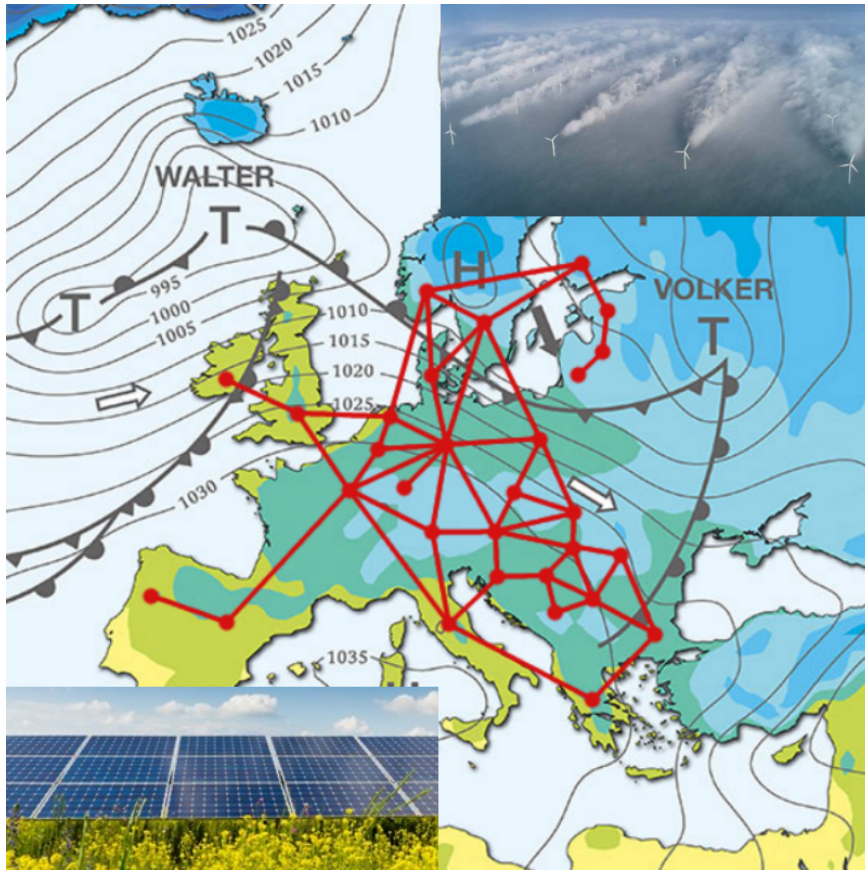


# Flow-tracing and nodal cost allocation

## in a heterogeneous highly renewable European electricity network



**E Eriksen, L Schwenk-Nebbe, B Tranberg, T Brown, M Greiner:**  
*Optimal heterogeneity of a simplified highly renewable pan-European electricity system,*  
**Energy 133 (2017) 913-28.**

**B Tranberg, L Schwenk-Nebbe, M Schäfer, J Hörsch, M Greiner:**  
*Flow-based nodal cost allocation in a heterogeneous highly renewable European electricity system,*  
**Energy (2018) in press.**

**B Tranberg, A Thomsen, R Rodriguez, G Andresen, M Schäfer, M Greiner:**  
*Power flow tracing in a simplified highly renewable European electricity network,*  
**New J. Physics 17 (2015) 105002.**

**M Schäfer, B Tranberg, S Hempel, S Schramm, M Greiner:**  
*Decompositions of injection patterns for nodal flow allocation in renewable electricity networks,*  
**Eur. Phys. J. B 90 (2017) 144.**

**J Hörsch, M Schäfer, S Becker, S Schramm, M Greiner:**  
*Flow tracing as a tool set for the analysis of networked large-scale renewable electricity systems,*  
**Int. J. Electrical Power and Energy Systems 96 (2018) 390-97.**

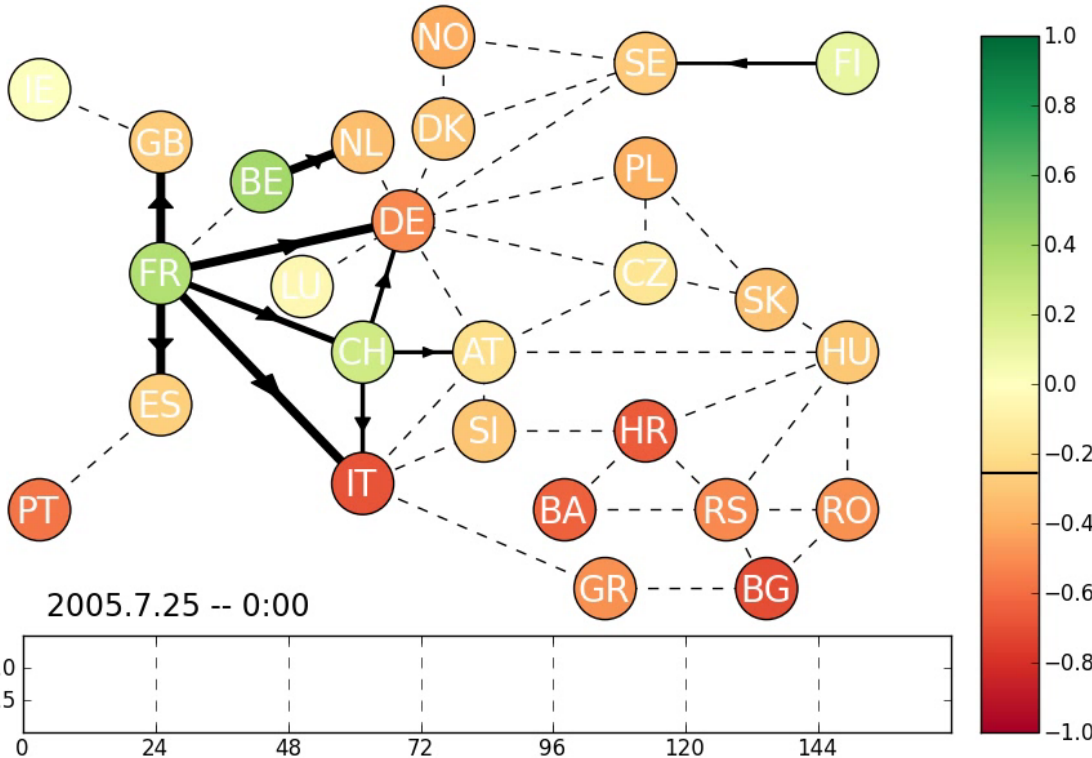
# Renewable European electricity network + fluctuating „weather forces“

