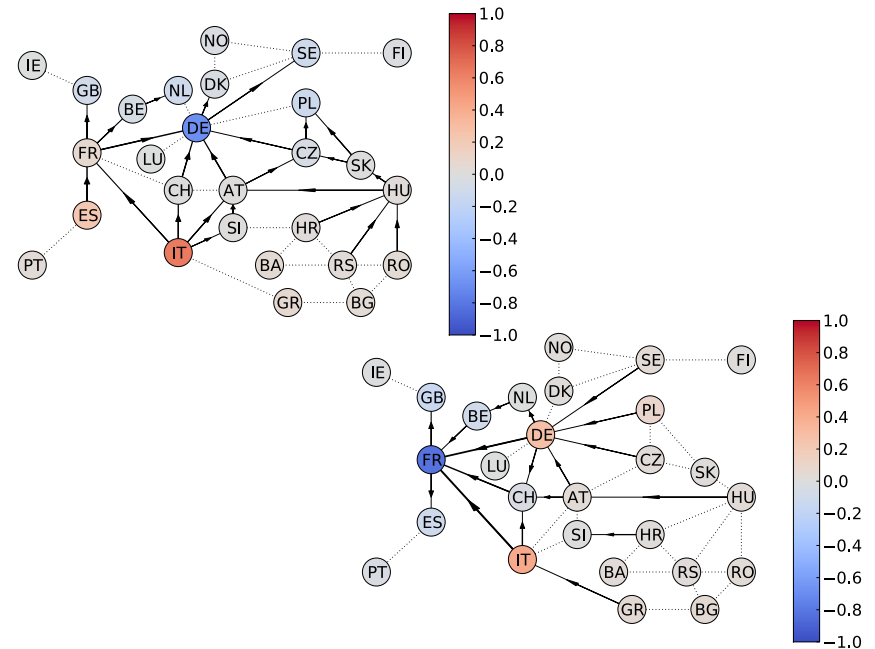
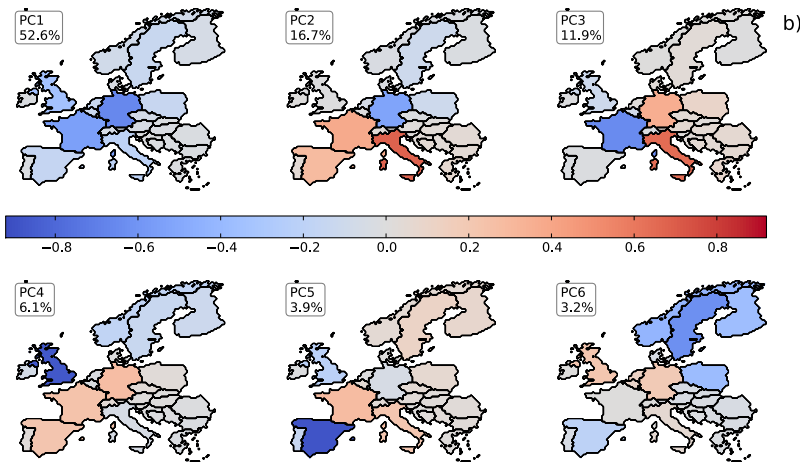
$$\langle G_n^{RES} \rangle_t = \langle L_n \rangle_t$$



$$\sum_n \langle G_n^{RES} \rangle_t = \sum_n \langle L_n \rangle_t$$

Fundamental Research on Renewable Energy Systems at the interface between engineering + mathematics + physics