$$G_n^R(t) = G_n^W(t) + G_n^S(t)$$

$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$

$$G_n^R(t) - L_n(t) = B_n(t) + P_n(t) + \dots$$



$$G_n^B(t) = (B_n(t))_-$$

$$C_n(t) = (B_n(t))_+$$

$$\sum_n P_n(t) = 0$$

$$F_l(t) = \sum_n H_{ln} P_n(t)$$

# Infrastructure measures

**backup energy**

$$E_n^B = \langle G_n^B \rangle$$

**backup capacity**

$$K_n^B = \max_q (G_n^B)$$

**transmission capacity**

$$K_l^T = \max_q |F_l| \cdot d_l$$

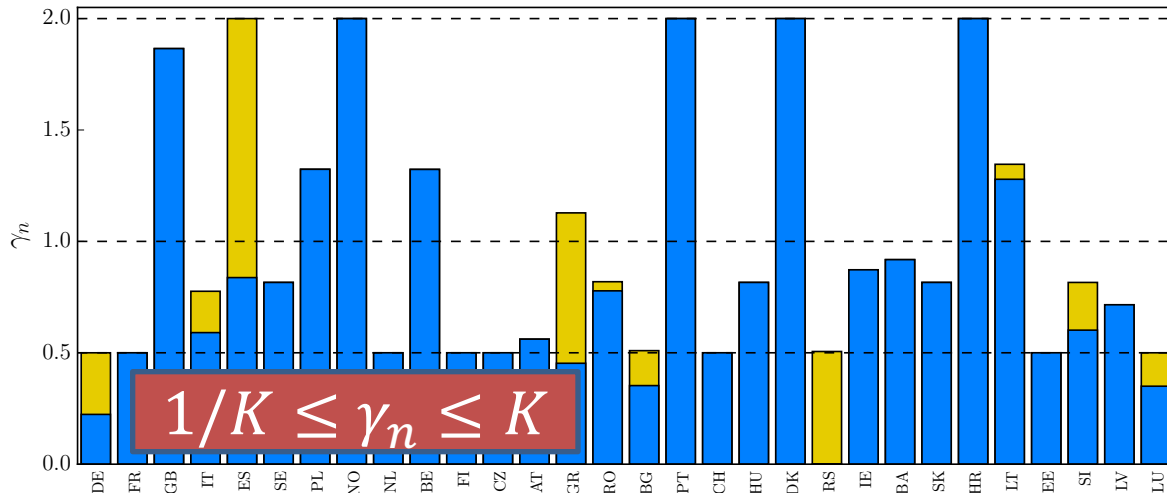
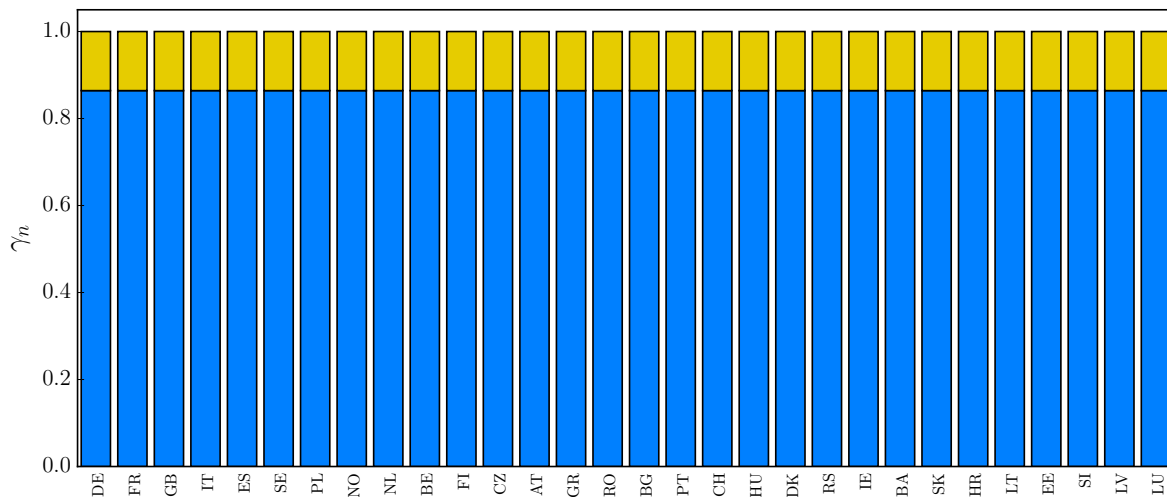
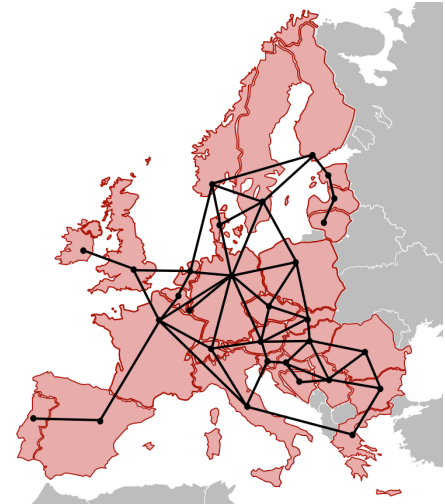
**wind capacity**

$$K_n^W = \frac{\alpha_n \gamma_n \langle L_n \rangle}{CF_n^W}$$

**solar capacity**

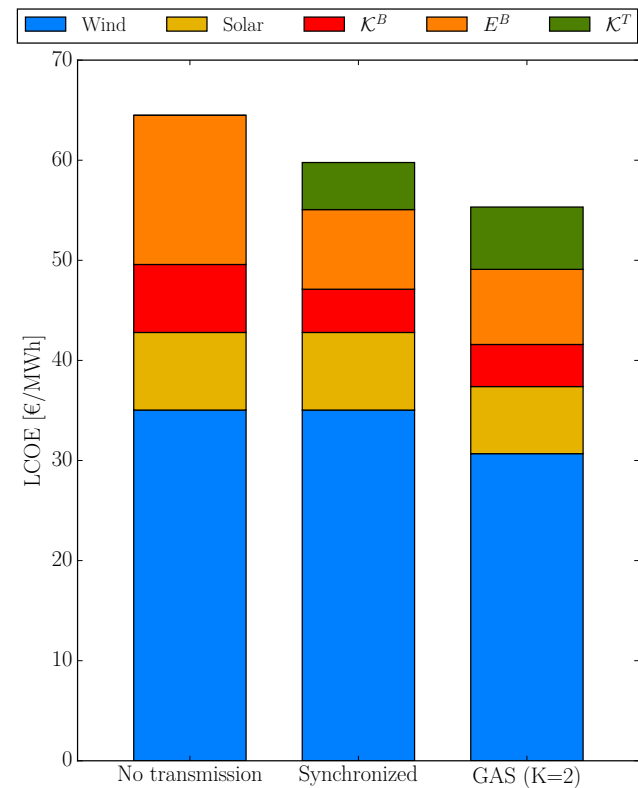
$$K_n^S = \frac{(1 - \alpha_n) \gamma_n \langle L_n \rangle}{CF_n^S}$$

# Breaking homogeneity: cost-optimal heterogeneity



$$\langle G_n^R \rangle = \gamma_n \langle L_n \rangle$$

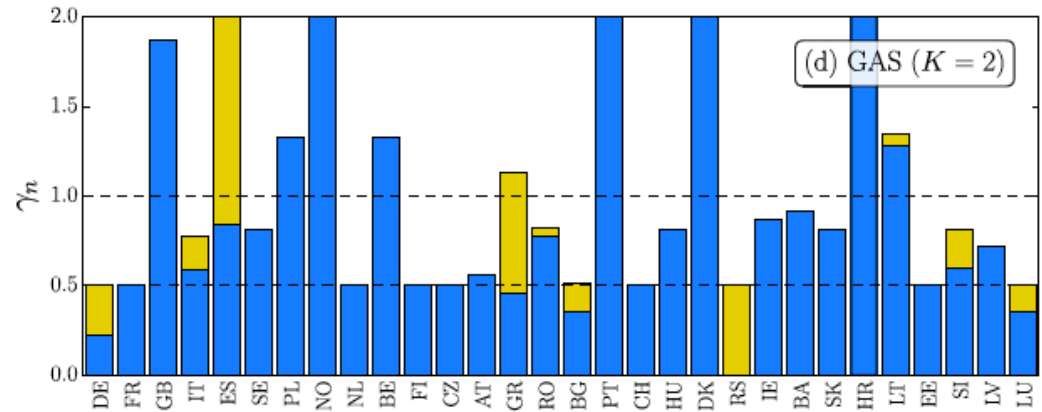
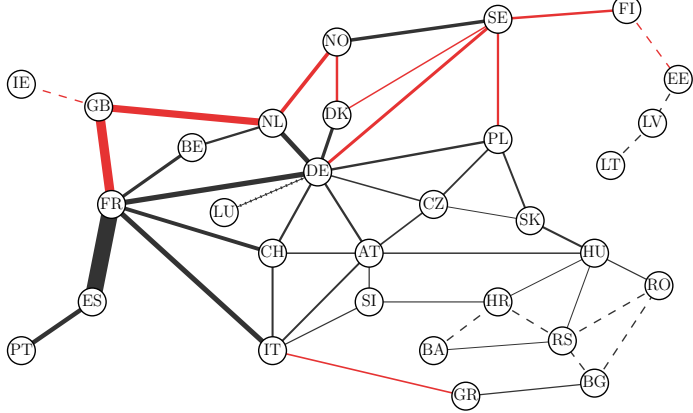
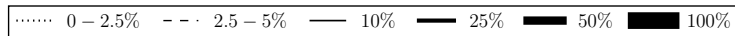
$$\langle G_n^W \rangle = \alpha_n \langle G_n^R \rangle$$