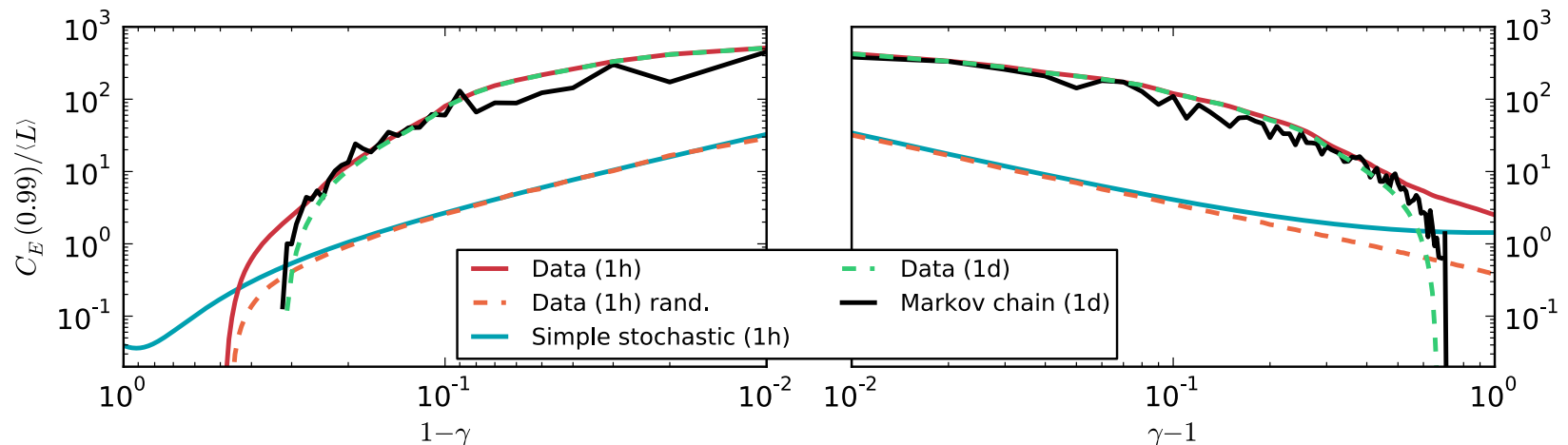
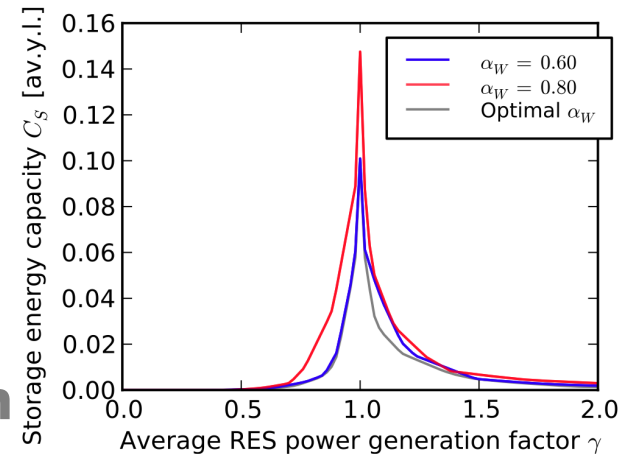
SOME FUNDAMENTAL CHALLENGES:
storage phase transition,
renormalisation scaling of power flows,
spatio-temporal flow pattern analysis,
self-organizing power flows,
emergence of socio-economic cooperation



Fundamental Research on Renewable Energy Systems at the interface between engineering + mathematics + physics