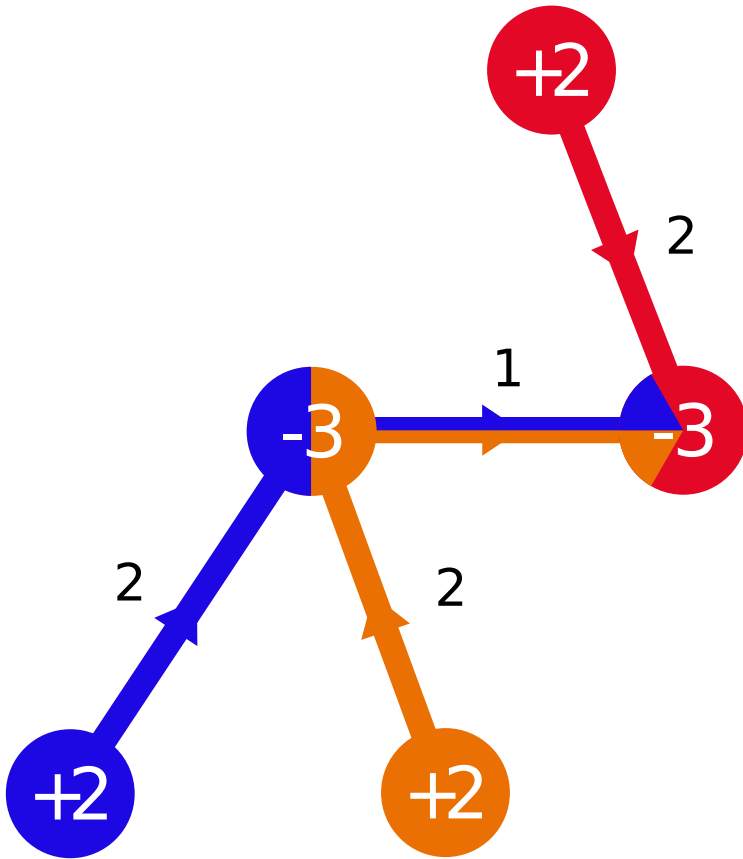
# Who pays for ...

## ... the transmission grid?

## ... the heterogeneity?



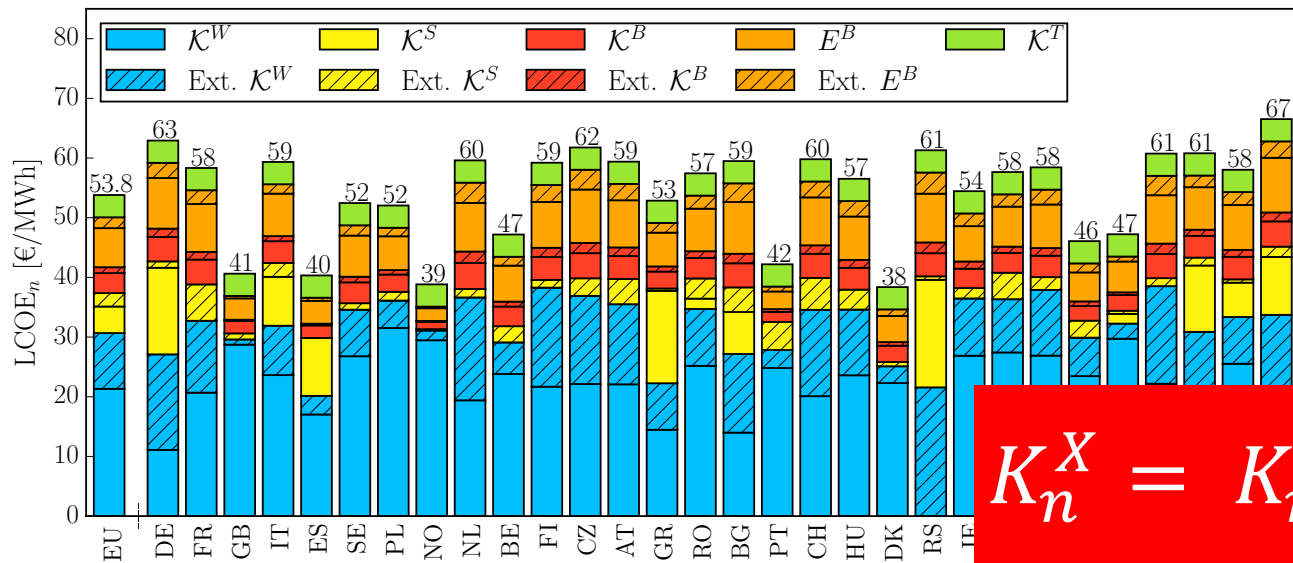
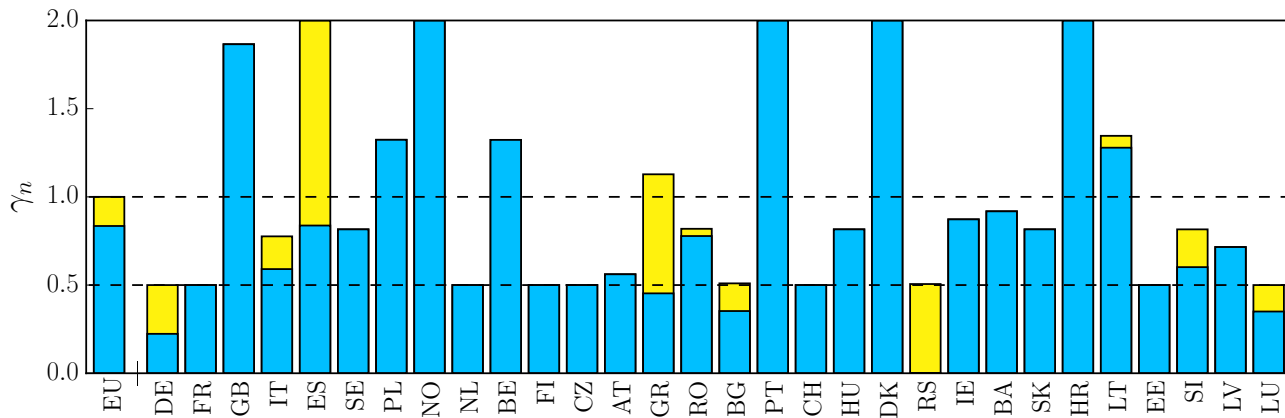
# Flow tracing



$$K_n^X = K_{nn}^X + \sum_{m \neq n} K_{nm}^X$$

$$\tilde{K}_n^X = K_{nn}^X + \sum_{m \neq n} K_{mn}^X$$

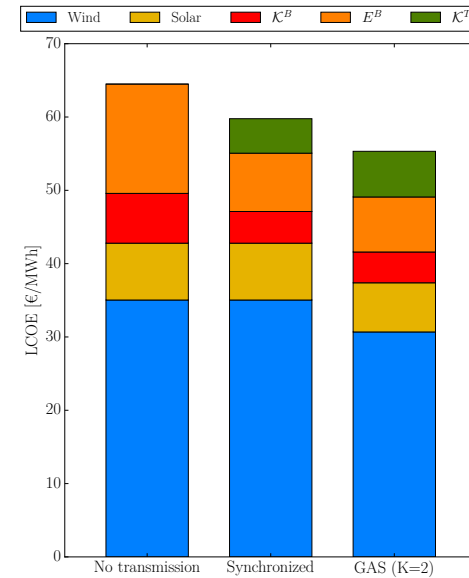
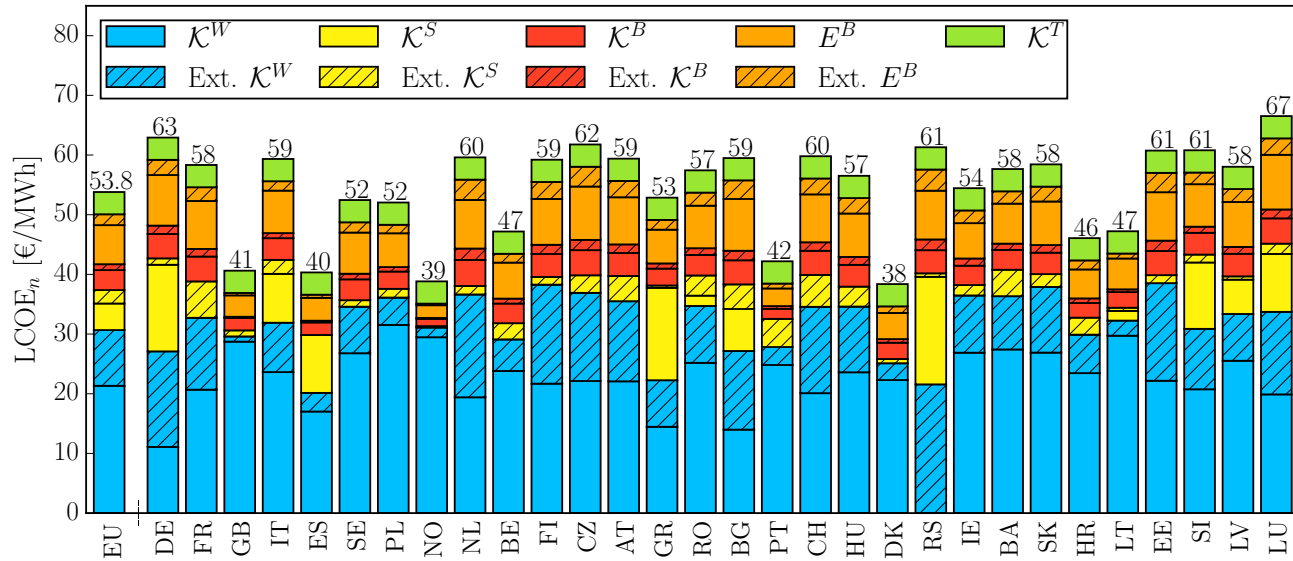
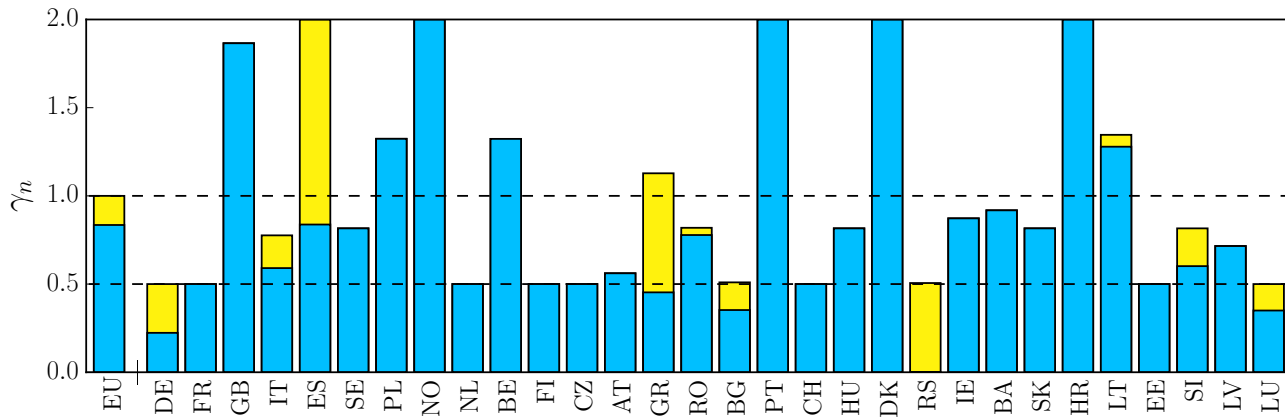
# Who pays for the heterogeneity?