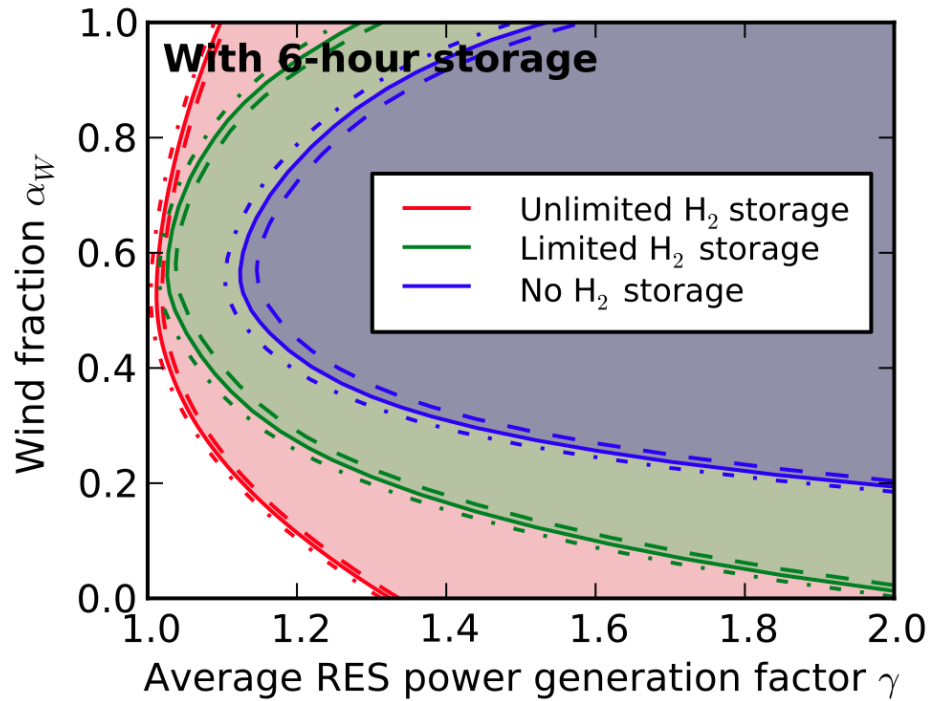
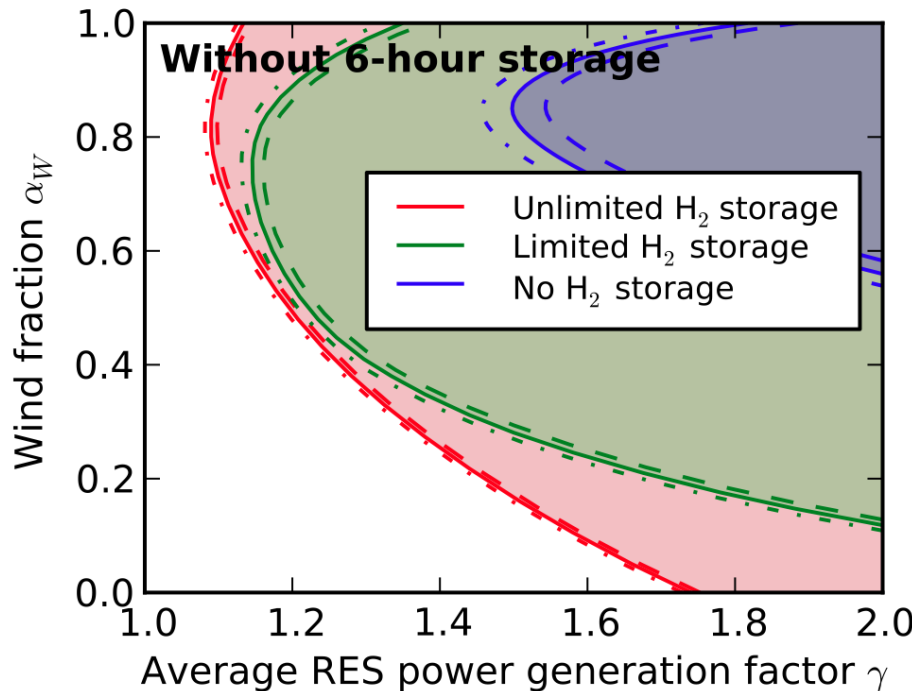
SOME FUNDAMENTAL CHALLENGES:

storage phase transition,
renormalisation scaling of power flows,
spatio-temporal flow pattern analysis,
self-organizing power flows,
emergence of socio-economic cooperation



Synergies: balancing + storage

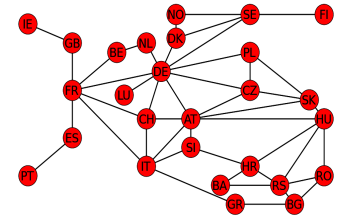
6h "battery" storage (2.2 TWh, $\eta=1.0$)
+ seasonal H₂ storage (25 TWh, $\eta=0.6$)
+ "hydro/bio" balancing (150 TWh)



Fundamental Research on Renewable Energy Systems at the interface between engineering + mathematics + physics

BIG SIMULATION: **100% = 100+X%**
COMPLEX NETWORKS OF SMART ENERGY SYSTEMS

all renewables + backup +
+ transmission + storage,
electricity + heating + transportation



DESIGN OF FUTURE ENERGY MARKETS

OPTIMAL TRANSITION 2050 → 2015

Fundamental Research on Renewable Energy Systems

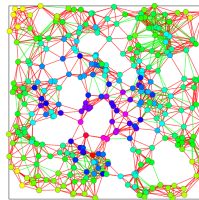
at the interface between engineering + mathematics + physics

Martin Greiner, Aarhus University
greiner@eng.au.dk

(1) 100% Renewable Energy Systems

G Andresen (PostDoc)
R Rodriguez (PHD)
S Becker (FIAS PhD)
B Sairanen (Master)
A Thomsen (Master)
M Dahl (Master)

(2) Complex Networks



C Hoffmann (IWES)
M Rasmussen (PostDoc)
D Heide (PhD)
T Jensen (Master)
A Søndergaard (Master)
T Zeyer (Master)

(3) Wind-farm Modeling + Optimization



U Poulsen (Assistant Professor)
J Herp (Master)