$$K_n^X = K_{nn}^X + \sum_{m \neq n} K_{nm}^X$$

$$\tilde{K}_n^X = K_{nn}^X + \sum_{m \neq n} K_{mn}^X$$

# Benefit of cooperation



$$\forall n: LCOE_n^{hom,notT} > LCOE_n^{hom,T} > LCOE_n^{het,T}$$



# next “physics” challenges

## big networks:

**power-flow renormalization  
small-world AC/DC networks,  
self-organizing power flows.**



A LETTERS JOURNAL EXPLORING  
THE FRONTIERS OF PHYSICS

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EPL, 119 (2017) 38004

doi: 10.1209/0295-5075/119/38004

## emerging renewable energy networks: socio-economic market + investment games

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**THE EUROPEAN  
PHYSICAL JOURNAL B**

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Eur. Phys. J. B (2017) 90: 144

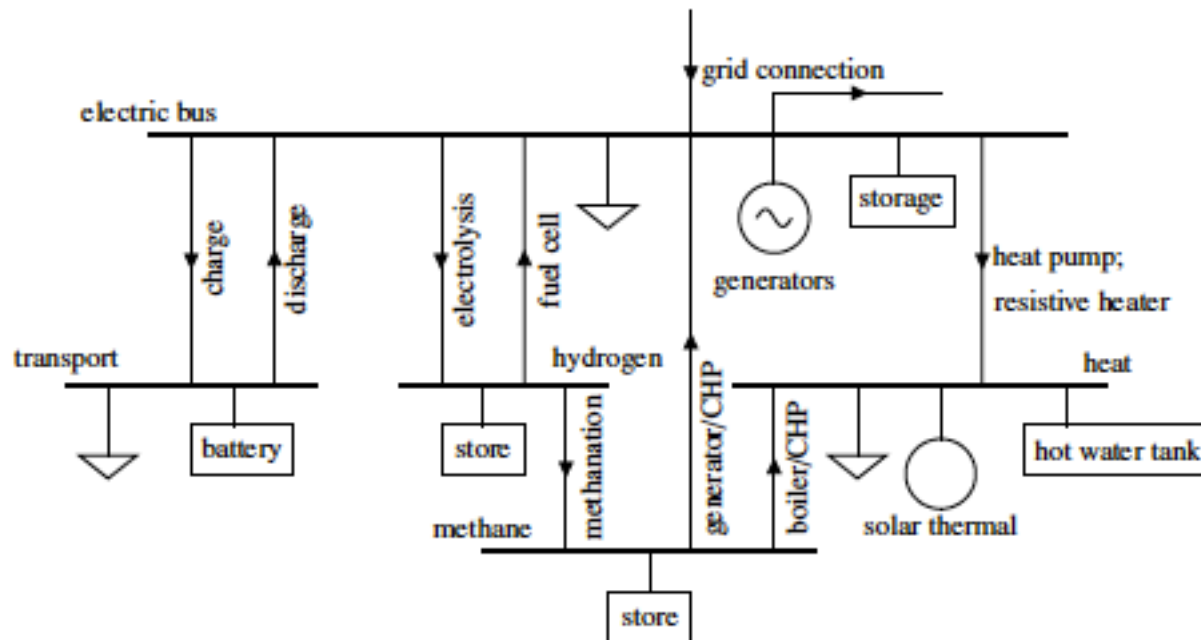
DOI: 10.1140/epjb/e2017-80200-y



AARHUS  
UNIVERSITY  
DEPARTMENT OF ENGINEERING

# “engineering” challenge: electricity → “smart” energy system

## cross-sector coupling



# Synergies of sector coupling and transmission extension in a cost-optimised, highly renewable European energy system

submitted to  
Energy

T. Brown<sup>a,\*</sup>, D. Schlachtberger<sup>a</sup>, A. Kies<sup>a</sup>, S. Schramm<sup>a</sup>, M. Greiner<sup>b</sup>

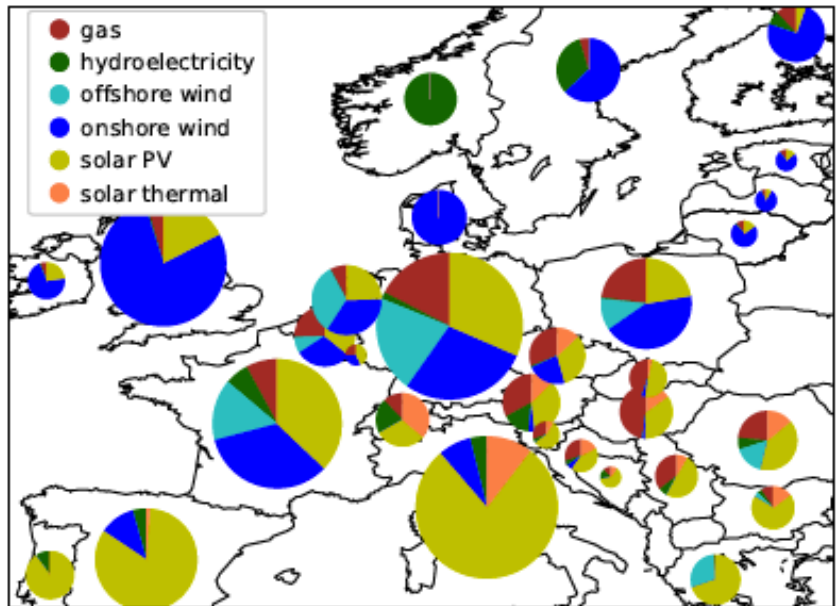
$$\min_{\substack{G_{n,s}, E_{n,s}, F_\ell, \\ g_{n,s,t}, f_{\ell,t}}} \left[ \sum_{n,s} c_{n,s} \cdot G_{n,s} + \sum_{n,s} \hat{c}_{n,s} \cdot E_{n,s} + \sum_{\ell} c_{\ell} \cdot F_{\ell} + \sum_{n,s,t} o_{n,s,t} \cdot g_{n,s,t} \right] \quad (1)$$

$$\sum_s g_{n,s,t} + \sum_{\ell} \alpha_{\ell,n,t} \cdot f_{\ell,t} = d_{n,t} \quad \leftrightarrow \quad \lambda_{n,t} \quad \forall n,t$$

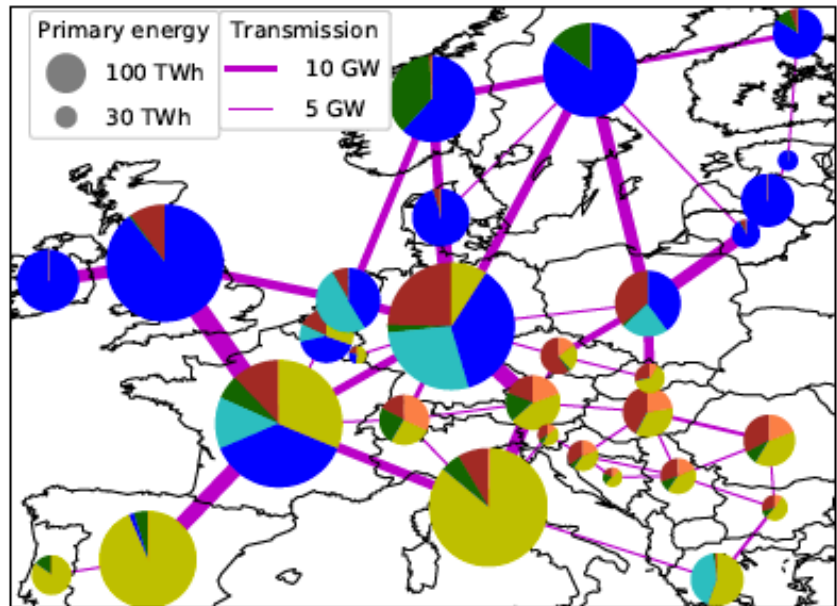
$$\sum_{\ell \in \text{HVDC}} l_{\ell} \cdot F_{\ell} \leq \text{CAP}_{LV}$$

$$\sum_{n,s,t} \varepsilon_s \frac{g_{n,s,t}}{\eta_{n,s}} + \sum_{n,s} \varepsilon_s (e_{n,s,t=0} - e_{n,s,t=T}) \leq \text{CAP}_{CO2} \quad \leftrightarrow \quad \mu_{CO2}$$

Scenario All-Flex-Central with no transmission



Scenario All-Flex-Central with optimal transmission

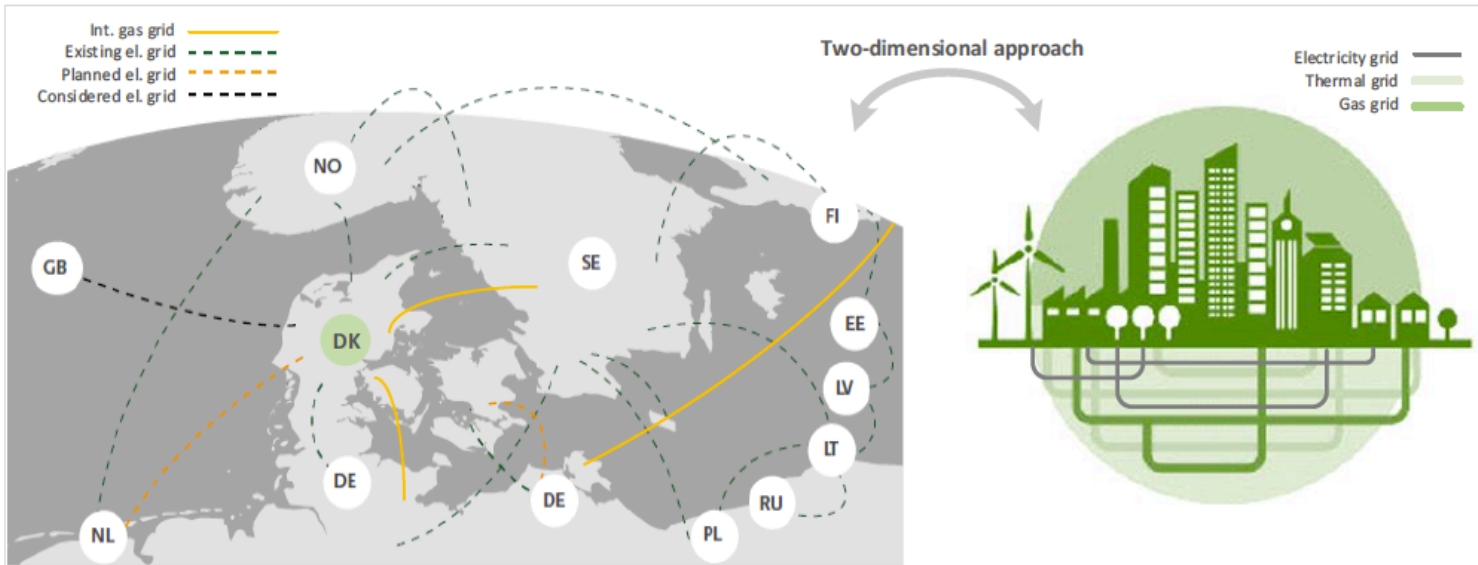
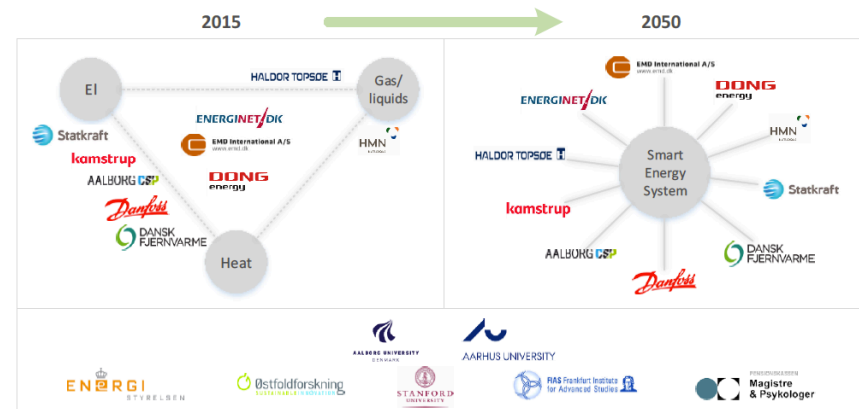


# „Energiewende“: kickoff to the second half

Danmarks Innovationsfond Grand Solutions  
(04.2017-03.2021, 2.3 M€)

## RE-Invest

Renewable Energy Investment Strategies  
– a 2dim interconnectivity approach



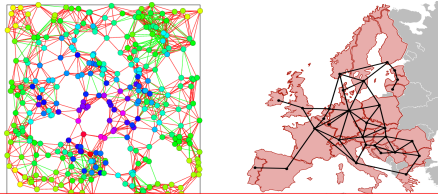
Aalborg U  
+  
Aarhus U

Figure 1. RE-Invest will combine the Smart Energy Systems cross-sectoral approach (right side) at Aalborg University with the cross-border approach (left side) and tools developed by Aarhus University at the European scale. This will lead to a **novel two-dimensional interconnectivity approach** for the design of robust and cost-effective investment strategies towards a sustainable energy system.

**Gorm Andresen** + **Mahdi Abkar** +  
**Martin Greiner** (greiner@eng.au.dk)

**(1) Highly Renewable Energy Networks**

**(2) Complex Networks**



**(3) Wind-farm Modeling + Optimization**

**(4) Turbulence**

J Trane (Master18)  
 A Khamas (Master18)  
 B Carlsen (Master16)  
 A Huche (Master16)  
 E Thorgersen (Master16)  
 M Therkildsen (Master15)  
 P Nybroe (Master15)  
 J Otten (Master15)  
 J Bjerre (Master15)



J Herp (Master13)  
 U Poulsen (Assist Prof)

M Schäfer (Carlsberg PostDoc)  
 M Victoria (PostDoc)  
 M Dahl (Master15 + PhD18)  
 B Tranberg (Master15 + PhD19)  
 H Liu (Master16 + PhD19)  
 S Kozarcanin (Master15 + PhD19)  
 K Zhu (PhD20)  
 J Kruse (Master18)  
 S Siggaard (Master17)  
 M Kofoed (Master16)  
 L Schwenk\_Nebbe (Master16)  
 M Janum (Master16)  
 M Raunbak (Master16)  
 C Poulsen (Master16)  
 N Skou-Nielsen (Master15)  
 M Hansen (Master15)  
 K Holm (Master15)  
 E Eriksen (Master15)  
 A Thomsen (Master14)  
 B Sairanen (Master14)  
 T Jensen (Master13)  
 T Zeyer (Master13)  
 A Søndergaard (Master13)  
 R Rodriguez (PhD14)  
 M Rasmussen (PostDoc11)

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- T Brown et.al.: *Synergies of sector coupling and transmission extension in a cost-optimised highly renewable European energy system*, **Energy** (2018) submitted.

# Research-driven Teaching (ENG + PHY)

**Regular:**            **Fluid Dynamics + Turbulence (10 ECTS),**  
                         **Wind Energy (5 ECTS),**  
                         Thermodynamics + Heat Transfer (10 ECTS),  
                         Turbomachinery + Compressible Fluids (5 ECTS).

**Occasional:**      **Statistical Turbulence (5 ECTS),**  
                         **Complex Networks (5 ECTS),**  
                         **Renewable Energy Networks (5 ECTS).**